

Chapter 758

Assurance for Superiority by a Margin Tests for the Ratio of Two Poisson Rates

Introduction

This procedure calculates the assurance of superiority by a margin tests of the ratio of two independent Poisson event rates. A Poisson regression model gives the probability distribution of the number of events occurring in a specified interval of time or space. The Poisson distribution is characterized by a single parameter which is the mean number of occurrences during the specified interval. The Poisson distribution is often used to fit count data, such as the number of lesions on a subject's legs or the number of episodes during a year.

The calculation is based on a user-specified prior distribution of the effect size parameters. This procedure may also be used to determine the needed sample size to obtain a specified assurance. The methods for assurance calculation in this procedure are based on O'Hagan, Stevens, and Campbell (2005).

Assurance

The assurance of a design is the expected value of the power with respect to one or more prior distributions of the design parameters. Assurance is also referred to as *Bayesian assurance*, *expected power*, *average power*, *statistical assurance*, *hybrid classical-Bayesian procedure*, or *probability of success*.

The power of a design is the probability of rejecting the null hypothesis, conditional on a given set of design attributes, such as the test statistic, the significance level, the sample size, and the effect size to be detected. As the effect size parameters are typically unknown quantities, the stated power may be very different from the true power if the specified parameter values are inaccurate.

While power is conditional on individual design parameter values, and is highly sensitive to those values, assurance is the average power across a presumed prior distribution of the effect size parameters. Thus, assurance adds a Bayesian element to the frequentist framework, resulting in a hybrid approach to the probability of trial or study success. It should be noted that when it comes time to perform the statistical test on the resulting data, these methods for calculating assurance assume that the traditional (frequentist) tests will be used.

The next section describes some of the ways in which the prior distributions for effect size parameters may be determined.

Elicitation

In order to calculate assurance, a suitable prior distribution for the effect size parameters must be determined. This process is called the *elicitation* of the prior distribution.

The elicitation may be as simple as choosing a distribution that seems plausible for the parameter(s) of interest, or as complex as combining the informed advice of several experts based on experience in the field, available pilot data, or previous studies. The accuracy of the assurance value depends on the accuracy

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of the elicited prior distribution. The assumption (or hope) is that an informed prior distribution will produce a more accurate estimate of the probability of trial success than a single value estimate. Because clinical trials and other studies are often costly, many institutions now routinely require an elicitation step.

Two reference texts that focus on elicitation are O'Hagan, Buck, Daneshkhah, Eiser, Garthwaite, Jenkinson, Oakley, and Rakow (2006) and Dias, Morton, and Quigley (2018).

Technical Details

Definition of Terms

The following table presents the various terms that are used.

Group	1 (Control)	2 (Treatment)
Sample size	N_1	N_2
Individual event rates	λ_1	λ_2

Dispersion parameter: φ ($\varphi > 1$ implies over-dispersion; $\varphi < 1$ implies under-dispersion)

Average exposure time: μ_t

Superiority by a margin ratio: RR_0 ($RR_0 > 1$ if higher rates better; $RR_0 < 1$ if higher rates worse)

Sample size ratio: $\theta = N_2/N_1$

Hypotheses

When higher rates are better, the superiority by a margin test hypotheses are

$$H_0: \frac{\lambda_2}{\lambda_1} \leq RR_0 \quad \text{vs.} \quad H_1: \frac{\lambda_2}{\lambda_1} > RR_0$$

where $RR_0 > 1$.

When higher rates are worse, the superiority by a margin test hypotheses are

$$H_0: \frac{\lambda_2}{\lambda_1} \geq RR_0 \quad \text{vs.} \quad H_1: \frac{\lambda_2}{\lambda_1} < RR_0$$

where $RR_0 < 1$.

Sample Size and Power Calculations

Sample Size Calculation

Zhu (2017) bases the sample size calculations on a superiority by a margin test derived from a Poisson regression model. The power calculation for a one-sided test is given by

$$Power \geq 1 - \Phi \left(\frac{\sqrt{N_1}(\log RR_0 - \log(\lambda_2/\lambda_1)) - z_\alpha \sqrt{V_0}}{\sqrt{V_1}} \right)$$

where

$$N_2 = \theta N_1$$

$$V_1 = \frac{\varphi}{\mu_t} \left(\frac{1}{\lambda_1} + \frac{1}{\theta \lambda_2} \right)$$

and V_0 may be calculated in either of two ways.

V_0 Calculation Method 1 (using assumed true rates)

$$V_{01} = \frac{\varphi}{\mu_t} \left(\frac{1}{\lambda_1} + \frac{1}{\theta \lambda_2} \right)$$

Using Method 1, V_0 and V_1 are equal.

V_0 Calculation Method 2 (fixed marginal total or restricted maximum likelihood estimation)

$$V_{02} = \frac{\varphi(1 + RR_0\theta)^2}{\mu_t RR_0 \theta (\lambda_1 + \theta \lambda_2)}$$

Zhu (2017) did not give a recommendation regarding whether Method 1 or Method 2 should be used, except to say that “sample sizes calculated using Method 2 are slightly larger compared to those calculated by Method 1 for most simulated scenarios...”.

Assurance Calculation

This assurance computation described here is based on O'Hagan, Stevens, and Campbell (2005).

Let $P'(H|\lambda_1, \lambda_2, \mu_t, \varphi)$ be the power function described above where H is the event that null hypothesis is rejected conditional on the parameter values. The specification of $\lambda_1, \lambda_2, \mu_t$, and φ is critical to the power calculation, but the actual values are seldom known. Assurance is defined as the expected power where the expectation is with respect to a joint prior distribution for the parameters $\lambda_1, \lambda_2, \mu_t$, and φ . Hence, the definition of assurance is

$$Assurance = E_{\lambda_1, \lambda_2, \mu_t, \varphi} (P'(H|\lambda_1, \lambda_2, \mu_t, \varphi)) = \int \int \int \int P'(H|\lambda_1, \lambda_2, \mu_t, \varphi) f(\lambda_1, \lambda_2, \mu_t, \varphi) d\lambda_1 d\lambda_2 d\mu_t d\varphi$$

where $f(\lambda_1, \lambda_2, \mu_t, \varphi)$ is the joint prior distribution using the four parameters.

In **PASS**, the joint prior distribution can be specified as either a discrete approximation to the joint prior distribution, or as individual prior distributions, one for each parameter.

Specifying a Joint Prior Distribution

If the joint prior distribution is to be specified directly, the distribution is specified in **PASS** using a discrete approximation to the function $f(\lambda_1, \lambda_2, \mu_t, \varphi)$. This provides flexibility in specifying the joint prior distribution. In the four-parameter case, five columns are entered on the spreadsheet: four for the parameters and a fifth for the probability. Each row gives a value for each parameter and the corresponding parameter-combination probability. The accuracy of the distribution approximation is controlled by the number of points (spreadsheet rows) that are used.

An example of entering a joint prior distribution is included at the end of the chapter.

Specifying Individual Prior Distributions

Ciarleglio, Arendt, and Peduzzi (2016) suggest that more flexibility is available if the joint prior distribution is separated into two independent univariate distributions as follows

$$f(\lambda_1, \lambda_2, \mu_t, \varphi) = f_1(\lambda_1)f_2(\lambda_2)f_3(\mu_t)f_4(\varphi)$$

where $f_1(\lambda_1)$ is the prior distribution of λ_1 , $f_2(\lambda_2)$ is the prior distribution of λ_2 , and so on. This method is also available in **PASS**. In this case, the definition of assurance becomes

$$Assurance = E_{\lambda_1, \lambda_2, \mu_t, \varphi} \left(P'(H | \lambda_1, \lambda_2, \mu_t, \varphi) \right) = \int \int \int \int P'(H | \lambda_1, \lambda_2, \mu_t, \varphi) f_1(\lambda_1) f_2(\lambda_2) f_3(\mu_t) f_4(\varphi) d\lambda_1 d\lambda_2 d\mu_t d\varphi$$

Using this definition, the assurance can be calculated using numerical integration. There are a variety of pre-programmed, univariate prior distributions available in **PASS**.

Fixed Values (No Prior) and Custom Values

For any given parameter, **PASS** also provides the option of entering a single fixed value for the prior distribution, or a series of values and corresponding probabilities (using the spreadsheet), rather than one of the pre-programmed distributions.

Numerical Integration in PASS (and Notes on Computation Speed)

When the prior distribution is specified as independent univariate distributions, **PASS** uses a numerical integration algorithm to compute the assurance value as follows:

The domain of each prior distribution is divided into M intervals. Since many of the available prior distributions are unbounded on one (e.g., Gamma) or both (e.g., Normal) ends, an approximation is made to make the domain finite. This is accomplished by truncating the distribution to a domain between the two quantiles: $q_{0.001}$ and $q_{0.999}$.

The value of M controls the accuracy and speed of the algorithm. If only one parameter is to be given a prior distribution, then a value of M between 50 and 100 usually gives an accurate result in a timely manner. However, if two parameters are given priors, the number of iterations needed increases from M to M^2 . For example, if M is 100, 10000 iterations are needed. Reducing M from 100 to 50 reduces the number of iterations from 10000 to 2500.

The algorithm runtime increases when searching for sample size rather than solving for assurance, as a search algorithm is employed in this case. When solving for sample size, we recommend reducing M to 20 or less while exploring various scenarios, and then increasing M to 50 or more for a final, more accurate, result.

List of Available Univariate Prior Distributions

This section lists the univariate prior distributions that may be used for any of the applicable parameters when the Prior Entry Method is set to Individual.

No Prior

If 'No Prior' is chosen for a parameter, the parameter is assumed to take on a single, fixed value with probability one.

Beta (Shape 1, Shape 2, a, c)

A random variable X that follows the beta distribution is defined on a finite interval $[a, c]$. Two shape parameters (α and β) control the shape of this distribution. Two location parameters a and c give the minimum and maximum of X .

The probability density function of the beta distribution is

$$f(x|\alpha, \beta, a, c) = \frac{\left(\frac{x-a}{c-a}\right)^{\alpha-1} \left(\frac{c-x}{c-a}\right)^{\beta-1}}{(c-a)B(\alpha, \beta)}$$

where $B(\alpha, \beta) = \Gamma(\alpha) \Gamma(\beta) / \Gamma(\alpha + \beta)$ and $\Gamma(z)$ is the gamma function.

The mean of X is

$$\mu_x = \frac{\alpha c + \beta a}{\alpha + \beta}$$

Various distribution shapes are controlled by the values of α and β . These include

Symmetric and Unimodal

$$\alpha = \beta > 1$$

U Shaped

$$\alpha = \beta < 1$$

Bimodal

$$\alpha, \beta < 1$$

Uniform

$$\alpha = \beta = 1$$

Parabolic

$$\alpha = \beta = 2$$

Bell-Shaped

$$\alpha = \beta > 2$$

Gamma (Shape, Scale)

A random variable X that follows the gamma distribution is defined on the interval $(0, \infty)$. A shape parameter, κ , and a scale parameter, θ , control the distribution.

The probability density function of the gamma distribution is

$$f(x|\kappa, \theta) = \frac{x^{\kappa-1} e^{-\frac{x}{\theta}}}{\theta^{\kappa} \Gamma(\kappa)}$$

where $\Gamma(z)$ is the gamma function.

The mean of X is

$$\mu_X = \frac{\kappa}{\theta}$$

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(Min \leq X \leq Max)$ where Min and Max are two truncation bounds.

Inverse-Gamma (Shape, Scale)

A random variable X that follows the inverse-gamma distribution is defined on the interval $(0, \infty)$. If $Y \sim \text{gamma}$, then $X = 1 / Y \sim \text{inverse-gamma}$. A shape parameter, α , and a scale parameter, β , control the distribution.

The probability density function of the inverse-gamma distribution is

$$f(x|\alpha, \beta) = \frac{\beta^{\alpha} x^{\alpha-1} e^{-\frac{\beta}{x}}}{\Gamma(\alpha)}$$

where $\Gamma(z)$ is the gamma function.

The mean of X is

$$\mu_X = \frac{\beta}{\alpha - 1} \text{ for } \alpha > 1$$

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(Min \leq X \leq Max)$ where Min and Max are two truncation bounds.

Logistic (Location, Scale)

A random variable X that follows the logistic distribution is defined on the interval $(-\infty, \infty)$. A location parameter, μ , and a scale parameter, s , control the distribution.

The probability density function of the logistic distribution is

$$f(x|\mu, s) = \frac{e^{-\frac{x-\mu}{s}}}{s \left(1 + e^{-\frac{x-\mu}{s}}\right)^2}$$

The mean of X is

$$\mu_X = \mu$$

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(Min \leq X \leq Max)$ where Min and Max are two truncation bounds.

Lognormal (Mean, SD)

A random variable X that follows the lognormal distribution is defined on the interval $(0, \infty)$. A location parameter, $\mu_{\log(X)}$, and a scale parameter, $\sigma_{\log(X)}$, control the distribution. If $Z \sim$ standard normal, then $X = e^{\mu + \sigma Z} \sim$ lognormal. Note that $\mu_{\log(X)} = E(\log(X))$ and $\sigma_{\log(X)} = \text{Standard Deviation}(\log(X))$.

The probability density function of the lognormal distribution is

$$f(x|\mu, \sigma) = \frac{e^{-\frac{1}{2}\left(\frac{\log x - \mu}{\sigma}\right)^2}}{x\sigma\sqrt{2\pi}}$$

The mean of X is

$$\mu_X = e^{\mu + \frac{\sigma^2}{2}}$$

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(\text{Min} \leq X \leq \text{Max})$ where Min and Max are two truncation bounds.

LogT (Mean, SD)

A random variable X that follows the logT distribution is defined on the interval $(0, \infty)$. A location parameter, $\mu_{\log(X)}$, a scale parameter, $\sigma_{\log(X)}$, and a shape parameter, ν , control the distribution. Note that ν is referred to as the *degrees of freedom*.

If $t \sim$ Student's t , then $X = e^{\mu + \sigma t} \sim$ logT.

The probability density function of the logT distribution is

$$f(x|\mu, \sigma, \nu) = \frac{\Gamma\left(\frac{\nu+1}{2}\right)}{x\Gamma\left(\frac{\nu}{2}\right)\sigma\sqrt{\nu\pi}} \left(1 + \frac{1}{\nu}\left(\frac{\log x - \mu}{\sigma}\right)^2\right)^{\left(\frac{-\nu-1}{2}\right)}$$

The mean of X is not defined.

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(\text{Min} \leq X \leq \text{Max})$ where Min and Max are two truncation bounds.

Normal (Mean, SD)

A random variable X that follows the normal distribution is defined on the interval $(-\infty, \infty)$. A location parameter, μ , and a scale parameter, σ , control the distribution.

The probability density function of the normal distribution is

$$f(x|\mu, \sigma) = \frac{e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}}{\sigma\sqrt{2\pi}}$$

The mean of X is

$$\mu_X = \mu$$

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(\text{Min} \leq X \leq \text{Max})$ where Min and Max are two truncation bounds.

T (Mean, SD, DF)

A random variable X that follows Student's t distribution is defined on the interval $(-\infty, \infty)$. A location parameter, μ , a scale parameter, σ , and a shape parameter, ν , control the distribution. Note that ν is referred to as the *degrees of freedom* or *DF*.

The probability density function of the Student's t distribution is

$$f(x|\mu, \sigma, \nu) = \frac{\Gamma\left(\frac{\nu+1}{2}\right)}{\Gamma\left(\frac{\nu}{2}\right) \sigma \sqrt{\nu\pi}} \left(1 + \frac{1}{\nu} \left(\frac{x-\mu}{\sigma}\right)^2\right)^{\frac{-(\nu+1)}{2}}$$

The mean of X is μ if $\nu > 1$.

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(Min \leq X \leq Max)$ where Min and Max are two truncation bounds.

Triangle (Mode, Min, Max)

Let a = minimum, b = maximum, and c = mode. A random variable X that follows a triangle distribution is defined on the interval (a, b) .

The probability density function of the triangle distribution is

$$f(x|a, b, c) = \begin{cases} \frac{2(x-a)}{(b-a)(c-a)} & \text{for } a \leq x < c \\ \frac{2}{b-a} & \text{for } x = c \\ \frac{2(b-x)}{(b-a)(b-c)} & \text{for } c < x \leq b \end{cases}$$

The mean of X is

$$\frac{a+b+c}{3}$$

Uniform (Min, Max)

Let a = minimum and b = maximum. A random variable X that follows a uniform distribution is defined on the interval $[a, b]$.

The probability density function of the uniform distribution is

$$f(x|a, b) = \begin{cases} \frac{1}{b-a} & \text{for } a \leq x \leq b \end{cases}$$

The mean of X is

$$\frac{a+b}{2}$$

Weibull (Shape, Scale)

A random variable X that follows the Weibull distribution is defined on the interval $(0, \infty)$. A shape parameter, κ , and a scale parameter, λ , control the distribution.

The probability density function of the Weibull distribution is

$$f(x|\kappa, \lambda) = \frac{\kappa}{\lambda} \left(\frac{x}{\lambda}\right)^{\kappa-1} e^{-\left(\frac{x}{\lambda}\right)^\kappa}$$

The mean of X is

$$\mu_X = \kappa \Gamma\left(1 + \frac{1}{\kappa}\right)$$

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(\text{Min} \leq X \leq \text{Max})$ where Min and Max are two truncation bounds.

Custom (Values and Probabilities in Spreadsheet)

This custom prior distribution is represented by a set of user-specified points and associated probabilities, entered in two columns of the spreadsheet. The points make up the entire set of values that are used for this parameter in the calculation of assurance. The associated probabilities should sum to one. Note that custom values and probabilities can be used to approximate any continuous distribution.

For example, a prior distribution of X might be

X_i	P_i
10	0.2
20	0.2
30	0.3
40	0.2
50	0.1

In this example, the mean of X is

$$\mu_X = \sum_{i=1}^5 X_i P_i$$

Example 1 – Assurance Over a Range of Sample Sizes

Researchers wish to compare two drugs to determine whether there is a meaningful decrease in the treatment event rate from the control event rate. In this case, higher rates are worse. They will analyze the data using a Poisson regression model. A one-sided test of the regression coefficient identifying the treatment group will have a significance level of 0.025. The value of RR0 is set at 0.9.

To complete their sample size study, the researchers want to run an assurance analysis for a range of group sample sizes from 200 to 800. An elicitation exercise determined that $\lambda_1 \sim N(1, 0.05^2)$, $\lambda_2 \sim N(0.7, 0.15^2)$, $\mu_t \sim N(1.0, 0.03^2)$, and $\varphi \sim N(1.8, 0.04^2)$.

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 1** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Design Tab

Solve For **Assurance**
 Prior Entry Method **Individual (Enter a prior distribution for each applicable parameter)**
 Higher Poisson Rates Are **Worse**
 Variance Calculation Method **Using Assumed True Rates**
 Alpha **0.025**
 Prior Distribution of $\mu(t)$ **Normal (Mean, SD)**
 Mean **1**
 SD **0.03**
 Truncation Boundaries **None**
 Group Allocation **Equal (N1 = N2)**
 Sample Size Per Group **200 400 600 800**
 RR0 (Superiority Margin Ratio) **0.9**
 Prior Distribution of λ_1 **Normal (Mean, SD)**
 Mean **1**
 SD **0.05**
 Truncation Boundaries **None**
 Prior Distribution of λ_2 **Normal (Mean, SD)**
 Mean **0.7**
 SD **0.15**
 Truncation Boundaries **None**
 Prior Distribution of φ **Normal (Mean, SD)**
 Mean **1.8**
 SD **0.04**
 Truncation Boundaries **None**

Options Tab

Number of Computation Points for each **20**
 Prior Distribution
 Maximum N1 in Sample Size Search **5000**

Output

Click the Calculate button to perform the calculations and generate the following output.

Numeric Reports

Numeric Results

Solve For: Assurance
 Hypotheses: $H_0: \lambda_2 / \lambda_1 \geq RR_0$ vs. $H_1: \lambda_2 / \lambda_1 < RR_0$
 Variance Method: Use Assumed True Event Rates
 Prior Type: Independent Univariate Distributions

Prior Distributions

$\mu(t)$: Normal (Mean = 1, SD = 0.03).
 λ_1 : Normal (Mean = 1, SD = 0.05).
 λ_2 : Normal (Mean = 0.7, SD = 0.15).
 ϕ : Normal (Mean = 1.8, SD = 0.04).

Assurance*	Power‡	N1	N2	N	Average Exposure Time $E(\mu(t))$	Event Rate		Rate Ratio		Dispersion $E(\phi)$	Alpha
						Group 1 $E(\lambda_1)$	Group 2 $E(\lambda_2)$	Actual RR	Sup-Marg RR0		
0.44320	0.39740	200	200	400	1	1	0.7	0.7	0.9	1.8	0.025
0.58275	0.67149	400	400	800	1	1	0.7	0.7	0.9	1.8	0.025
0.65059	0.83752	600	600	1200	1	1	0.7	0.7	0.9	1.8	0.025
0.69110	0.92504	800	800	1600	1	1	0.7	0.7	0.9	1.8	0.025

* The number of points used for computation of the prior(s) was 20.

‡ Power was calculated using $\lambda_1 = E(\lambda_1) = 1$, $\lambda_2 = E(\lambda_2) = 0.7$, $\mu(t) = E(\mu(t)) = 1$, and $\phi = E(\phi) = 1.8$.

Assurance The expected power where the expectation is with respect to the prior distribution(s).
 Power The power calculated using the parameter values shown in the footnote. Note that these parameter values may be different from those shown in the report.
 N1 The number of subjects in group 1.
 N2 The number of subjects in group 2.
 N The total sample size. $N = N1 + N2$.
 $E(\mu(t))$ The expected value over its prior distribution of the average exposure time across subjects in both groups.
 $E(\lambda_1)$ The expected value over its prior distribution of the group 1 mean event rate.
 $E(\lambda_2)$ The expected value over its prior distribution of the group 2 mean event rate.
 RR The ratio of the average event rates (λ_2 / λ_1).
 RR0 The superiority margin ratio is the smallest (or largest) the ratio can be and still be called superior.
 $E(\phi)$ The expected value over its prior distribution of the dispersion parameter ($\phi > 1$ implies over-dispersion, $\phi < 1$ implies under-dispersion).
 Alpha The probability of rejecting a true null hypothesis.

Summary Statements

Group sample sizes of 200 in group 1 and 200 in group 2 achieve 0.4432 assurance using a superiority by a margin test of the ratio of two Poisson event rates. The superiority by a margin event rate ratio is 0.9. This test is based on a Poisson regression model. The average group 2 (treatment) event rate is 0.7 and the average group 1 (control) event rate is 1. The variance of the Poisson regression coefficient being tested is calculated using the assumed true rates. The significance level (alpha) of the test is 0.025. The prior distribution used for the group 1 event rate is Normal (Mean = 1, SD = 0.05). The prior distribution used for the group 2 event rate is Normal (Mean = 0.7, SD = 0.15). The prior distribution used for the average exposure time is Normal (Mean = 1, SD = 0.03). The prior distribution used for the dispersion factor is Normal (Mean = 1.8, SD = 0.04).

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Dropout-Inflated Sample Size

Dropout Rate	Sample Size			Dropout-Inflated Enrollment Sample Size			Expected Number of Dropouts		
	N1	N2	N	N1'	N2'	N'	D1	D2	D
20%	200	200	400	250	250	500	50	50	100
20%	400	400	800	500	500	1000	100	100	200
20%	600	600	1200	750	750	1500	150	150	300
20%	800	800	1600	1000	1000	2000	200	200	400

Dropout Rate	The percentage of subjects (or items) that are expected to be lost at random during the course of the study and for whom no response data will be collected (i.e., will be treated as "missing"). Abbreviated as DR.
N1, N2, and N	The evaluable sample sizes at which power is computed (as entered by the user). If N1 and N2 subjects are evaluated out of the N1' and N2' subjects that are enrolled in the study, the design will achieve the stated power.
N1', N2', and N'	The number of subjects that should be enrolled in the study in order to obtain N1, N2, and N evaluable subjects, based on the assumed dropout rate. N1' and N2' are calculated by inflating N1 and N2 using the formulas $N1' = N1 / (1 - DR)$ and $N2' = N2 / (1 - DR)$, with N1' and N2' always rounded up. (See Julious, S.A. (2010) pages 52-53, or Chow, S.C., Shao, J., Wang, H., and Lohknygina, Y. (2018) pages 32-33.)
D1, D2, and D	The expected number of dropouts. $D1 = N1' - N1$, $D2 = N2' - N2$, and $D = D1 + D2$.

Dropout Summary Statements

Anticipating a 20% dropout rate, 250 subjects should be enrolled in Group 1, and 250 in Group 2, to obtain final group sample sizes of 200 and 200, respectively.

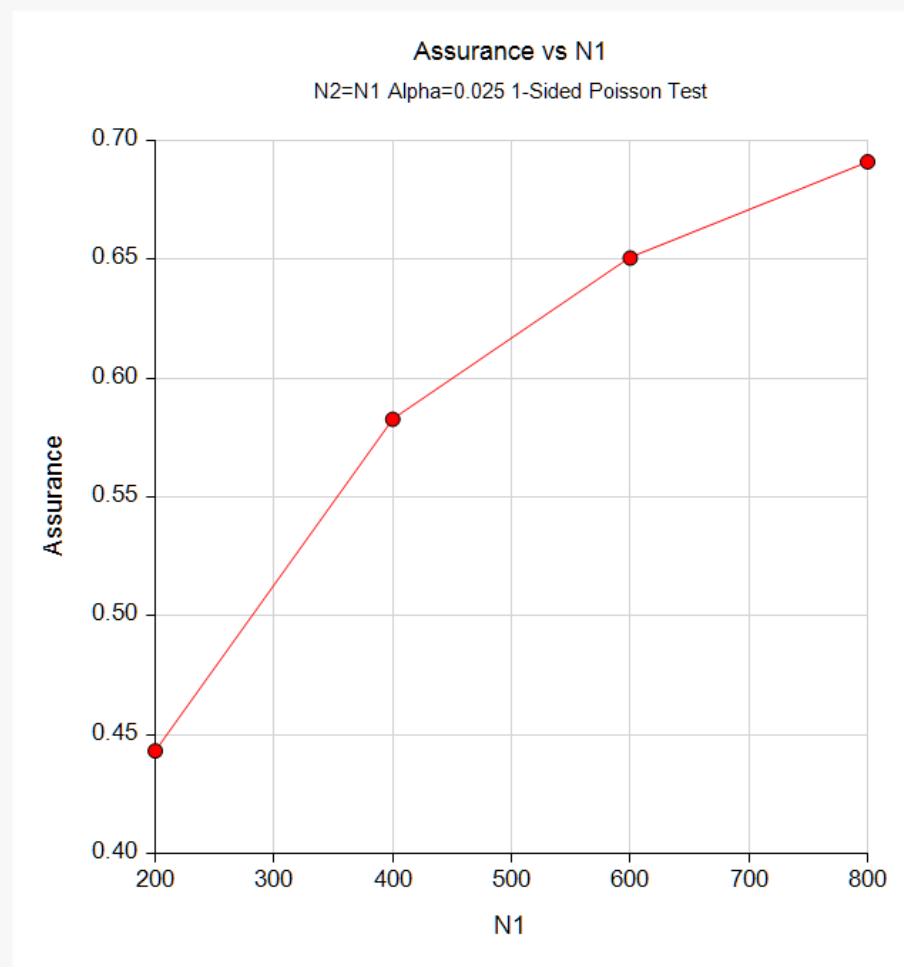
References

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This report shows the assurance values obtained by the various sample sizes.

Plots Section

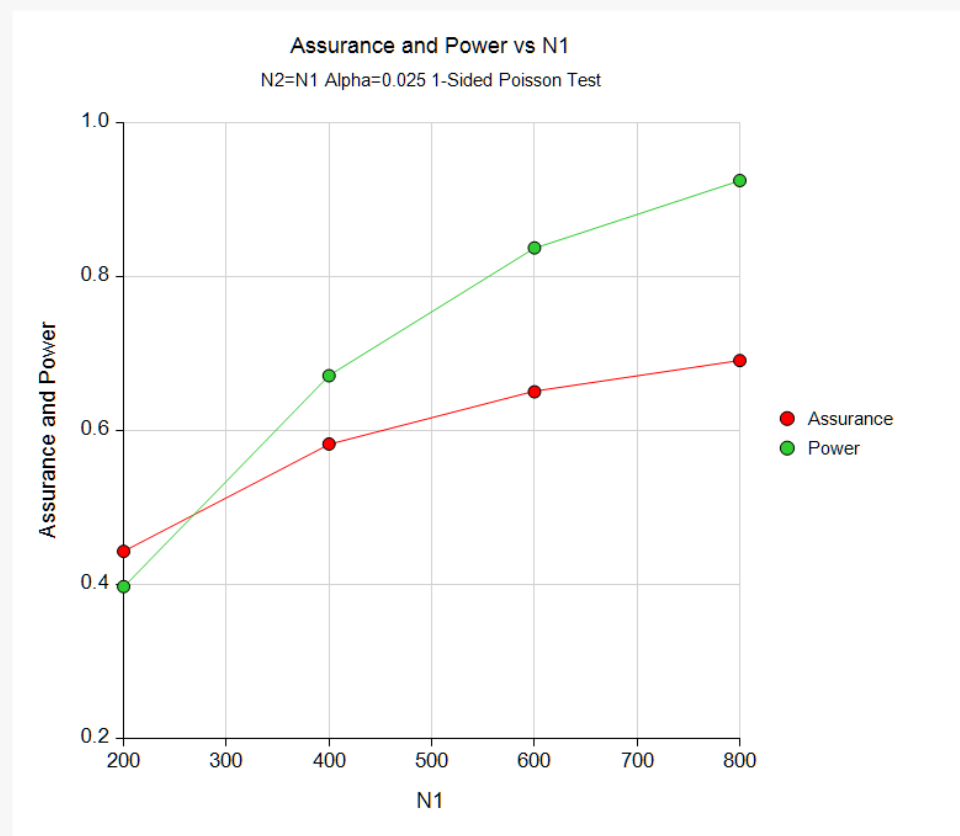
Plots



This plot shows the relationship between the assurance and sample size. Note the diminishing impact on assurance of each increase in the number of subjects.

Comparison Plots Section

Comparison Plots



This plot compares the assurance and power across values of sample size. Note that assurance does not increase nearly as fast as does power.

Example 2 – Validation using Hand Computation

We could not find a validation example in the literature, so we have developed a validation example of our own. Suppose a one-sided test is used in which $N_1 = N_2 = 800$ and the significance level is 0.025 and $R_0 = 0.9$.

The prior distribution of λ_1 is approximated by the following table.

λ_1	Prob
0.95	0.4
1.05	0.6

The prior distribution of λ_2 is approximated by the following table.

λ_2	Prob
0.6	0.4
0.8	0.6

The prior distribution of $\mu(t)$ is approximated by the following table.

$\mu(t)$	Prob
0.96	0.5
1.04	0.5

The prior distribution of ϕ is approximated by the following table.

ϕ	Prob
1.7	0.5
1.9	0.5

The *Superiority by a Margin Tests for the Ratio of Two Poisson Rates* procedure is used to compute the power for each of the 16 combinations of the four parameters. The results of these calculations are shown next.

Numeric Results

Solve For: Power
 Test Direction Assumption: Higher Poisson Rates Are Worse
 Hypotheses: $H_0: \lambda_2 / \lambda_1 \geq R_0$ vs. $H_1: \lambda_2 / \lambda_1 < R_0$
 Variance Calculation Method: Using Assumed True Rates

Power	N1	N2	N	Average Exposure Time $\mu(t)$	Grp 1 Cntrl Event Rate λ_1	Grp 2 Trt Event Rate λ_2	Event Rate Ratio λ_2 / λ_1	Superiority Margin Ratio R_0	Dispersion ϕ	Alpha
0.99541	800	800	1600	0.96	0.95	0.6	0.63158	0.9	1.7	0.025
0.15182	800	800	1600	0.96	0.95	0.8	0.84211	0.9	1.7	0.025
0.99997	800	800	1600	0.96	1.05	0.6	0.57143	0.9	1.7	0.025
0.66485	800	800	1600	0.96	1.05	0.8	0.76190	0.9	1.7	0.025
0.99082	800	800	1600	0.96	0.95	0.6	0.63158	0.9	1.9	0.025
0.14029	800	800	1600	0.96	0.95	0.8	0.84211	0.9	1.9	0.025
0.99988	800	800	1600	0.96	1.05	0.6	0.57143	0.9	1.9	0.025
0.61664	800	800	1600	0.96	1.05	0.8	0.76190	0.9	1.9	0.025
0.99738	800	800	1600	1.04	0.95	0.6	0.63158	0.9	1.7	0.025
0.16094	800	800	1600	1.04	0.95	0.8	0.84211	0.9	1.7	0.025
0.99999	800	800	1600	1.04	1.05	0.6	0.57143	0.9	1.7	0.025
0.69956	800	800	1600	1.04	1.05	0.8	0.76190	0.9	1.7	0.025
0.99437	800	800	1600	1.04	0.95	0.6	0.63158	0.9	1.9	0.025

Assurance for Superiority by a Margin Tests for the Ratio of Two Poisson Rates

0.14846	800	800	1600	1.04	0.95	0.8	0.84211	0.9	1.9	0.025
0.99995	800	800	1600	1.04	1.05	0.6	0.57143	0.9	1.9	0.025
0.65130	800	800	1600	1.04	1.05	0.8	0.76190	0.9	1.9	0.025

The assurance calculation is made by summing the quantities $[(power_{i,j,k,l})(p(\lambda_{1i}))(p(\lambda_{2j}))(p(\mu_k))(p(\varphi_l))]$ as follows

$$\begin{aligned}
 Assurance &= (0.99541 \times 0.4 \times 0.4 \times 0.5 \times 0.5) + (0.15182 \times 0.4 \times 0.6 \times 0.5 \times 0.5) + \dots \\
 &\quad + (0.65130 \times 0.6 \times 0.6 \times 0.5 \times 0.5) \\
 &= 0.67211.
 \end{aligned}$$

To run this example, the spreadsheet will need to be loaded with the following eight columns in which the first two are for λ_1 , the second two are for λ_2 , and so on.

C1	C2	C3	C4	C5	C6	C7	C8
0.95	0.4	0.6	0.4	0.96	0.5	1.7	0.5
1.05	0.6	0.8	0.6	1.04	0.5	1.9	0.5

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 2** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Design Tab

Solve For	Assurance
Prior Entry Method.....	Individual (Enter a prior distribution for each applicable parameter)
Higher Poisson Rates Are.....	Worse
Variance Calculation Method.....	Using Assumed True Rates
Alpha.....	0.025
Prior Distribution of $\mu(t)$	Custom (Values and Probabilities in Spreadsheet)
Column of Values	C5
Column of Pr(Values).....	C6
Group Allocation	Equal (N1 = N2)
Sample Size Per Group	800
RR0 (Superiority Margin Ratio).....	0.9
Prior Distribution of λ_1	Custom (Values and Probabilities in Spreadsheet)
Column of Values	C1
Column of Pr(Values).....	C2
Prior Distribution of λ_2	Custom (Values and Probabilities in Spreadsheet)
Column of Values	C3
Column of Pr(Values).....	C4
Prior Distribution of φ	Custom (Values and Probabilities in Spreadsheet)
Column of Values	C7
Column of Pr(Values).....	C8

Assurance for Superiority by a Margin Tests for the Ratio of Two Poisson Rates

Options Tab

Number of Computation Points for each**20**

Prior Distribution

Maximum N1 in Sample Size Search**5000**

Input Spreadsheet Data

Row	C1	C2	C3	C4	C5	C6	C7	C8
1	0.95	0.4	0.6	0.4	0.96	0.5	1.7	0.5
2	1.05	0.6	0.8	0.6	1.04	0.5	1.9	0.5

Output

Click the Calculate button to perform the calculations and generate the following output.

Numeric Results

Solve For: [Assurance](#)
 Hypotheses: H0: $\lambda_2 / \lambda_1 \geq RR0$ vs. H1: $\lambda_2 / \lambda_1 < RR0$
 Variance Method: Use Assumed True Event Rates
 Prior Type: Independent Univariate Distributions

Prior Distributions

$\mu(t)$: Point List (Values = C5, Probs = C6).
 C5: 0.96 1.04
 C6: 0.5 0.5
 λ_1 : Point List (Values = C1, Probs = C2).
 C1: 0.95 1.05
 C2: 0.4 0.6
 λ_2 : Point List (Values = C3, Probs = C4).
 C3: 0.6 0.8
 C4: 0.4 0.6
 ϕ : Point List (Values = C7, Probs = C8).
 C7: 1.7 1.9
 C8: 0.5 0.5

Assurance	Power‡	N1	N2	N	Average Exposure Time E($\mu(t)$)	Event Rate		Rate Ratio		Dispersion E(ϕ)	Alpha
						Group 1 E(λ_1)	Group 2 E(λ_2)	Actual RR	Sup-Marg RR0		
0.67211	0.8899	800	800	1600	1	1.01	0.72	0.71287	0.9	1.8	0.025

‡ Power was calculated using $\lambda_1 = E(\lambda_1) = 1.01$, $\lambda_2 = E(\lambda_2) = 0.72$, $\mu(t) = E(\mu(t)) = 1$, and $\phi = E(\phi) = 1.8$.

PASS has also calculated the assurance as 0.67211 which validates the procedure.

Example 3 – Finding the Sample Size Needed to Achieve a Specified Assurance

Continuing with Example 1, the researchers want to investigate the sample sizes necessary to achieve assurances of 0.4, 0.5, 0.6, 0.7, and 0.8.

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 3** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Design Tab

Solve For	Sample Size
Prior Entry Method.....	Individual (Enter a prior distribution for each applicable parameter)
Higher Poisson Rates Are.....	Worse
Variance Calculation Method.....	Using Assumed True Rates
Assurance.....	0.4 0.5 0.6 0.7 0.8
Alpha.....	0.025
Prior Distribution of $\mu(t)$	Normal (Mean, SD)
Mean.....	1
SD.....	0.03
Truncation Boundaries.....	None
Group Allocation	Equal (N1 = N2)
RR0 (Superiority Margin Ratio).....	0.9
Prior Distribution of λ_1	Normal (Mean, SD)
Mean.....	1
SD.....	0.05
Truncation Boundaries.....	None
Prior Distribution of λ_2	Normal (Mean, SD)
Mean.....	0.7
SD.....	0.15
Truncation Boundaries.....	None
Prior Distribution of ϕ	Normal (Mean, SD)
Mean.....	1.8
SD.....	.04
Truncation Boundaries.....	None

Options Tab

Number of Computation Points for each.....	10
Prior Distribution	
Maximum N1 in Sample Size Search	5000

Output

Click the Calculate button to perform the calculations and generate the following output.

Numeric Reports

Numeric Results

Solve For: [Sample Size](#)
 Hypotheses: $H_0: \lambda_2 / \lambda_1 \geq RR_0$ vs. $H_1: \lambda_2 / \lambda_1 < RR_0$
 Variance Method: Use Assumed True Event Rates
 Prior Type: Independent Univariate Distributions

Prior Distributions

$\mu(t)$: Normal (Mean = 1, SD = 0.03).
 λ_1 : Normal (Mean = 1, SD = 0.05).
 λ_2 : Normal (Mean = 0.7, SD = 0.15).
 φ : Normal (Mean = 1.8, SD = 0.04).

Assurance	Power‡	N1	N2	N	Average Exposure Time E($\mu(t)$)	Event Rate		Rate Ratio		Dispersion E(φ)	Alpha
						Group 1 E(λ_1)	Group 2 E(λ_2)	Actual RR	Sup-Marg RR0		
0.40079	0.33701	164	164	328	1	1	0.7	0.7	0.9	1.8	0.025
0.50009	0.49427	262	262	524	1	1	0.7	0.7	0.9	1.8	0.025
0.60011	0.71371	441	441	882	1	1	0.7	0.7	0.9	1.8	0.025
0.70002	0.94097	859	859	1718	1	1	0.7	0.7	0.9	1.8	0.025
0.80001	0.99999	2632	2632	5264	1	1	0.7	0.7	0.9	1.8	0.025

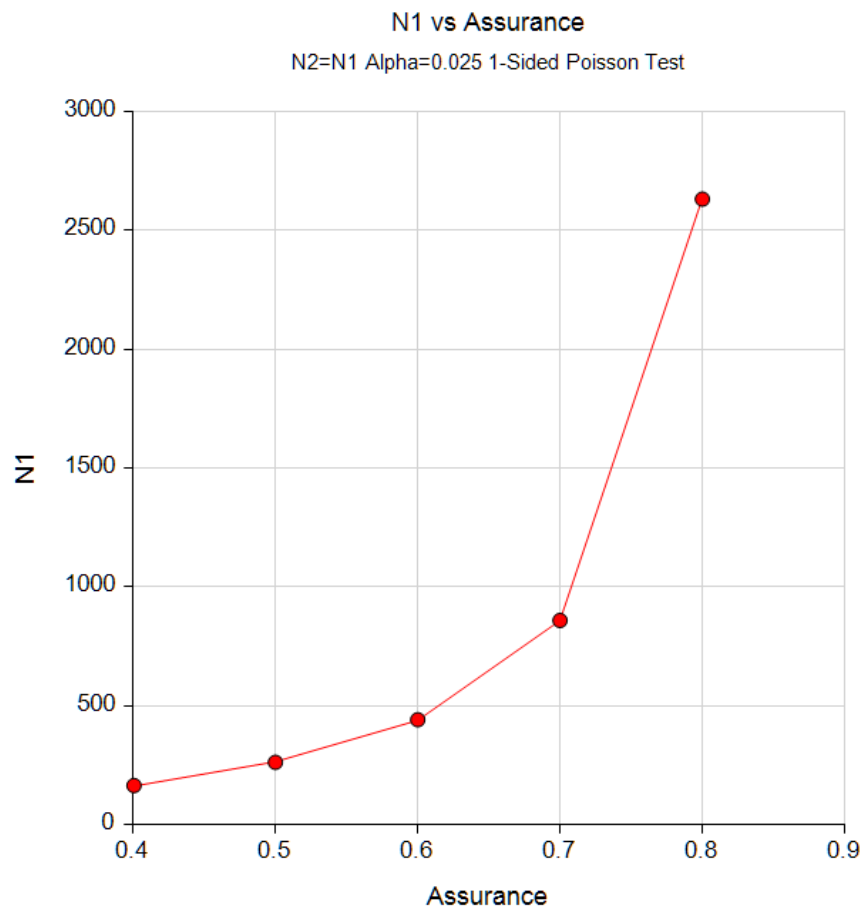
* The number of points used for computation of the prior(s) was 10.

‡ Power was calculated using $\lambda_1 = E(\lambda_1) = 1$, $\lambda_2 = E(\lambda_2) = 0.7$, $\mu(t) = E(\mu(t)) = 1$, and $\varphi = E(\varphi) = 1.8$.

This report shows the required sample size for each assurance target.

Plots Section

Plots



This plot shows the relationship between the sample size and assurance.

Example 4 – Joint Prior Distribution

The following example shows the complexity required to specify a joint distribution for four parameters.

Suppose a one-sided test will be used in which $N_1 = N_2 = 800$, $RR_0 = 0.9$, and the significance level is 0.025.

Further suppose that the joint prior distribution of the λ_1 (control), λ_2 (treatment), $\mu(t)$, and φ is approximated by the following table. In a real study, the values in this table would be provided by an elicitation study.

Note that the program will rescale the probabilities so they sum to one.

λ_1	λ_2	$\mu(t)$	φ	Prob
0.95	0.6	0.96	1.7	0.04
0.95	0.8	0.96	1.7	0.06
1.05	0.6	0.96	1.7	0.06
1.05	0.8	0.96	1.7	0.09
0.95	0.6	0.96	1.9	0.04
0.95	0.8	0.96	1.9	0.06
1.05	0.6	0.96	1.9	0.06
1.05	0.8	0.96	1.9	0.09
0.95	0.6	1.04	1.7	0.04
0.95	0.8	1.04	1.7	0.06
1.05	0.6	1.04	1.7	0.06
1.05	0.8	1.04	1.7	0.09
0.95	0.6	1.04	1.9	0.04
0.95	0.8	1.04	1.9	0.06
1.05	0.6	1.04	1.9	0.06
1.05	0.8	1.04	1.9	0.09

To run this example, the spreadsheet will need to be loaded with the following five columns.

<u>C1</u>	<u>C2</u>	<u>C3</u>	<u>C4</u>	<u>C5</u>
0.95	0.6	0.96	1.7	0.04
0.95	0.8	0.96	1.7	0.06
1.05	0.6	0.96	1.7	0.06
1.05	0.8	0.96	1.7	0.09
0.95	0.6	0.96	1.9	0.04
0.95	0.8	0.96	1.9	0.06
1.05	0.6	0.96	1.9	0.06
1.05	0.8	0.96	1.9	0.09
0.95	0.6	1.04	1.7	0.04
0.95	0.8	1.04	1.7	0.06
1.05	0.6	1.04	1.7	0.06
1.05	0.8	1.04	1.7	0.09
0.95	0.6	1.04	1.9	0.04
0.95	0.8	1.04	1.9	0.06
1.05	0.6	1.04	1.9	0.06
1.05	0.8	1.04	1.9	0.09

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 4** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Design Tab

Solve For **Assurance**
 Prior Entry Method **Combined (Enter parameter values and probabilities on spreadsheet)**
 Higher Poisson Rates Are **Worse**
 Variance Calculation Method **Using Assumed True Rates**
 Alpha **0.025**
 Column of $\mu(t)$ Values **C3**
 Group Allocation **Equal (N1 = N2)**
 Sample Size Per Group **800**
 RR0 (Superiority Margin Ratio) **0.9**
 Column of λ_1 Values **C1**
 Column of λ_2 Values **C2**
 Column of ϕ Values **C4**
 Column of Pr(Values) **C5**

Options Tab

Number of Computation Points for each **10**
 Prior Distribution
 Maximum N1 in Sample Size Search **5000**

Input Spreadsheet Data

Row	C1	C2	C3	C4	C5
1	0.95	0.6	0.96	1.7	0.03
2	0.95	0.8	0.96	1.7	0.06
3	1.05	0.6	0.96	1.7	0.08
4	1.05	0.8	0.96	1.7	0.09
5	0.95	0.6	0.96	1.9	0.13
6	0.95	0.8	0.96	1.9	0.06
7	1.05	0.6	0.96	1.9	0.08
8	1.05	0.8	0.96	1.9	0.09
9	0.95	0.6	1.04	1.7	0.12
10	0.95	0.8	1.04	1.7	0.06
11	1.05	0.6	1.04	1.7	0.08
12	1.05	0.8	1.04	1.7	0.09
13	0.95	0.6	1.04	1.9	0.14
14	0.95	0.8	1.04	1.9	0.06
15	1.05	0.6	1.04	1.9	0.08
16	1.05	0.8	1.04	1.9	0.09

Output

Click the Calculate button to perform the calculations and generate the following output.

Numeric Results

Solve For: [Assurance](#)
 Hypotheses: H0: $\lambda_2 / \lambda_1 \geq RR0$ vs. H1: $\lambda_2 / \lambda_1 < RR0$
 Variance Method: Use Assumed True Event Rates
 Prior Type: Joint Multivariate Distribution

Prior Distribution
 Point Lists
 λ_1 : C1: 0.95 0.95 1.05 1.05 0.95 0.95 1.05 1.05 0.95 0.95 1.05 1.05 0.95 0.95 1.05 1.05
 λ_2 : C2: 0.6 0.8 0.6 0.8 0.6 0.8 0.6 0.8 0.6 0.8 0.6 0.8 0.6 0.8 0.6 0.8
 $\mu(t)$: C3: 0.96 0.96 0.96 0.96 0.96 0.96 0.96 0.96 1.04 1.04 1.04 1.04 1.04 1.04 1.04 1.04
 ϕ : C4: 1.7 1.7 1.7 1.7 1.9 1.9 1.9 1.9 1.7 1.7 1.7 1.7 1.9 1.9 1.9 1.9
 Prob: C5: 0.03 0.06 0.08 0.09 0.13 0.06 0.08 0.09 0.12 0.06 0.08 0.09 0.14 0.06 0.08 0.09

Assurance	Power‡	N1	N2	N	Average Exposure Time $E(\mu(t))$	Event Rate		Rate Ratio		Dispersion $E(\phi)$	Alpha
						Group 1 $E(\lambda_1)$	Group 2 $E(\lambda_2)$	Actual RR	Sup-Marg RR0		
0.75414	0.9489	800	800	1600	1.00299	1.00075	0.68955	0.68904	0.9	1.80896	0.025

‡ Power was calculated using $\lambda_1 = E(\lambda_1) = 1.00075$, $\lambda_2 = E(\lambda_2) = 0.68955$, $\mu(t) = E(\mu(t)) = 1.00299$, and $\phi = E(\phi) = 1.80896$.

PASS has calculated the assurance as 0.75414.

Example 5 – Joint Prior Validation

The problem given in Example 2 will be used to validate the joint prior distribution method. This will be done by running the independent-prior scenario used in that example through the joint-prior method and checking that the assurance values match.

The joint prior distribution can be found by multiplying the four independent probabilities in each row. This results in the following discrete probability distribution.

λ_1	λ_2	$\mu(t)$	φ	Prob
1.2	1.3	0.95	1.7	0.04
1.2	1.7	0.95	1.7	0.06
1.6	1.3	0.95	1.7	0.06
1.6	1.7	0.95	1.7	0.09
1.2	1.3	0.95	1.9	0.04
1.2	1.7	0.95	1.9	0.06
1.6	1.3	0.95	1.9	0.06
1.6	1.7	0.95	1.9	0.09
1.2	1.3	1.05	1.7	0.04
1.2	1.7	1.05	1.7	0.06
1.6	1.3	1.05	1.7	0.06
1.6	1.7	1.05	1.7	0.09
1.2	1.3	1.05	1.9	0.04
1.2	1.7	1.05	1.9	0.06
1.6	1.3	1.05	1.9	0.06
1.6	1.7	1.05	1.9	0.09

To run this example, the spreadsheet is loaded with the following five columns.

C1	C2	C3	C4	C5
1.2	1.3	0.95	1.7	0.04
1.2	1.7	0.95	1.7	0.06
1.6	1.3	0.95	1.7	0.06
1.6	1.7	0.95	1.7	0.09
1.2	1.3	0.95	1.9	0.04
1.2	1.7	0.95	1.9	0.06
1.6	1.3	0.95	1.9	0.06
1.6	1.7	0.95	1.9	0.09
1.2	1.3	1.05	1.7	0.04
1.2	1.7	1.05	1.7	0.06
1.6	1.3	1.05	1.7	0.06
1.6	1.7	1.05	1.7	0.09
1.2	1.3	1.05	1.9	0.04
1.2	1.7	1.05	1.9	0.06
1.6	1.3	1.05	1.9	0.06
1.6	1.7	1.05	1.9	0.09

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 5** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Design Tab

Solve For **Assurance**
 Prior Entry Method **Combined (Enter parameter values and probabilities on spreadsheet)**
 Higher Poisson Rates Are **Worse**
 Variance Calculation Method **Using Assumed True Rates**
 Alpha **0.025**
 Column of $\mu(t)$ Values **C3**
 Group Allocation **Equal (N1 = N2)**
 Sample Size Per Group **800**
 RR0 (Superiority Margin Ratio) **0.9**
 Column of λ_1 Values **C1**
 Column of λ_2 Values **C2**
 Column of ϕ Values **C4**
 Column of Pr(Values) **C5**

Options Tab

Number of Computation Points for each **10**
 Prior Distribution
 Maximum N1 in Sample Size Search **5000**

Input Spreadsheet Data

Row	C1	C2	C3	C4	C5
1	0.95	0.6	0.96	1.7	0.04
2	0.95	0.8	0.96	1.7	0.06
3	1.05	0.6	0.96	1.7	0.06
4	1.05	0.8	0.96	1.7	0.09
5	0.95	0.6	0.96	1.9	0.04
6	0.95	0.8	0.96	1.9	0.06
7	1.05	0.6	0.96	1.9	0.06
8	1.05	0.8	0.96	1.9	0.09
9	0.95	0.6	1.04	1.7	0.04
10	0.95	0.8	1.04	1.7	0.06
11	1.05	0.6	1.04	1.7	0.06
12	1.05	0.8	1.04	1.7	0.09
13	0.95	0.6	1.04	1.9	0.04
14	0.95	0.8	1.04	1.9	0.06
15	1.05	0.6	1.04	1.9	0.06
16	1.05	0.8	1.04	1.9	0.09

Output

Click the Calculate button to perform the calculations and generate the following output.

Numeric Results

Solve For: [Assurance](#)
 Hypotheses: H0: $\lambda_2 / \lambda_1 \geq RR0$ vs. H1: $\lambda_2 / \lambda_1 < RR0$
 Variance Method: Use Assumed True Event Rates
 Prior Type: Joint Multivariate Distribution

Prior Distribution
 Point Lists
 λ_1 : C1: 0.95 0.95 1.05 1.05 0.95 0.95 1.05 1.05 0.95 0.95 1.05 1.05 0.95 0.95 1.05 1.05
 λ_2 : C2: 0.6 0.8 0.6 0.8 0.6 0.8 0.6 0.8 0.6 0.8 0.6 0.8 0.6 0.8 0.6 0.8
 $\mu(t)$: C3: 0.96 0.96 0.96 0.96 0.96 0.96 0.96 0.96 1.04 1.04 1.04 1.04 1.04 1.04 1.04 1.04
 ϕ : C4: 1.7 1.7 1.7 1.7 1.9 1.9 1.9 1.9 1.7 1.7 1.7 1.7 1.9 1.9 1.9 1.9
 Prob: C5: 0.04 0.06 0.06 0.09 0.04 0.06 0.06 0.09 0.04 0.06 0.06 0.09 0.04 0.06 0.06 0.09

Assurance	Power‡	N1	N2	N	Average Exposure Time E($\mu(t)$)	Event Rate		Rate Ratio		Dispersion E(ϕ)	Alpha
						Group 1 E(λ_1)	Group 2 E(λ_2)	Actual RR	Sup-Marg RR0		
0.67211	0.8899	800	800	1600	1	1.01	0.72	0.71287	0.9	1.8	0.025

‡ Power was calculated using $\lambda_1 = E(\lambda_1) = 1.01$, $\lambda_2 = E(\lambda_2) = 0.72$, $\mu(t) = E(\mu(t)) = 1$, and $\phi = E(\phi) = 1.8$.

PASS has also calculated the assurance as 0.67211 which matches Example 2 and thus validates the procedure.