

Chapter 323

Assurance for Equivalence Tests for the Ratio of Two Proportions

Introduction

This procedure calculates the assurance of equivalence tests of the ratio of two independent proportions. Schuirmann's (1987) two one-sided tests (TOST) approach is used to test equivalence. Only a brief introduction to the subject will be given here. For a comprehensive discussion, refer to Chow and Liu (1999).

The assurance calculation is based on a user-specified prior distribution of the effect size parameters. This procedure may also be used to determine the needed sample size to obtain a specified assurance.

The methods for assurance calculation in this procedure are based on O'Hagan, Stevens, and Campbell (2005).

Assurance

The assurance of a design is the expected value of the power with respect to one or more prior distributions of the design parameters. Assurance is also referred to as *Bayesian assurance*, *expected power*, *average power*, *statistical assurance*, *hybrid classical-Bayesian procedure*, or *probability of success*.

The power of a design is the probability of rejecting the null hypothesis, conditional on a given set of design attributes, such as the test statistic, the significance level, the sample size, and the effect size to be detected. As the effect size parameters are typically unknown quantities, the stated power may be very different from the true power if the specified parameter values are inaccurate.

While power is conditional on individual design parameter values, and is highly sensitive to those values, assurance is the average power across a presumed prior distribution of the effect size parameters. Thus, assurance adds a Bayesian element to the frequentist framework, resulting in a hybrid approach to the probability of trial or study success. It should be noted that when it comes time to perform the statistical test on the resulting data, these methods for calculating assurance assume that the traditional (frequentist) tests will be used.

The next section describes some of the ways in which the prior distributions for effect size parameters may be determined.

Elicitation

In order to calculate assurance, a suitable prior distribution for the effect size parameters must be determined. This process is called the *elicitation* of the prior distribution.

The elicitation may be as simple as choosing a distribution that seems plausible for the parameter(s) of interest, or as complex as combining the informed advice of several experts based on experience in the field, available pilot data, or previous studies. The accuracy of the assurance value depends on the accuracy of the elicited prior distribution. The assumption (or hope) is that an informed prior distribution will produce a more accurate estimate of the probability of trial success than a single value estimate. Because clinical trials and other studies are often costly, many institutions now routinely require an elicitation step.

Two reference texts that focus on elicitation are O'Hagan, Buck, Daneshkhah, Eiser, Garthwaite, Jenkinson, Oakley, and Rakow (2006) and Dias, Morton, and Quigley (2018).

Test Procedure

Suppose you have two populations from which dichotomous (binary) responses will be recorded. The probability (or risk) of obtaining the event of interest in population 1 (the treatment group) is P_1 and in population 2 (the control group) is P_2 . The corresponding failure proportions are given by $Q_1 = 1 - P_1$ and $Q_2 = 1 - P_2$.

The assumption is made that the responses from each group follow a binomial distribution. This means that the event probability, P_i , is the same for all subjects within the group and that the response from one subject is independent of that of any other subject.

Random samples of N_1 and N_2 individuals are obtained from these two populations. The data from these samples can be displayed in a 2-by-2 contingency table as follows

Group	Success	Failure	Total
Treatment	x_{11}	x_{12}	N_1
Control	x_{21}	x_{22}	N_2
Total	M_1	M_2	N

The binomial proportions P_1 and P_2 are estimated from these data using the formulae

$$\hat{P}_1 = \frac{x_{11}}{N_1}$$

$$\hat{P}_2 = \frac{x_{21}}{N_2}$$

In the following discussion, let $P_{1.0} = P_1|H_0$ and $P_{1.1} = P_1|H_1$. The value of P_2 remains the same for both hypotheses, so $P_2 = P_2|H_0 = P_2|H_1$.

Equivalence Test

An *equivalence test* tests that two groups are not different by more than a small, negligible amount. The ratio is a popular way to compare two proportions. It is easy to interpret and communicate. It gives the relative impact of the treatment. However, there are subtle difficulties that can arise with its interpretation.

Equivalence Test Hypotheses

PASS follows the *two one-sided tests* approach described by Schuirmann (1987) and Phillips (1990). Let $R = P_1/P_2$ represent the ratio of the two group proportions. Lower and upper equivalence bounds, $R_{0,L}$ and $R_{0,U}$, define the region of equivalence.

With $R_{0,L} < 1$ and $R_{0,U} > 1$, the null hypothesis of non-equivalence is

$$H_0: R \leq R_{0,L} \text{ or } R \geq R_{0,U}.$$

The alternative hypothesis of equivalence is

$$H_1: R_{0,L} < R < R_{0,U}.$$

Test Statistics

Several test statistics have been proposed for testing whether the difference, ratio, or odds ratio are different from a specified value. The main difference among the several test statistics is in the formula used to compute the standard error used in the denominator.

Following is a list of the test statistics available in **PASS** for testing proportion ratios. You should use the test statistic that you will use to analyze your data. You may choose a method because it is a standard in your industry, because it seems to have better statistical properties, or because your statistical package calculates it. Whatever your reasons for selecting a certain test statistic, you should use the same test statistic during power or sample calculations.

Miettinen and Nurminen's Likelihood Score Test

Miettinen and Nurminen (1985) proposed a test statistic for testing whether the ratio is equal to a specified value, R_0 . The regular MLE's, \hat{p}_1 and \hat{p}_2 , are used in the numerator of the score statistic while MLE's \tilde{p}_1 and \tilde{p}_2 , constrained so that $\tilde{p}_1/\tilde{p}_2 = R_0$, are used in the denominator. A correction factor of $N/(N-1)$ is applied to make the variance estimate less biased. The significance level of the test statistic is based on the asymptotic normality of the score statistic.

The formula for computing this test statistic is

$$z_{MNR} = \frac{\hat{p}_1 / \hat{p}_2 - R_0}{\hat{\sigma}_{MNR}}$$

where

$$\hat{\sigma}_{MNR} = \sqrt{\left(\frac{\tilde{p}_1 \tilde{q}_1}{N_1} + R_0^2 \frac{\tilde{p}_2 \tilde{q}_2}{N_2}\right) \left(\frac{N}{N-1}\right)}$$

$$\tilde{p}_1 = \tilde{p}_2 R_0$$

$$\tilde{p}_2 = \frac{-B - \sqrt{B^2 - 4AC}}{2A}$$

$$A = NR_0$$

$$B = -[N_1 R_0 + x_{11} + N_2 + x_{21} R_0]$$

$$C = M_1$$

Farrington and Manning's Likelihood Score Test

Farrington and Manning (1990) proposed a test statistic for testing whether the ratio is equal to a specified value, R_0 . The regular MLE's, \hat{p}_1 and \hat{p}_2 , are used in the numerator of the score statistic while MLE's \tilde{p}_1 and \tilde{p}_2 , constrained so that $\tilde{p}_1/\tilde{p}_2 = R_0$, are used in the denominator. The significance level of the test statistic is based on the asymptotic normality of the score statistic.

The formula for computing the test statistic is

$$z_{FMR} = \frac{\hat{p}_1 / \hat{p}_2 - R_0}{\sqrt{\left(\frac{\tilde{p}_1 \tilde{q}_1}{N_1} + R_0^2 \frac{\tilde{p}_2 \tilde{q}_2}{N_2}\right) \left(\frac{N}{N-1}\right)}}$$

where the estimates, \tilde{p}_1 and \tilde{p}_2 , are computed as in the corresponding test of Miettinen and Nurminen (1985) given above.

Gart and Nam's Likelihood Score Test

Gart and Nam (1988), page 329, proposed a modification to the Farrington and Manning (1988) ratio test that corrected for skewness. Let $z_{FMR}(R_0)$ stand for the Farrington and Manning ratio test statistic described above. The skewness corrected test statistic, z_{GNR} , is the appropriate solution to the quadratic equation

$$(-\tilde{\psi})z_{GNR}^2 + (-1)z_{GNR} + (z_{FMR}(R_0) + \tilde{\psi}) = 0$$

where

$$\tilde{\psi} = \frac{1}{6\tilde{u}^{3/2}} \left(\frac{\tilde{q}_1(\tilde{q}_1 - \tilde{p}_1)}{N_1^2 \tilde{p}_1^2} - \frac{\tilde{q}_2(\tilde{q}_2 - \tilde{p}_2)}{N_2^2 \tilde{p}_2^2} \right)$$

$$\tilde{u} = \frac{\tilde{q}_1}{N_1 \tilde{p}_1} + \frac{\tilde{q}_2}{N_2 \tilde{p}_2}$$

Power Calculations

The power is calculated using the standard formulas for the z-test. The differences in the results of the above tests occur because of the different formulas that are used for the standard error. To compute the power, the values of \hat{p}_1 and \hat{p}_2 in the test statistic are replaced by the corresponding values of P_1 and P_2 . The power is then computed using the normal approximation to the binomial as presented in Chow et al. (2008).

Assurance Calculation

This assurance computation described here is based on O'Hagan, Stevens, and Campbell (2005).

Let $P'(H|P_1, P_2)$ be the power function described above where H is the event that null hypothesis is rejected conditional on the parameter values. The specification of P_1 and P_2 is critical to the power calculation, but the actual values are seldom known. Assurance is defined as the expected power where the expectation is with respect to a joint prior distribution for the parameters P_1 and P_2 . Hence, the definition of assurance is

$$Assurance = E_{P_1, P_2}(P'(H|P_1, P_2)) = \iint P'(H|P_1, P_2) f(P_1, P_2) dP_1 dP_2$$

where $f(P_1, P_2)$ is the joint prior distribution of P_1 and P_2 .

In **PASS**, the joint prior distribution can be specified as either a discrete approximation to the joint prior distribution, or as individual prior distributions, one for each parameter.

Specifying a Joint Prior Distribution

If the joint prior distribution is to be specified directly, the distribution is specified in **PASS** using a discrete approximation to the function $f(P_1, P_2)$. This provides flexibility in specifying the joint prior distribution. In the two-parameter case, three columns are entered on the spreadsheet: two for the parameters and a third for the probability. Each row gives a value for each parameter and the corresponding parameter-combination probability. The accuracy of the distribution approximation is controlled by the number of points (spreadsheet rows) that are used.

An example of entering a joint prior distribution is included at the end of the chapter.

Specifying Individual Prior Distributions

Ciarleglio, Arendt, and Peduzzi (2016) suggest that more flexibility is available if the joint prior distribution is separated into two independent univariate distributions as follows

$$f(P_1, P_2) = f_1(P_1)f_2(P_2)$$

where $f_1(P_1)$ is the prior distribution of P_1 and $f_2(P_2)$ is the prior distribution of P_2 . This method is also available in **PASS**. In this case, the definition of assurance becomes

$$Assurance = E_{P_1, P_2}(P'(H|P_1, P_2)) = \iint P'(H|P_1, P_2)f_1(P_1)f_2(P_2)dP_1 dP_2$$

Using this definition, the assurance can be calculated using numerical integration. There are a variety of pre-programmed, univariate prior distributions available in **PASS**.

Fixed Values (No Prior) and Custom Values

For any given parameter, **PASS** also provides the option of entering a single fixed value for the prior distribution, or a series of values and corresponding probabilities (using the spreadsheet), rather than one of the pre-programmed distributions.

Numerical Integration in PASS (and Notes on Computation Speed)

When the prior distribution is specified as independent univariate distributions, **PASS** uses a numerical integration algorithm to compute the assurance value as follows:

The domain of each prior distribution is divided into M intervals. Since many of the available prior distributions are unbounded on one (e.g., Gamma) or both (e.g., Normal) ends, an approximation is made to make the domain finite. This is accomplished by truncating the distribution to a domain between the two quantiles: $q_{0.001}$ and $q_{0.999}$.

The value of M controls the accuracy and speed of the algorithm. If only one parameter is to be given a prior distribution, then a value of M between 50 and 100 usually gives an accurate result in a timely manner. However, if two parameters are given priors, the number of iterations needed increases from M to M^2 . For example, if M is 100, 10000 iterations are needed. Reducing M from 100 to 50 reduces the number of iterations from 10000 to 2500.

The algorithm runtime increases when searching for sample size rather than solving for assurance, as a search algorithm is employed in this case. When solving for sample size, we recommend reducing M to 20 or less while exploring various scenarios, and then increasing M to 50 or more for a final, more accurate, result.

List of Available Univariate Prior Distributions

This section lists the univariate prior distributions that may be used for any of the applicable parameters when the Prior Entry Method is set to Individual.

No Prior

If 'No Prior' is chosen for a parameter, the parameter is assumed to take on a single, fixed value with probability one.

Beta (Shape 1, Shape 2, a, c)

A random variable X that follows the beta distribution is defined on a finite interval $[a, c]$. Two shape parameters (α and β) control the shape of this distribution. Two location parameters a and c give the minimum and maximum of X .

The probability density function of the beta distribution is

$$f(x|\alpha, \beta, a, c) = \frac{\left(\frac{x-a}{c-a}\right)^{\alpha-1} \left(\frac{c-x}{c-a}\right)^{\beta-1}}{(c-a)B(\alpha, \beta)}$$

where $B(\alpha, \beta) = \Gamma(\alpha) \Gamma(\beta) / \Gamma(\alpha + \beta)$ and $\Gamma(z)$ is the gamma function.

The mean of X is

$$\mu_X = \frac{\alpha c + \beta a}{\alpha + \beta}$$

Various distribution shapes are controlled by the values of α and β . These include

Symmetric and Unimodal

$$\alpha = \beta > 1$$

U Shaped

$$\alpha = \beta < 1$$

Bimodal

$$\alpha, \beta < 1$$

Uniform

$$\alpha = \beta = 1$$

Parabolic

$$\alpha = \beta = 2$$

Bell-Shaped

$$\alpha = \beta > 2$$

Gamma (Shape, Scale)

A random variable X that follows the gamma distribution is defined on the interval $(0, \infty)$. A shape parameter, κ , and a scale parameter, θ , control the distribution.

The probability density function of the gamma distribution is

$$f(x|\kappa, \theta) = \frac{x^{\kappa-1} e^{-\frac{x}{\theta}}}{\theta^{\kappa} \Gamma(\kappa)}$$

where $\Gamma(z)$ is the gamma function.

The mean of X is

$$\mu_X = \frac{\kappa}{\theta}$$

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(Min \leq X \leq Max)$ where Min and Max are two truncation bounds.

Inverse-Gamma (Shape, Scale)

A random variable X that follows the inverse-gamma distribution is defined on the interval $(0, \infty)$. If $Y \sim \text{gamma}$, then $X = 1 / Y \sim \text{inverse-gamma}$. A shape parameter, α , and a scale parameter, β , control the distribution.

The probability density function of the inverse-gamma distribution is

$$f(x|\alpha, \beta) = \frac{\beta^{\alpha} x^{\alpha-1} e^{-\frac{\beta}{x}}}{\Gamma(\alpha)}$$

where $\Gamma(z)$ is the gamma function.

The mean of X is

$$\mu_X = \frac{\beta}{\alpha - 1} \text{ for } \alpha > 1$$

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(Min \leq X \leq Max)$ where Min and Max are two truncation bounds.

Logistic (Location, Scale)

A random variable X that follows the logistic distribution is defined on the interval $(-\infty, \infty)$. A location parameter, μ , and a scale parameter, s , control the distribution.

The probability density function of the logistic distribution is

$$f(x|\mu, s) = \frac{e^{-\frac{x-\mu}{s}}}{s \left(1 + e^{-\frac{x-\mu}{s}}\right)^2}$$

The mean of X is

$$\mu_X = \mu$$

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(Min \leq X \leq Max)$ where Min and Max are two truncation bounds.

Lognormal (Mean, SD)

A random variable X that follows the lognormal distribution is defined on the interval $(0, \infty)$. A location parameter, $\mu_{\log(X)}$, and a scale parameter, $\sigma_{\log(X)}$, control the distribution. If $Z \sim$ standard normal, then $X = e^{\mu + \sigma Z} \sim$ lognormal. Note that $\mu_{\log(X)} = E(\log(X))$ and $\sigma_{\log(X)} = \text{Standard Deviation}(\log(X))$.

The probability density function of the lognormal distribution is

$$f(x|\mu, \sigma) = \frac{e^{-\frac{1}{2}\left(\frac{\log x - \mu}{\sigma}\right)^2}}{x\sigma\sqrt{2\pi}}$$

The mean of X is

$$\mu_X = e^{\mu + \frac{\sigma^2}{2}}$$

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(Min \leq X \leq Max)$ where Min and Max are two truncation bounds.

LogT (Mean, SD)

A random variable X that follows the logT distribution is defined on the interval $(0, \infty)$. A location parameter, $\mu_{\log(X)}$, a scale parameter, $\sigma_{\log(X)}$, and a shape parameter, ν , control the distribution. Note that ν is referred to as the *degrees of freedom*.

If $t \sim \text{Student's } t$, then $X = e^{\mu + \sigma t} \sim \text{logT}$.

The probability density function of the logT distribution is

$$f(x|\mu, \sigma, \nu) = \frac{\Gamma\left(\frac{\nu+1}{2}\right)}{x\Gamma\left(\frac{\nu}{2}\right)\sigma\sqrt{\nu\pi}} \left(1 + \frac{1}{\nu} \left(\frac{\log x - \mu}{\sigma}\right)^2\right)^{\left(\frac{-\nu-1}{2}\right)}$$

The mean of X is not defined.

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(\text{Min} \leq X \leq \text{Max})$ where Min and Max are two truncation bounds.

Normal (Mean, SD)

A random variable X that follows the normal distribution is defined on the interval $(-\infty, \infty)$. A location parameter, μ , and a scale parameter, σ , control the distribution.

The probability density function of the normal distribution is

$$f(x|\mu, \sigma) = \frac{e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}}{\sigma\sqrt{2\pi}}$$

The mean of X is

$$\mu_X = \mu$$

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(\text{Min} \leq X \leq \text{Max})$ where Min and Max are two truncation bounds.

T (Mean, SD, DF)

A random variable X that follows Student's t distribution is defined on the interval $(-\infty, \infty)$. A location parameter, μ , a scale parameter, σ , and a shape parameter, ν , control the distribution. Note that ν is referred to as the *degrees of freedom* or *DF*.

The probability density function of the Student's t distribution is

$$f(x|\mu, \sigma, \nu) = \frac{\Gamma\left(\frac{\nu+1}{2}\right)}{\Gamma\left(\frac{\nu}{2}\right)\sigma\sqrt{\nu\pi}} \left(1 + \frac{1}{\nu} \left(\frac{x-\mu}{\sigma}\right)^2\right)^{\left(\frac{-\nu-1}{2}\right)}$$

The mean of X is μ if $\nu > 1$.

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(\text{Min} \leq X \leq \text{Max})$ where Min and Max are two truncation bounds.

Triangle (Mode, Min, Max)

Let a = minimum, b = maximum, and c = mode. A random variable X that follows a triangle distribution is defined on the interval (a, b) .

The probability density function of the triangle distribution is

$$f(x|a, b, c) = \begin{cases} \frac{2(x-a)}{(b-a)(c-a)} & \text{for } a \leq x < c \\ \frac{2}{b-a} & \text{for } x = c \\ \frac{2(b-x)}{(b-a)(b-c)} & \text{for } c < x \leq b \end{cases}$$

The mean of X is

$$\frac{a + b + c}{3}$$

Uniform (Min, Max)

Let a = minimum and b = maximum. A random variable X that follows a uniform distribution is defined on the interval $[a, b]$.

The probability density function of the uniform distribution is

$$f(x|a, b) = \begin{cases} \frac{1}{b-a} & \text{for } a \leq x \leq b \end{cases}$$

The mean of X is

$$\frac{a + b}{2}$$

Weibull (Shape, Scale)

A random variable X that follows the Weibull distribution is defined on the interval $(0, \infty)$. A shape parameter, κ , and a scale parameter, λ , control the distribution.

The probability density function of the Weibull distribution is

$$f(x|\kappa, \lambda) = \frac{\kappa}{\lambda} \left(\frac{x}{\lambda}\right)^{\kappa-1} e^{-\left(\frac{x}{\lambda}\right)^{\kappa}}$$

The mean of X is

$$\mu_X = \kappa \Gamma\left(1 + \frac{1}{\kappa}\right)$$

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(\text{Min} \leq X \leq \text{Max})$ where Min and Max are two truncation bounds.

Custom (Values and Probabilities in Spreadsheet)

This custom prior distribution is represented by a set of user-specified points and associated probabilities, entered in two columns of the spreadsheet. The points make up the entire set of values that are used for this parameter in the calculation of assurance. The associated probabilities should sum to one. Note that custom values and probabilities can be used to approximate any continuous distribution.

For example, a prior distribution of X might be

X_i	P_i
10	0.2
20	0.2
30	0.3
40	0.2
50	0.1

In this example, the mean of X is

$$\mu_X = \sum_{i=1}^5 X_i P_i$$

Example 1 – Assurance Over a Range of Sample Sizes

Suppose a study is being conducted to show that a drug produced by a new supplier is equivalent the drug produced by the current supplier.

Researchers conducted a power analysis using the PASS procedure *Equivalence Tests for the Ratio of Two Proportions* and determined that an appropriate sample size needed to achieve the 80% power at the 0.05 significance level when using the Farrington and Manning score test. The baseline cure rate is 0.40. The cure rate of the new drug is anticipated to be about 0.41 as well. The equivalence ratios are set at 0.8 and 1.25.

To complete their sample size study, the researchers want to run an assurance analysis for a range of group sample sizes from 300 to 2000. An elicitation exercise determined that the prior distribution of the P1 should be normal with mean 0.40 and standard deviation 0.04. The elicitation also concluded that prior distribution of P2 should be normal with mean 0.41 and standard deviation 0.02.

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 1** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Design Tab

Solve For	Assurance
Prior Entry Method	Individual (Enter a prior distribution for each applicable parameter)
Test Type	Likelihood Score (Farrington & Manning)
Alpha	0.05
Group Allocation	Equal (N1 = N2)
Sample Size Per Group	300 700 1100 1500 2000
R0.U (Upper Equivalence Ratio)	1.25
R0.L (Lower Equivalence Ratio)	0.8
Prior Distribution of P1	Normal (Mean, SD)
Mean	0.40
SD	0.04
Truncation Boundaries	None
Prior Distribution of P2	Normal (Mean, SD)
Mean	0.41
SD	0.02
Truncation Boundaries	None

Options Tab

Number of Computation Points for each	20
Prior Distribution	
Maximum N1 in Sample Size Search	5000

Assurance for Equivalence Tests for the Ratio of Two Proportions

Output

Click the Calculate button to perform the calculations and generate the following output.

Numeric Reports

Numeric Results

Solve For: [Assurance](#)

Test Statistic: Farrington & Manning Likelihood Score Test

Hypotheses: $H_0: P_1 / P_2 \leq R_{0.L} \text{ or } P_1 / P_2 \geq R_{0.U}$ vs. $H_1: R_{0.L} < P_1 / P_2 < R_{0.U}$

Prior Type: Independent Univariate Distributions

Prior Distributions

P1: Normal (Mean = 0.4, SD = 0.04).

P2: Normal (Mean = 0.41, SD = 0.02).

Assurance*	Power‡	Sample Size			Expected Group 1 Proportion E(P1)	Expected Group 2 Proportion E(P2)	Ratio of Proportions			
							Equivalence			
		N1	N2	N			H1 R1	Lower R0.L	Upper R0.U	Alpha
0.31251	0.44095	300	300	600	0.4	0.41	0.97561	0.8	1.25	0.05
0.62653	0.90399	700	700	1400	0.4	0.41	0.97561	0.8	1.25	0.05
0.72942	0.98409	1100	1100	2200	0.4	0.41	0.97561	0.8	1.25	0.05
0.77940	0.99746	1500	1500	3000	0.4	0.41	0.97561	0.8	1.25	0.05
0.81447	0.99976	2000	2000	4000	0.4	0.41	0.97561	0.8	1.25	0.05

* The number of points used for computation of the prior(s) was 20.

‡ Power was calculated using $P_1 = E(P_1) = 0.4$ and $P_2 = E(P_2) = 0.41$.

Assurance	The expected power where the expectation is with respect to the prior distribution(s).
Power	The power calculated using the parameter values shown in the footnote. Note that these parameter values may be different from those shown in the report.
N1	The number of subjects in group 1.
N2	The number of subjects in group 2.
N	The total sample size. $N = N_1 + N_2$.
E(P1)	The expected value over its prior distribution of the group 1 response proportion.
E(P2)	The expected value over its prior distribution of the group 2 response proportion.
R1	The ratio of the two proportions assumed by the alternative hypothesis.
R0.L	The lower equivalence ratio of the two proportions.
R0.U	The upper equivalence ratio of the two proportions.
Alpha	The probability of rejecting a true null hypothesis.

Summary Statements

A parallel two-group design will be used to test whether the Group 1 (treatment) proportion (P1) is equivalent to the Group 2 (control) proportion (P2), with proportion ratio equivalence bounds of 0.8 and 1.25 ($H_0: P_1 / P_2 \leq 0.8 \text{ or } P_1 / P_2 \geq 1.25$ versus $H_1: 0.8 < P_1 / P_2 < 1.25$). The comparison will be made using two one-sided, two-sample Farrington & Manning Likelihood Score tests of the ratio, with an overall Type I error rate (α) of 0.05. The prior distribution used for the Group 1 proportion is Normal (Mean = 0.4, SD = 0.04). The prior distribution used for the Group 2 proportion is Normal (Mean = 0.41, SD = 0.02). With sample sizes of 300 for Group 1 (treatment) and 300 for Group 2 (control), the assurance (average power) is 0.31251.

Assurance for Equivalence Tests for the Ratio of Two Proportions

Dropout-Inflated Sample Size

Dropout Rate	Sample Size			Dropout-Inflated Enrollment Sample Size			Expected Number of Dropouts		
	N1	N2	N	N1'	N2'	N'	D1	D2	D
20%	300	300	600	375	375	750	75	75	150
20%	700	700	1400	875	875	1750	175	175	350
20%	1100	1100	2200	1375	1375	2750	275	275	550
20%	1500	1500	3000	1875	1875	3750	375	375	750
20%	2000	2000	4000	2500	2500	5000	500	500	1000

Dropout Rate	The percentage of subjects (or items) that are expected to be lost at random during the course of the study and for whom no response data will be collected (i.e., will be treated as "missing"). Abbreviated as DR.
N1, N2, and N	The evaluable sample sizes at which power is computed (as entered by the user). If N1 and N2 subjects are evaluated out of the N1' and N2' subjects that are enrolled in the study, the design will achieve the stated power.
N1', N2', and N'	The number of subjects that should be enrolled in the study in order to obtain N1, N2, and N evaluable subjects, based on the assumed dropout rate. N1' and N2' are calculated by inflating N1 and N2 using the formulas $N1' = N1 / (1 - DR)$ and $N2' = N2 / (1 - DR)$, with N1' and N2' always rounded up. (See Julious, S.A. (2010) pages 52-53, or Chow, S.C., Shao, J., Wang, H., and Lohknygina, Y. (2018) pages 32-33.)
D1, D2, and D	The expected number of dropouts. $D1 = N1' - N1$, $D2 = N2' - N2$, and $D = D1 + D2$.

Dropout Summary Statements

Anticipating a 20% dropout rate, 375 subjects should be enrolled in Group 1, and 375 in Group 2, to obtain final group sample sizes of 300 and 300, respectively.

References

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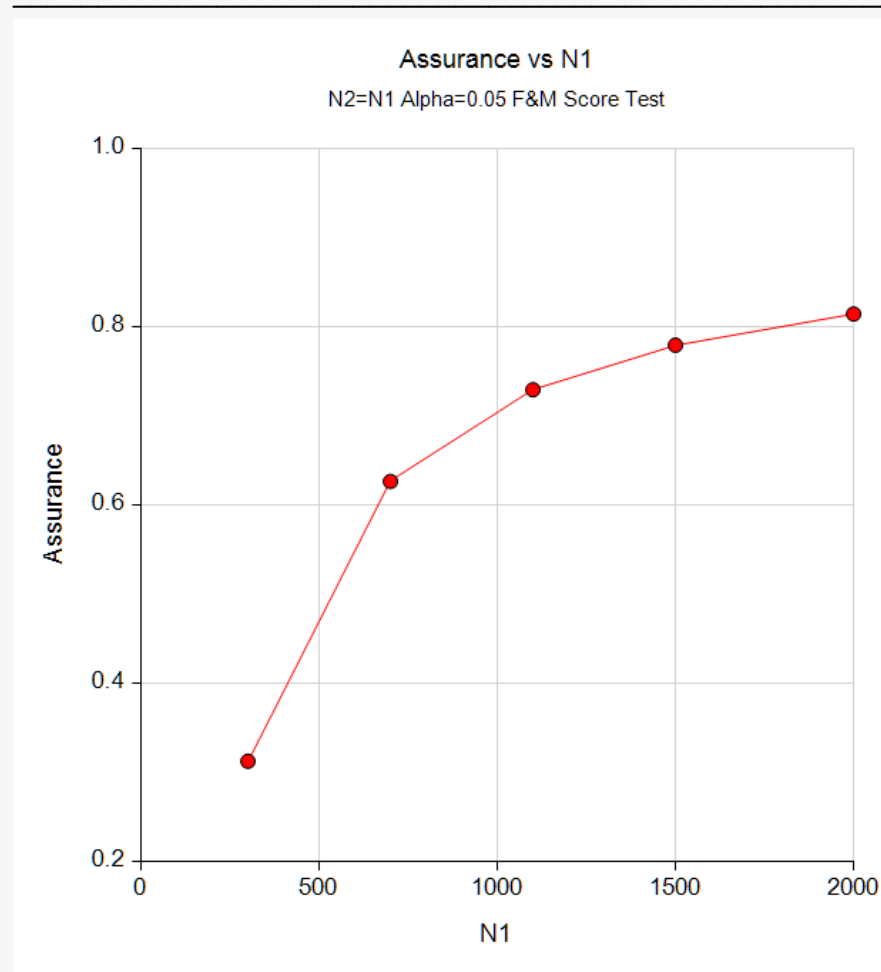
Assurance for Equivalence Tests for the Ratio of Two Proportions

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This report shows the assurance values obtained by the various sample sizes.

Plots Section

Plots

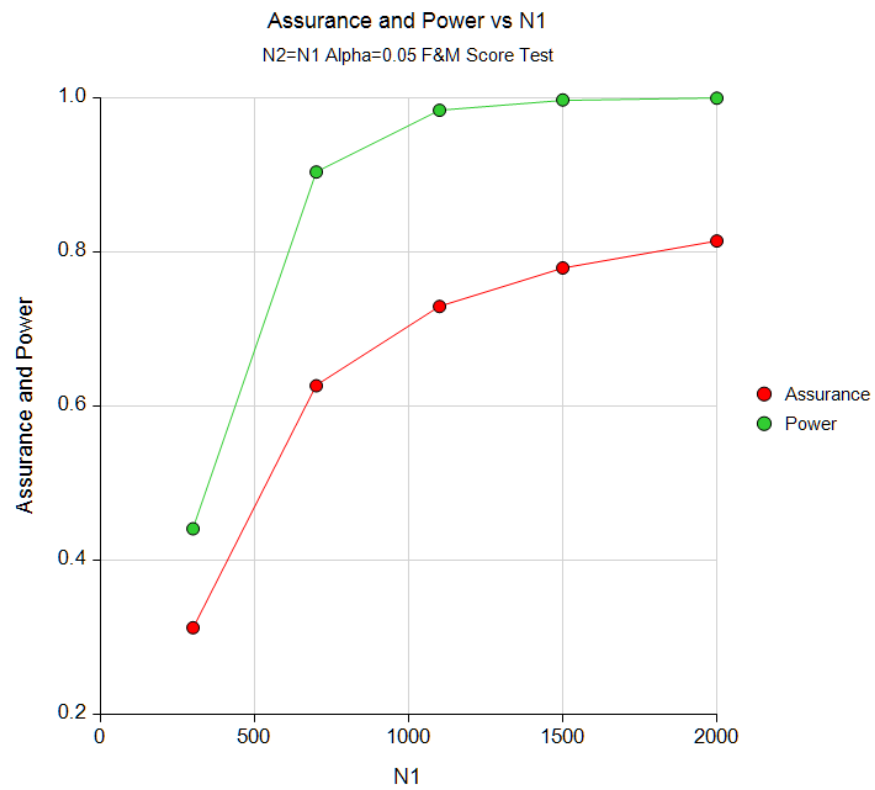


This plot shows the relationship between the assurance and sample size.

Assurance for Equivalence Tests for the Ratio of Two Proportions

Comparison Plots Section

Comparison Plots



This plot compares the assurance and power across values of sample size.

Example 2 – Validation using Hand Computation

We could not find a validation example in the literature, so we have developed a validation example of our own.

Suppose a Farrington and Manning Likelihood Score test is used in which $N1 = N2 = 1000$ and the significance level is 0.05. Further suppose that the equivalence ratios are 0.80 and 1.25.

The prior distribution of P1.1 is approximated by the following table.

<u>P1.1</u>	<u>Prob</u>
0.38	0.3
0.44	0.4
0.50	0.3

The prior distribution of P2 is approximated by the following table.

<u>P2</u>	<u>Prob</u>
0.42	0.2
0.44	0.6
0.46	0.2

Note that in both of these tables, the parameter values are equi-spaced. This is important when using a discrete approximation such as we have here.

The *Equivalence Tests for the Ratio of Two Proportions* procedure is used to compute the power for each of the nine combinations of P1 and P2. The results of these calculations are shown next.

Numeric Results

Solve For: [Power](#)
 Groups: 1 = Treatment, 2 = Reference
 Test Statistic: Farrington & Manning Likelihood Score Test
 Hypotheses: $H0: P1 / P2 \leq R0.L \text{ or } P1 / P2 \geq R0.U$ vs. $H1: R0.L < P1 / P2 < R0.U$

Power*	Sample Size			Proportions				Ratio			
				Equivalence		Actual P1.1	Reference P2	Equivalence		Actual R1	Alpha
	N1	N2	N	Lower P1.0L	Upper P1.0U			Lower R0.L	Upper R0.U		
0.72215	1000	1000	2000	0.336	0.525	0.38	0.42	0.8	1.25	0.90476	0.05
0.41061	1000	1000	2000	0.352	0.550	0.38	0.44	0.8	1.25	0.86364	0.05
0.14973	1000	1000	2000	0.368	0.575	0.38	0.46	0.8	1.25	0.82609	0.05
0.96082	1000	1000	2000	0.336	0.525	0.44	0.42	0.8	1.25	1.04762	0.05
0.99398	1000	1000	2000	0.352	0.550	0.44	0.44	0.8	1.25	1.00000	0.05
0.97392	1000	1000	2000	0.368	0.575	0.44	0.46	0.8	1.25	0.95652	0.05
0.25945	1000	1000	2000	0.336	0.525	0.50	0.42	0.8	1.25	1.19048	0.05
0.63569	1000	1000	2000	0.352	0.550	0.50	0.44	0.8	1.25	1.13636	0.05
0.90885	1000	1000	2000	0.368	0.575	0.50	0.46	0.8	1.25	1.08696	0.05

* Power was computed using the normal approximation method.

The assurance calculation is made by summing the quantities $\left[(power_{i,j}) (p(P1_i)) (p(P2_j)) \right]$ as follows

$$Assurance = (0.72215 \times 0.3 \times 0.2) + (0.41061 \times 0.3 \times 0.6) + \dots + (0.90885 \times 0.3 \times 0.2) = 0.704079.$$

Assurance for Equivalence Tests for the Ratio of Two Proportions

To run this example, the spreadsheet will need to be loaded with the following four columns in which the first two are for P1 and the second two are for P2.

C1	C2	C3	C4
0.38	0.3	0.42	0.2
0.44	0.4	0.44	0.6
0.50	0.3	0.46	0.2

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 2** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Design Tab

Solve For	Assurance
Prior Entry Method	Individual (Enter a prior distribution for each applicable parameter)
Test Type	Likelihood Score (Farrington & Manning)
Alpha	0.05
Group Allocation	Equal (N1 = N2)
Sample Size Per Group	1000
R0.U (Upper Equivalence Ratio)	1.25
R0.L (Lower Equivalence Ratio)	0.8
Prior Distribution of P1	Custom (Values and Probabilities in Spreadsheet)
Column of Values	C1
Column of Pr(Values)	C2
Prior Distribution of P2	Custom (Values and Probabilities in Spreadsheet)
Column of Values	C3
Column of Pr(Values)	C4

Options Tab

Number of Computation Points for each	20
Prior Distribution	
Maximum N1 in Sample Size Search	5000

Input Spreadsheet Data

Row	C1	C2	C3	C4
1	0.38	0.3	0.42	0.2
2	0.44	0.4	0.44	0.6
3	0.50	0.3	0.46	0.2

Assurance for Equivalence Tests for the Ratio of Two Proportions

Output

Click the Calculate button to perform the calculations and generate the following output.

Numeric Results

Solve For: [Assurance](#)

Test Statistic: Farrington & Manning Likelihood Score Test

Hypotheses: $H_0: P_1 / P_2 \leq R_{0.L} \text{ or } P_1 / P_2 \geq R_{0.U}$ vs. $H_1: R_{0.L} < P_1 / P_2 < R_{0.U}$

Prior Type: Independent Univariate Distributions

Prior Distributions

P1: Point List (Values = C1, Probs = C2).

C1: 0.38 0.44 0.5

C2: 0.3 0.4 0.3

P2: Point List (Values = C3, Probs = C4).

C3: 0.42 0.44 0.46

C4: 0.2 0.6 0.2

		Ratio of Proportions								
		Sample Size			Expected Group 1 Proportion E(P1)	Expected Group 2 Proportion E(P2)	Equivalence			Alpha
Assurance	Power‡	N1	N2	N			H1 R1	Lower R0.L	Upper R0.U	
0.70407	0.99398	1000	1000	2000	0.44	0.44	1	0.8	1.25	0.05

‡ Power was calculated using $P_1 = E(P_1) = 0.44$ and $P_2 = E(P_2) = 0.44$.

PASS has also calculated the assurance as 0.70407 which is within rounding of 0.704079. This validates the procedure.

Example 3 – Finding the Sample Size Needed to Achieve a Specified Assurance

Continuing with Example 1, the researchers want to investigate the sample sizes necessary to achieve assurances of 0.4, 0.5, 0.6, 0.7, and 0.8.

In order to reduce the runtime during this exploratory phase of the analysis, the number of points in the prior computation is set to 20. This slightly reduces the accuracy, but greatly reduces the runtime.

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 3** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Design Tab

Solve For	Sample Size
Prior Entry Method	Individual (Enter a prior distribution for each applicable parameter)
Test Type	Likelihood Score (Farrington & Manning)
Assurance	0.4 0.5 0.6 0.7 0.8
Alpha	0.05
Group Allocation	Equal (N1 = N2)
R0.U (Upper Equivalence Ratio)	1.25
R0.L (Lower Equivalence Ratio)	0.8
Prior Distribution of P1	Normal (Mean, SD)
Mean	0.40
SD	0.04
Truncation Boundaries	None
Prior Distribution of P2	Normal (Mean, SD)
Mean	0.41
SD02
Truncation Boundaries	None

Options Tab

Number of Computation Points for each	20
Prior Distribution	
Maximum N1 in Sample Size Search	5000

Assurance for Equivalence Tests for the Ratio of Two Proportions

Output

Click the Calculate button to perform the calculations and generate the following output.

Numeric Reports

Numeric Results

Solve For: [Sample Size](#)

Test Statistic: Farrington & Manning Likelihood Score Test

Hypotheses: $H_0: P_1 / P_2 \leq R_{0.L} \text{ or } P_1 / P_2 \geq R_{0.U}$ vs. $H_1: R_{0.L} < P_1 / P_2 < R_{0.U}$

Prior Type: Independent Univariate Distributions

Prior Distributions

P1: Normal (Mean = 0.4, SD = 0.04).

P2: Normal (Mean = 0.41, SD = 0.02).

Assurance*			Sample Size			Expected Group 1 Proportion E(P1)	Expected Group 2 Proportion E(P2)	Ratio of Proportions			
								Equivalence			Alpha
Actual	Target	Power‡	N1	N2	N			H1 R1	Lower R0.L	Upper R0.U	
0.40039	0.4	0.57931	366	366	732	0.4	0.41	0.97561	0.8	1.25	0.05
0.50070	0.5	0.73556	472	472	944	0.4	0.41	0.97561	0.8	1.25	0.05
0.60016	0.6	0.87340	638	638	1276	0.4	0.41	0.97561	0.8	1.25	0.05
0.70016	0.7	0.96855	949	949	1898	0.4	0.41	0.97561	0.8	1.25	0.05
0.80004	0.8	0.99925	1760	1760	3520	0.4	0.41	0.97561	0.8	1.25	0.05

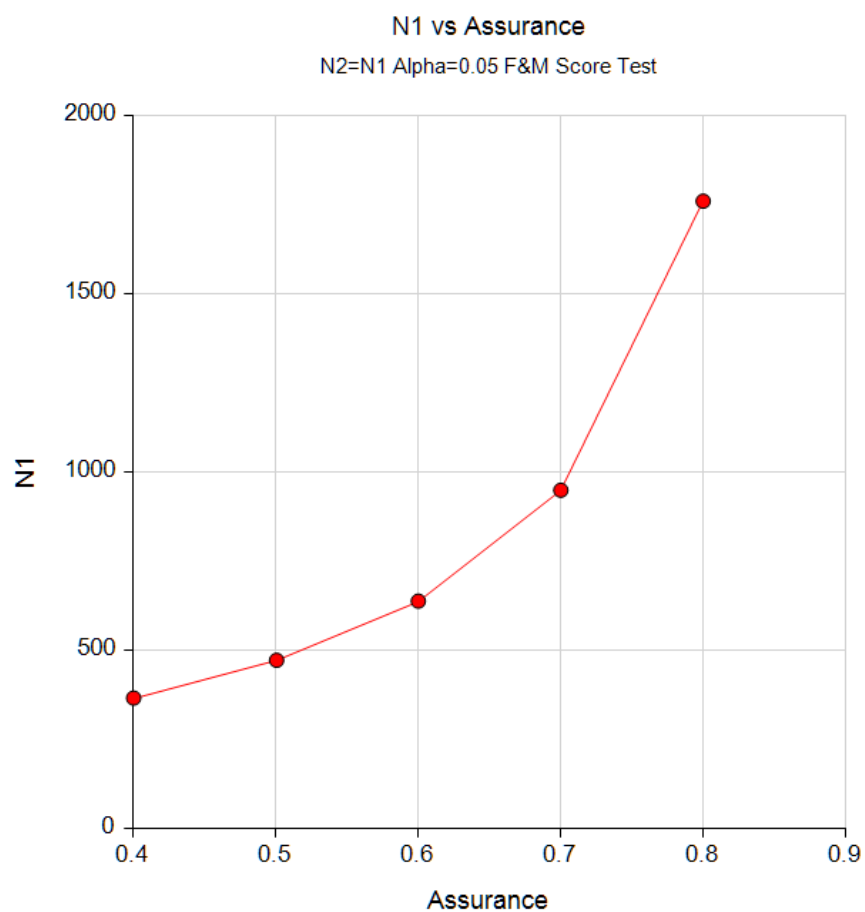
* The number of points used for computation of the prior(s) was 20.

‡ Power was calculated using $P_1 = E(P_1) = 0.4$ and $P_2 = E(P_2) = 0.41$.

This report shows the required sample size for each assurance target.

Plots Section

Plots



This plot shows the relationship between the sample size and assurance.

Example 4 – Joint Prior Distribution

The following example shows the complexity required to specify a joint distribution for two parameters.

Suppose a likelihood-score (Farrington and Manning) test is used in an equivalence study. In this study, $N_1 = N_2 = 2000$, the significance level is 0.05, and the equivalence ratios are 0.80 and 1.25.

Further suppose that the joint prior distribution of the P1 (treatment) and P2 (control) is approximated by the following table. In a real study, the values in this table would be provided by an elicitation study.

Note that the program will rescale the probabilities so they sum to one.

P1	P2	Prob
0.32	0.34	0.05
0.36	0.34	0.10
0.44	0.34	0.25
0.34	0.35	0.20
0.37	0.35	0.25
0.45	0.35	0.40
0.34	0.36	0.50
0.38	0.36	0.55
0.46	0.36	0.70
0.35	0.37	0.50
0.39	0.37	0.55
0.47	0.37	0.70
0.36	0.38	0.20
0.40	0.38	0.25
0.48	0.38	0.40
0.37	0.39	0.05
0.41	0.39	0.10
0.49	0.39	0.25

To run this example, the spreadsheet will need to be loaded with the following four columns.

C1	C2	C3
0.32	0.34	0.05
0.36	0.34	0.10
0.44	0.34	0.25
0.34	0.35	0.20
0.37	0.35	0.25
0.45	0.35	0.40
0.34	0.36	0.50
0.38	0.36	0.55
0.46	0.36	0.70
0.35	0.37	0.50
0.39	0.37	0.55
0.47	0.37	0.70
0.36	0.38	0.20
0.40	0.38	0.25
0.48	0.38	0.40

Assurance for Equivalence Tests for the Ratio of Two Proportions

0.37 0.39 0.05
 0.41 0.39 0.10
 0.49 0.39 0.25

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 4** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Design Tab

Solve For **Assurance**
 Prior Entry Method **Combined (Enter parameter values and probabilities on spreadsheet)**
 Test Type **Likelihood Score (Farrington & Manning)**
 Alpha **0.05**
 Group Allocation **Equal (N1 = N2)**
 Sample Size Per Group **2000**
 R0.U (Upper Equivalence Ratio) **1.25**
 R0.L (Lower Equivalence Ratio) **0.8**
 Column of P1 Values **C1**
 Column of P2 Values **C2**
 Column of Pr(Values) **C3**

Options Tab

Number of Computation Points for each **20**
 Prior Distribution
 Maximum N1 in Sample Size Search **5000**

Input Spreadsheet Data

Row	C1	C2	C3
1	0.32	0.34	0.05
2	0.36	0.34	0.10
3	0.44	0.34	0.25
4	0.34	0.35	0.20
5	0.37	0.35	0.25
6	0.45	0.35	0.40
7	0.34	0.36	0.50
8	0.38	0.36	0.55
9	0.46	0.36	0.70
10	0.35	0.37	0.50
11	0.39	0.37	0.55
12	0.47	0.37	0.70
13	0.36	0.38	0.20
14	0.40	0.38	0.25
15	0.48	0.38	0.40
16	0.37	0.39	0.05
17	0.41	0.39	0.10
18	0.49	0.39	0.25

Assurance for Equivalence Tests for the Ratio of Two Proportions

Output

Click the Calculate button to perform the calculations and generate the following output.

Numeric Results

Solve For: [Assurance](#)

Test Statistic: Farrington & Manning Likelihood Score Test

Hypotheses: $H_0: P_1 / P_2 \leq R_{0.L} \text{ or } P_1 / P_2 \geq R_{0.U}$ vs. $H_1: R_{0.L} < P_1 / P_2 < R_{0.U}$

Prior Type: Joint Multivariate Distribution

Prior Distribution

Point Lists

P1: C1: 0.32 0.36 0.44 0.34 0.37 0.45 0.34 0.38 0.46 0.35 0.39 0.47 0.36 0.4 0.48 0.37 0.41 0.49

P2: C2: 0.34 0.34 0.34 0.35 0.35 0.35 0.36 0.36 0.36 0.37 0.37 0.37 0.38 0.38 0.38 0.39 0.39 0.39

Prob: C3: 0.05 0.1 0.25 0.2 0.25 0.4 0.5 0.55 0.7 0.5 0.55 0.7 0.2 0.25 0.4 0.05 0.1 0.25

		Ratio of Proportions								
Assurance	Power‡	Sample Size			Expected Group 1 Proportion E(P1)	Expected Group 2 Proportion E(P2)	Equivalence			Alpha
		N1	N2	N			H1 R1	Lower R0.L	Upper R0.U	
0.55314	0.82853	2000	2000	4000	0.41133	0.365	1.12694	0.8	1.25	0.05

‡ Power was calculated using $P_1 = E(P_1) = 0.41133$ and $P_2 = E(P_2) = 0.365$.

PASS has calculated the assurance as 0.55314.

Example 5 – Joint Prior Validation

The settings given in Example 2 will be used to validate the joint prior distribution method. This will be done by running the independent-prior scenario used in that example through the joint-prior method and checking that the assurance values match.

In Example 2, the prior distributions of the P1 and P2 are

<u>P1</u>	<u>Prob</u>
0.38	0.3
0.44	0.4
0.50	0.3

<u>P2</u>	<u>Prob</u>
0.42	0.2
0.44	0.6
0.46	0.2

The joint prior distribution can be found by multiplying the three independent probabilities in each row. This results in the following discrete probability distribution.

<u>P1</u>	<u>P2</u>	<u>P(P1)</u>	<u>P(P2)</u>	<u>Prob</u>
0.38	0.42	0.3	0.2	0.06
0.38	0.44	0.3	0.6	0.18
0.38	0.46	0.3	0.2	0.06
0.44	0.42	0.4	0.2	0.08
0.44	0.44	0.4	0.6	0.24
0.44	0.46	0.4	0.2	0.08
0.50	0.42	0.3	0.2	0.06
0.50	0.44	0.3	0.6	0.18
0.50	0.46	0.3	0.2	0.06

To run this example, the spreadsheet is loaded with the following four columns.

<u>C1</u>	<u>C2</u>	<u>C3</u>	<u>C4</u>	<u>C5</u>
0.38	0.42	0.3	0.2	0.06
0.38	0.44	0.3	0.6	0.18
0.38	0.46	0.3	0.2	0.06
0.44	0.42	0.4	0.2	0.08
0.44	0.44	0.4	0.6	0.24
0.44	0.46	0.4	0.2	0.08
0.50	0.42	0.3	0.2	0.06
0.50	0.44	0.3	0.6	0.18
0.50	0.46	0.3	0.2	0.06

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 5** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Design Tab

Solve For **Assurance**
 Prior Entry Method **Combined (Enter parameter values and probabilities on spreadsheet)**
 Test Type **Likelihood Score (Farrington & Manning)**
 Alpha **0.05**
 Group Allocation **Equal (N1 = N2)**
 Sample Size Per Group **1000**
 R0.U (Upper Equivalence Ratio) **1.25**
 R0.L (Lower Equivalence Ratio) **0.8**
 Column of P1 Values **C1**
 Column of P2 Values **C2**
 Column of Pr(Values) **C5**

Options Tab

Number of Computation Points for each **20**
 Prior Distribution
 Maximum N1 in Sample Size Search **5000**

Input Spreadsheet Data

Row	C1	C2	C3	C4	C5
1	0.38	0.42	0.3	0.2	0.06
2	0.38	0.44	0.3	0.6	0.18
3	0.38	0.46	0.3	0.2	0.06
4	0.44	0.42	0.4	0.2	0.08
5	0.44	0.44	0.4	0.6	0.24
6	0.44	0.46	0.4	0.2	0.08
7	0.50	0.42	0.3	0.2	0.06
8	0.50	0.44	0.3	0.6	0.18
9	0.50	0.46	0.3	0.2	0.06

Assurance for Equivalence Tests for the Ratio of Two Proportions

Output

Click the Calculate button to perform the calculations and generate the following output.

Numeric Results

Solve For: [Assurance](#)

Test Statistic: Farrington & Manning Likelihood Score Test

Hypotheses: $H_0: P_1 / P_2 \leq R_{0.L} \text{ or } P_1 / P_2 \geq R_{0.U}$ vs. $H_1: R_{0.L} < P_1 / P_2 < R_{0.U}$

Prior Type: Joint Multivariate Distribution

Prior Distribution

Point Lists

P1: C1: 0.38 0.38 0.38 0.44 0.44 0.44 0.5 0.5 0.5

P2: C2: 0.42 0.44 0.46 0.42 0.44 0.46 0.42 0.44 0.46

Prob: C5: 0.06 0.18 0.06 0.08 0.24 0.08 0.06 0.18 0.06

		Ratio of Proportions								
		Sample Size			Expected Group 1 Proportion E(P1)	Expected Group 2 Proportion E(P2)	Equivalence			Alpha
Assurance	Power‡	N1	N2	N			H1 R1	Lower R0.L	Upper R0.U	
0.70407	0.99398	1000	1000	2000	0.44	0.44	1	0.8	1.25	0.05

‡ Power was calculated using $P_1 = E(P_1) = 0.44$ and $P_2 = E(P_2) = 0.44$.

PASS has also calculated the assurance as 0.70407 which matches Example 2 and thus validates the procedure.