Chapter 726

Assurance for Tests for the Difference of Two Hazard Rates Assuming an Exponential Model

Introduction

This procedure calculates the assurance of tests for the difference of two hazard rates which assume an exponential model. These results can also be used for a logrank test and a proportional hazards test. The assurance calculation in this procedure is based on a user-specified prior distribution of the applicable parameters. This procedure may also be used to determine the needed sample size to obtain a specified assurance.

The procedure is based on the *unconditional* method of Chow, Shao, and Wang (2008) which, in turn, is based on the *conditional* methods of Lachin and Foulkes (1986). The conditional procedure does not extend to non-inferiority, non-zero null, or equivalence tests as easily as the unconditional method does (see Chow, Shao, and Wang (2008) page 173). The power calculations are based on the **PASS** procedure *Tests for the Difference of Two Hazard Rates Assuming an Exponential Model*. Refer to that procedure for more details on the test.

The assurance calculation used in this procedure is based on O'Hagan, Stevens, and Campbell (2005).

Assurance

The assurance of a design is the expected value of the power with respect to one or more prior distributions of the design parameters. Assurance is also referred to as *Bayesian assurance*, *expected power*, *average power*, *statistical assurance*, *hybrid classical-Bayesian procedure*, or *probability of success*.

The power of a design is the probability of rejecting the null hypothesis, conditional on a given set of design attributes, such as the test statistic, the significance level, the sample size, and the effect size to be detected. As many of the parameters are typically unknown quantities, the stated power may be very different from the true power if the specified parameter values are inaccurate.

While power is conditional on individual design parameter values, and is highly sensitive to those values, assurance is the average power across a presumed prior distribution of the parameters. Thus, assurance adds a Bayesian element to the frequentist framework, resulting in a hybrid approach to the probability of trial or study success. It should be noted that when it comes time to perform the statistical test on the resulting data, these methods for calculating assurance assume that the traditional (frequentist) tests will be used.

The next section describes some of the ways in which the prior distributions for effect size parameters may be determined.

Elicitation

In order to calculate assurance, a suitable prior distribution for the applicable parameters must be determined. This process is called the *elicitation* of the prior distribution.

The elicitation may be as simple as choosing a distribution that seems plausible for the parameter(s) of interest, or as complex as combining the informed advice of several experts based on experience in the field, available pilot data, or previous studies. The accuracy of the assurance value depends on the accuracy of the elicited prior distribution. The assumption (or hope) is that an informed prior distribution will produce a more accurate estimate of the probability of trial success than a single value estimate. Because clinical trials and other studies are often costly, many institutions now routinely require an elicitation step.

Two reference texts that focus on elicitation are O'Hagan, Buck, Daneshkhah, Eiser, Garthwaite, Jenkinson, Oakley, and Rakow (2006) and Dias, Morton, and Quigley (2018).

Technical Details

We assume that a study is to be made to compare the hazard rates of a control group and an experimental group. The control group (group 1) consists of patients that will receive the existing treatment. In cases where no existing treatment exists, group 1 consists of patients that will receive a placebo. Group 2 will receive the new treatment.

We assume that the critical event of interest is death and that two treatments have survival distributions with instantaneous death (hazard) rates, λ_1 and λ_2 . These hazard rates are a subject's probability of death in a short period of time. The survival times are assumed to be exponential. This section presents the *unconditional* method of Chow, Shao, and Wang (2008).

Basic Model

Suppose a clinical trial consists of two independent groups labeled "1" and "2" (where group 1 is the control group and group 2 is the treatment group). The total sample size is N and the sizes of the two groups are N_1 and N_2 . Usually, you would plan to have $N_1 = N_2$.

Test Statistic

The power and sample size formulas presented below are for the logrank test statistic. However, they were originally developed for comparing the difference of two exponential hazard rates. Simulation studies then showed that they approximated the power of the logrank test.

Test Comparing Hazard Rates

The original test statistic is the difference of the hazard rates estimated by maximum likelihood divided by their standard error. The maximum likelihood estimate of an exponential hazard rate for a particular group is

$$\hat{\lambda} = \frac{\text{number of events}}{\text{sum of study time of all subjects}}$$

Chow, Shao, and Wang (2008) indicate that the test statistic

$$Z = \frac{\hat{\lambda}_2 - \hat{\lambda}_1}{\sqrt{\frac{\sigma^2(\hat{\lambda}_1)}{N_1} + \frac{\sigma^2(\hat{\lambda}_2)}{N_2}}}$$

where

$$\sigma^{2}(\lambda) = \frac{\lambda^{2}}{1 + \frac{e^{-\lambda T}(1 - e^{\lambda R})}{\lambda R}}$$

follows the standard normal standard normal distribution at least approximately.

Power Calculations

Assuming an exponential model with hazard rates λ_1 and λ_2 for the two groups, Chow et al. (2008) give the following equation relating N and power of a two-tailed test.

$$\frac{(\lambda_2 - \lambda_1)}{\sqrt{\frac{\sigma^2(\lambda_1, \omega_1, G)}{N_1} + \frac{\sigma^2(\lambda_2, \omega_2, G)}{N_2}}} - z_{1-\alpha/2} = z_{1-\beta}$$

where

$$\sigma^{2}(\lambda_{i}, \omega_{i}, G) = \frac{\lambda_{i}^{2}}{E(d_{i}|\lambda_{i}, \omega_{i}, G)}$$

$$E(d_{i}|\lambda_{i}, \omega_{i}, G) = \left(\frac{\lambda_{i}}{\lambda_{i} + \omega_{i}}\right) \left(1 + \frac{G \exp\{-(\lambda_{i} + \omega_{i})T\} \left[1 - \exp\{(\lambda_{i} + \omega_{i} - G)R\}\right]}{(\lambda_{i} + \omega_{i} - G)\left[1 - \exp\{-GR\}\right]}\right)$$

$$E(d_{i}|\lambda_{i}, \omega_{i}, 0) = \left(\frac{\lambda_{i}}{\lambda_{i} + \omega_{i}}\right) \left(1 + \frac{\exp\{-(\lambda_{i} + \omega_{i})T\} \left[1 - \exp\{(\lambda_{i} + \omega_{i})R\}\right]}{(\lambda_{i} + \omega_{i})R}\right)$$

These parameters are interpreted as follows:

<u>Parameter</u>	<u>Interpretation</u>
$\sigma^2(\lambda,\omega,G)$	Variance of $\hat{\lambda}$
$E(d_i \lambda_i,\omega_i,G)$	Expected proportion of events (deaths) in group i
d_i	Indicates a person does $(d_i=1)$ or does not $(d_i=0)$ die in group i

Assurance for Tests for the Difference of Two Hazard Rates Assuming an Exponential Model

 λ_i Hazard rate of group *i* (see below)

 ω_i Loss to follow-up hazard rate of group i (see below)

A Patient entry parameter (see below)

R Accrual time

T Total time

T - R Follow-up time

Exponential Distribution

The hazard rate from the exponential distribution, λ , is usually estimated using maximum likelihood techniques. In the planning stages, you have to obtain an estimate of this parameter. To see how to accomplish this, let's briefly review the exponential distribution. The density function of the exponential is defined as

$$f(t) = \lambda \exp{-\lambda t}, t \ge 0, \lambda > 0.$$

The cumulative survival distribution function is

$$S(t) = \exp{-\lambda t}, t \ge 0.$$

Solving this for λ yields

$$\lambda = -\frac{\log\{S(t)\}}{t}$$

Note that S(t) gives the probability of surviving t years. To obtain a planning estimate of λ , you need only know the proportion surviving during a particular time period. You can then use the above equation to calculate λ .

Patient Entry

Patients are enrolled during the accrual period. **PASS** lets you specify the pattern in which subjects are enrolled. Suppose patient entry times are distributed as g(t) where t_i is the entry time of the i^{th} individual and $0 \le t_i \le R$. Let g(t) follow the truncated exponential distribution with parameter G, which has the density

$$g(t) = \begin{cases} \frac{G \exp\{-Gt\}}{1 - G \exp\{-GR\}} & \text{if } 0 \le t \le R, \ G \ne 0 \\ 1 & \text{otherwise} \end{cases}$$

where

R is accrual time.

G is interpreted as follows:

G > 0 results in a convex (faster than expected) entry distribution.

G < 0 results in a concave (slower than expected) entry distribution.

G=0 results in the uniform entry distribution in which g(t)=1/R.

Rather than specify *G* directly, **PASS** has you enter the percentage of the accrual time (called *A*) that will be needed to enroll 50% of the subjects. Using an iterative search, the value of *G* corresponding to this percentage is calculated and used in the calculations.

Losses to Follow-Up

The staggered patient entry over the accrual period results in censoring times ranging from T-R to T years during the follow-up period. This is often referred to as administrative censoring, since it is caused by the conclusion of the study rather than by some random factor working on an individual. To model the losses to follow-up in each group which come from other causes, we use the exponential distribution again, this time with hazard rates ω_1 and ω_2 . You can obtain appropriate loss-to-follow-up hazard rates using the following formula or by using the Survival Parameter Conversion Tool available from the Tools menu or by pressing the small button to the rate of the loss-to-follow-up hazard rate box.

$$\omega = -\frac{\log\{1 - P_{loss}(R)\}}{R}$$

Assurance Calculation

This assurance computation described here is based on O'Hagan, Stevens, and Campbell (2005).

Let $P_1(H|\lambda_1,\lambda_2,\omega_1,\omega_2,A)$ be the power function described above where H is the event that the null hypothesis is rejected conditional on a specific set of parameter values. The specification of $\lambda_1,\lambda_2,\omega_1,\omega_2$, and A is critical to the power calculation, but the actual values are seldom known. Assurance is defined as the expected power where the expectation is with respect to a joint prior distribution for $\lambda_1,\lambda_2,\omega_1,\omega_2$, and A. Hence, assurance is

$$Assurance = E_{\lambda_{1},\lambda_{2},\omega_{1},\omega_{2},A}(P_{1}(H|\lambda_{1},\lambda_{2},\omega_{1},\omega_{2},A))$$

$$= \iiint P_{1}(H|\lambda_{1},\lambda_{2},\omega_{1},\omega_{2},A)f(\lambda_{1},\lambda_{2},\omega_{1},\omega_{2},A)d\lambda_{1}d\lambda_{2}d\omega_{1}d\omega_{2}dA$$

where $f(\lambda_1, \lambda_2, \omega_1, \omega_2, A)$ is the joint prior density of $\lambda_1, \lambda_2, \omega_1, \omega_2$, and A.

In **PASS**, the joint prior distribution can be specified as either a discrete approximation to the joint prior distribution, or as individual prior distributions, one for each parameter.

Specifying a Joint Prior Distribution

If the joint prior distribution is to be specified directly, the distribution is specified in **PASS** using a discrete approximation to the function $f(\lambda_1, \lambda_2, \omega_1, \omega_2, A)$. This provides flexibility in specifying the joint prior distribution. In the five-parameter case, six columns are entered on the spreadsheet: five for the parameters and a sixth for the probability. Each row gives a value for each parameter and the corresponding parameter-combination probability. The accuracy of the distribution approximation is controlled by the number of points (spreadsheet rows) that are used.

An example of entering a joint prior distribution is included at the end of the chapter.

Specifying Individual Prior Distributions

Ciarleglio, Arendt, and Peduzzi (2016) suggest that more flexibility is available if the joint prior distribution is separated into five independent univariate distributions as follows:

$$f(\lambda_1, \lambda_2, \omega_1, \omega_2, A) = f_1(\lambda_1) f_2(\lambda_2) f_3(\omega_1) f_4(\omega_2) f_5(A)$$

where $f_1(\lambda_1)$ is the prior distribution of λ_1 , $f_2(\lambda_2)$ is the prior distribution of λ_2 , and so on. This is the definition that is used in **PASS**. The definition of assurance becomes

$$Assurance = E_{\lambda_1,\lambda_2,\omega_1,\omega_2,A} (P_1(H|\lambda_1,\lambda_2,\omega_1,\omega_2,A))$$

$$= \iiint \int \int \int \int P_1(H|\lambda_1,\lambda_2,\omega_1,\omega_2,A) f_1(\lambda_1) f_2(\lambda_2) f_3(\omega_1) f_4(\omega_2) f_5(A) d\lambda_1 d\lambda_2 d\omega_1 d\omega_2 dA$$

Using this definition, the assurance can be calculated using numerical integration. There are a variety of pre-programmed, univariate prior distributions available in **PASS**.

Assurance for Tests for the Difference of Two Hazard Rates Assuming an Exponential Model

Fixed Values (No Prior) and Custom Values

For any given parameter, **PASS** also provides the option of entering a single fixed value for the prior distribution, or a series of values and corresponding probabilities (using the spreadsheet), rather than one of the pre-programmed distributions.

Numerical Integration in PASS (and Notes on Computation Speed)

When the prior distribution is specified as independent univariate distributions, **PASS** uses a numerical integration algorithm to compute the assurance value as follows:

The domain of each prior distribution is divided into M intervals. Since many of the available prior distributions are unbounded on one (e.g., Gamma) or both (e.g., Normal) ends, an approximation is made to make the domain finite. This is accomplished by truncating the distribution to a domain between the two quantiles: $q_{0.001}$ and $q_{0.999}$.

The value of M controls the accuracy and speed of the algorithm. If only one parameter is to be given a prior distribution, then a value of M between 50 and 100 usually gives an accurate result in a timely manner. However, if two parameters are given priors, the number of iterations needed increases from M to M^2 . For example, if M is 100, 10000 iterations are needed. Reducing M from 100 to 50 reduces the number of iterations from 10000 to 2500.

The algorithm runtime increases when searching for sample size rather than solving for assurance, as a search algorithm is employed in this case. When solving for sample size, we recommend reducing *M* to 20 or less while exploring various scenarios, and then increasing *M* to 50 or more for a final, more accurate, result.

List of Available Univariate Prior Distributions

This section lists the univariate prior distributions that may be used for any of the applicable parameters when the Prior Entry Method is set to Individual.

No Prior

If 'No Prior' is chosen for a parameter, the parameter is assumed to take on a single, fixed value with probability one.

Beta (Shape 1, Shape 2, a, c)

A random variable X that follows the beta distribution is defined on a finite interval [a, c]. Two shape parameters (α and β) control the shape of this distribution. Two location parameters α and c give the minimum and maximum of X.

The probability density function of the beta distribution is

$$f(x|\alpha,\beta,a,c) = \frac{\left(\frac{x-a}{c-a}\right)^{\alpha-1} \left(\frac{c-x}{c-a}\right)^{\beta-1}}{(c-a)B(\alpha,\beta)}$$

where $B(\alpha, \beta) = \Gamma(\alpha) \Gamma(\beta) / \Gamma(\alpha + \beta)$ and $\Gamma(z)$ is the gamma function.

The mean of X is

$$\mu_X = \frac{\alpha c + \beta a}{\alpha + \beta}$$

Various distribution shapes are controlled by the values of α and β . These include

Symmetric and Unimodal

$$\alpha = \beta > 1$$

U Shaped

$$\alpha = \beta < 1$$

Bimodal

$$\alpha, \beta < 1$$

Uniform

$$\alpha = \beta = 1$$

Parabolic

$$\alpha = \beta = 2$$

Bell-Shaped

$$\alpha = \beta > 2$$

Gamma (Shape, Scale)

A random variable X that follows the gamma distribution is defined on the interval $(0, \infty)$. A shape parameter, κ , and a scale parameter, θ , control the distribution.

The probability density function of the gamma distribution is

$$f(x|\kappa,\theta) = \frac{x^{\kappa-1}e^{-\frac{x}{\theta}}}{\theta^{\kappa}\Gamma(\kappa)}$$

where $\Gamma(z)$ is the gamma function.

The mean of X is

$$\mu_X = \frac{\kappa}{\theta}$$

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(Min \le X \le Max)$ where Min and Max are two truncation bounds.

Inverse-Gamma (Shape, Scale)

A random variable X that follows the inverse-gamma distribution is defined on the interval $(0, \infty)$. If $Y \sim$ gamma, then X = 1 / $Y \sim$ inverse-gamma. A shape parameter, α , and a scale parameter, β , control the distribution.

The probability density function of the inverse-gamma distribution is

$$f(x|\alpha,\beta) = \frac{\beta^{\alpha} x^{\alpha-1} e^{-\frac{\beta}{x}}}{\Gamma(\alpha)}$$

where $\Gamma(z)$ is the gamma function.

The mean of X is

$$\mu_X = \frac{\beta}{\alpha - 1}$$
 for $\alpha > 1$

Logistic (Location, Scale)

A random variable X that follows the logistic distribution is defined on the interval $(-\infty, \infty)$. A location parameter, μ , and a scale parameter, s, control the distribution.

The probability density function of the logistic distribution is

$$f(x|\mu,s) = \frac{e^{-\frac{x-\mu}{s}}}{s\left(1 + e^{-\frac{x-\mu}{s}}\right)^2}$$

The mean of X is

$$\mu_X = \mu$$

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(Min \le X \le Max)$ where Min and Max are two truncation bounds.

Lognormal (Mean, SD)

A random variable X that follows the lognormal distribution is defined on the interval $(0, \infty)$. A location parameter, $\mu_{\log(X)}$, and a scale parameter, $\sigma_{\log(X)}$, control the distribution. If $Z \sim$ standard normal, then $X = e^{\mu + \sigma Z} \sim \text{lognormal}$. Note that $\mu_{\log(X)} = E(\log(X))$ and $\sigma_{\log(X)} = Standard\ Deviation(\log(X))$.

The probability density function of the lognormal distribution is

$$f(x|\mu,\sigma) = \frac{e^{-\frac{1}{2}\left(\frac{\log x - \mu}{\sigma}\right)^2}}{x\sigma\sqrt{2\pi}}$$

The mean of X is

$$\mu_X = e^{\mu + \frac{\sigma^2}{2}}$$

LogT (Mean, SD)

A random variable X that follows the logT distribution is defined on the interval $(0, \infty)$. A location parameter, $\mu_{\log(X)}$, a scale parameter, $\sigma_{\log(X)}$, and a shape parameter, ν , control the distribution. Note that ν is referred to as the *degrees of freedom*.

If t ~ Student's t, then $X = e^{\mu + \sigma t} \sim \log T$.

The probability density function of the logT distribution is

$$f(x|\mu,\sigma,\nu) = \frac{\Gamma\left(\frac{\nu+1}{2}\right)}{x\Gamma\left(\frac{\nu}{2}\right)\sigma\sqrt{\nu\pi}} \left(1 + \frac{1}{\nu}\left(\frac{\log x - \mu}{\sigma}\right)^2\right)^{\left(\frac{-\nu-1}{2}\right)}$$

The mean of *X* is not defined.

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(Min \le X \le Max)$ where Min and Max are two truncation bounds.

Normal (Mean, SD)

A random variable *X* that follows the normal distribution is defined on the interval $(-\infty, \infty)$. A location parameter, μ , and a scale parameter, σ , control the distribution.

The probability density function of the normal distribution is

$$f(x|\mu,\sigma) = \frac{e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}}{\sigma\sqrt{2\pi}}$$

The mean of X is

$$\mu_X = \mu$$

A truncated version of the distribution is constructed by dividing the density by $1 - \text{Prob}(Min \le X \le Max)$ where Min and Max are two truncation bounds.

T (Mean, SD, DF)

A random variable X that follows Student's t distribution is defined on the interval $(-\infty, \infty)$. A location parameter, μ , a scale parameter, σ , and a shape parameter, ν , control the distribution. Note that ν is referred to as the *degrees of freedom* or *DF*.

The probability density function of the Student's t distribution is

$$f(x|\mu,\sigma,\nu) = \frac{\Gamma\left(\frac{\nu+1}{2}\right)}{\Gamma\left(\frac{\nu}{2}\right)\sigma\sqrt{\nu\pi}} \left(1 + \frac{1}{\nu}\left(\frac{x-\mu}{\sigma}\right)^2\right)^{\left(\frac{-\nu-1}{2}\right)}$$

The mean of *X* is μ if $\nu > 1$.

Triangle (Mode, Min, Max)

Let a = minimum, b = maximum, and c = mode. A random variable X that follows a triangle distribution is defined on the interval (a, b).

The probability density function of the triangle distribution is

$$f(x|a,b,c) = \begin{cases} \frac{2(x-a)}{(b-a)(c-a)} & \text{for } a \le x < c \\ \frac{2}{b-a} & \text{for } x = c \\ \frac{2(b-x)}{(b-a)(b-c)} & \text{for } c < x \le b \end{cases}$$

The mean of X is

$$\frac{a+b+c}{3}$$

Uniform (Min, Max)

Let a = minimum and b = maximum. A random variable X that follows a uniform distribution is defined on the interval [a, b].

The probability density function of the uniform distribution is

$$f(x|a,b) = \begin{cases} \frac{1}{b-a} & \text{for } a \le x \le b \end{cases}$$

The mean of X is

$$\frac{a+b}{2}$$

Weibull (Shape, Scale)

A random variable X that follows the Weibull distribution is defined on the interval $(0, \infty)$. A shape parameter, κ , and a scale parameter, λ , control the distribution.

The probability density function of the Weibull distribution is

$$f(x|\kappa,\lambda) = \frac{\kappa}{\lambda} \left(\frac{x}{\lambda}\right)^{\kappa-1} e^{-\left(\frac{x}{\lambda}\right)^{\kappa}}$$

The mean of X is

$$\mu_X = \kappa \Gamma \left(1 + \frac{1}{\kappa} \right)$$

Custom (Values and Probabilities in Spreadsheet)

This custom prior distribution is represented by a set of user-specified points and associated probabilities, entered in two columns of the spreadsheet. The points make up the entire set of values that are used for this parameter in the calculation of assurance. The associated probabilities should sum to one. Note that custom values and probabilities can be used to approximate any continuous distribution.

For example, a prior distribution of X might be

X_i	$\boldsymbol{P_i}$
10	0.2
20	0.2
30	0.3
40	0.2
50	0.1

In this example, the mean of X is

$$\mu_X = \sum_{i=1}^5 X_i P_i$$

Example 1 – Assurance Over a Range of Sample Sizes

A researcher is planning a clinical trial using a parallel, two-group, equal sample allocation design to compare the survivability of a new treatment with that of the current treatment using a one-sided test with a significance level of 0.025. The proportion surviving one-year after the current treatment is 0.50 ($\lambda_1=0.693$). The power is desired when the proportion surviving in new treatment is 0.75 ($\lambda_2=0.288$).

The trial will include a recruitment period of one-year after which participants will be followed for an additional two-years. It is assumed that patients will enter the study uniformly over the accrual period. The researcher estimates a loss-to-follow hazard rate of 0.165 in both the control and the experimental groups.

To complete their sample size study, the researchers want to run an assurance analysis for a range of group sample sizes from 20 to 80. An elicitation exercise determined the prior distributions of the parameters as: $\lambda_1 \sim N(0.693, 0.05)$, $\lambda_2 \sim N(0.288, 0.05)$, $\omega_1 \sim N(0.165, 0.01)$, $\omega_2 \sim N(0.165, 0.01)$, and $A \sim N(50,3)$.

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 1** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Solve For	Assurance
Prior Entry Method	Individual (Enter a prior distribution for each applicable parameter)
Alternative Hypothesis	Η1: λ2 - λ1 < 0
Alpha	0.025
Group Allocation	Equal (N1 = N2)
Sample Size Per Group	20 40 60 80
Prior Distribution of ω1	Normal (Mean, SD)
Mean	0.165
SD	0.01
Truncation Boundaries	None
Prior Distribution of ω2	Normal (Mean, SD)
Mean	0.165
SD	0.01
Truncation Boundaries	None
Accrual Time (R)	1
Follow-Up Time (T - R)	2
Prior Distribution of A	Normal (Mean, SD)
Mean	50
SD	3
Truncation Boundaries	None
Prior Distribution of λ1	Normal (Mean, SD)
Mean	0.693
SD	0.05
Truncation Boundaries	None

Assurance for Tests for the Difference of Two Hazard Rates Assuming an Exponential Model

Prior Distribution of λ2	Normal (Mean, SD)	
Mean	0.288	
SD	0.05	
Truncation Boundaries	None	
Options Tab		
Options Tab Number of Computation Points fo	r each 20	
•	r each 20	

Output

Click the Calculate button to perform the calculations and generate the following output.

Numeric Reports

Numeric Results

Solve For: Assurance

 $\begin{array}{lll} \mbox{Groups:} & 1 = \mbox{Control, } 2 = \mbox{Treatment} \\ \mbox{Hypotheses:} & \mbox{Ho: } \lambda 2 - \lambda 1 \geq 0 \mbox{ vs. } \mbox{H1: } \lambda 2 - \lambda 1 < 0 \\ \mbox{Test Statistic:} & \mbox{Hazard Rate Difference, } \lambda 2 - \lambda 1 \\ \mbox{Elapsed Times:} & \mbox{Accrual = 1, Follow-Up = 2, Total = 3} \\ \mbox{Prior Type:} & \mbox{Independent Univariate Distributions} \\ \end{array}$

Prior Distributions

λ1: Normal (Mean = 0.693, SD = 0.05).
 λ2: Normal (Mean = 0.288, SD = 0.05).
 ω1: Normal (Mean = 0.165, SD = 0.01).
 ω2: Normal (Mean = 0.165, SD = 0.01).
 A: Normal (Mean = 50, SD = 3).

		N	lequire umber Events	of	Sa	ample	Size	Expected Hazard Rate Group 1	Expected Hazard Rate Group 2	Expected Loss Hazard Rate Group 1	Expected Loss Hazard Rate Group 2	Expected Percent Accrual Time until 50% Accrued	
Assurance*	Power‡	E1	E2	Ε	N1	N2	N	Ε(λ1)	Ε(λ2)	Ε(ω1)	Ε(ω2)	E(A)	Alpha
0.49278	0.49292	14	9	23	20	20	40	0.693	0.288	0.165	0.165	50	0.025
0.76209	0.78429	28	17	46	40	40	80	0.693	0.288	0.165	0.165	50	0.025
0.88890	0.91985	43	26	68	60	60	120	0.693	0.288	0.165	0.165	50	0.025
0.94624	0.97285	57	34	91	80	80	160	0.693	0.288	0.165	0.165	50	0.025

^{*} The number of points used for computation of the prior(s) was 20.

Assurance The expected power where the expectation is with respect to the prior distribution(s).

Power The power calculated using the means of the prior distributions as the values of the corresponding parameters.

E1 The required number of events in group 1.
E2 The required number of events in group 2.
E The total number of required events . E = E1 + E2.

 $\begin{array}{lll} \text{N1} & \text{The number of subjects in group 1.} \\ \text{N2} & \text{The number of subjects in group 2.} \\ \text{N} & \text{The total sample size. N = N1 + N2.} \\ \text{E}(\lambda 1) & \text{The expected hazard rate in group 1.} \\ \text{E}(\lambda 2) & \text{The expected hazard rate in group 2.} \\ \end{array}$

 $\begin{array}{ll} E(\omega 1) & \text{The expected hazard rate at which subjects in group 1 are lost to follow-up.} \\ E(\omega 2) & \text{The expected hazard rate at which subjects in group 2 are lost to follow-up.} \\ E(A) & \text{The expected percent of the accrual time until 50% of the subjects are accrued.} \end{array}$

Alpha The probability of rejecting a true null hypothesis.

[‡] Power was calculated using $\lambda 1 = E(\lambda 1) = 0.693$, $\lambda 2 = E(\lambda 2) = 0.288$, $\omega 1 = E(\omega 1) = 0.165$, $\omega 2 = E(\omega 2) = 0.165$, and A = E(A) = 50.

Assurance for Tests for the Difference of Two Hazard Rates Assuming an Exponential Model

Summary Statements

A parallel two-group design will be used to test whether the Group 2 (treatment) hazard rate is less than the Group 1 (control) hazard rate (H0: $\lambda 2 - \lambda 1 \ge 0$ versus H1: $\lambda 2 - \lambda 1 < 0$). The comparison will be made using a one-sided, two-sample Z-test of the hazard rate difference, with a Type I error rate (α) of 0.025. It is intended that subjects will enter the study during an accrual period of 1 time unit(s). The follow-up period is 2 time unit(s). It is assumed that the survival times are exponentially distributed. The prior distribution used for the hazard rate in Group 1 is Normal (Mean = 0.693, SD = 0.05). The prior distribution used for the hazard rate in Group 2 is Normal (Mean = 0.185, SD = 0.01). The prior distribution used for the loss hazard rate in Group 1 is Normal (Mean = 0.165, SD = 0.01). The prior distribution used for the percent of accrual time until 50% are accrued is Normal (Mean = 50, SD = 3). With sample sizes of 20 for Group 1 (control) and 20 for Group 2 (treatment), the assurance (average power) is 0.49278.

References

O'Hagan, A., Stevens, J.W., and Campbell, M.J. 2005. 'Assurance in clinical trial design'. Pharmaceutical Statistics, Volume 4, Pages 187-201.

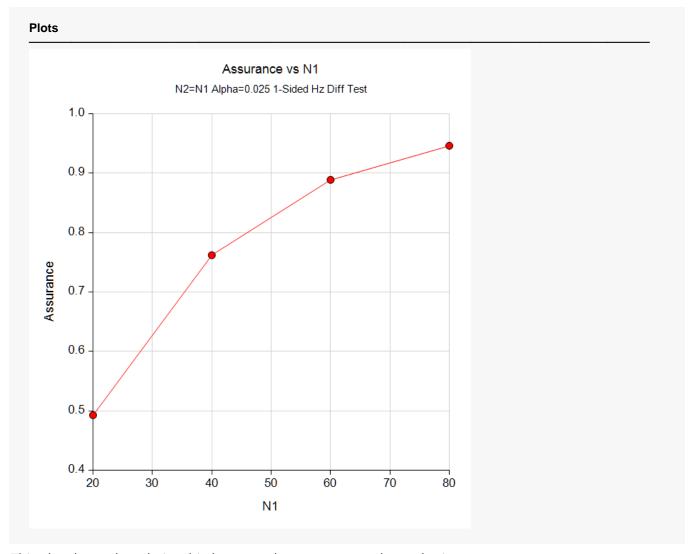
Ciarleglio, M.M., Arendt, C.D., and Peduzzi, P.N. 2016. 'Selection of the effect size for sample size determination for a continuous response in a superiority clinical trial using a hybrid classical and Bayesian procedure'. Clinical Trials, Volume 13(3), pages 275-285.

Dias, L.C., Morton, A., and Quigley, J. 2018. Elicitation, The Science and Art of Structuring Judgement. Springer. Chow, S.C., Shao, J., Wang, H., and Lokhnygina, Y. 2018. Sample Size Calculations in Clinical Research, Third Edition. Taylor & Francis/CRC. Boca Raton, Florida. Section 7.2.1, Page 152.

Lachin, John M. and Foulkes, Mary A. 1986. 'Evaluation of Sample Size and Power for Analyses of Survival with Allowance for Nonuniform Patient Entry, Losses to Follow-up, Noncompliance, and Stratification', Biometrics, Volume 42, September, pages 507-516.

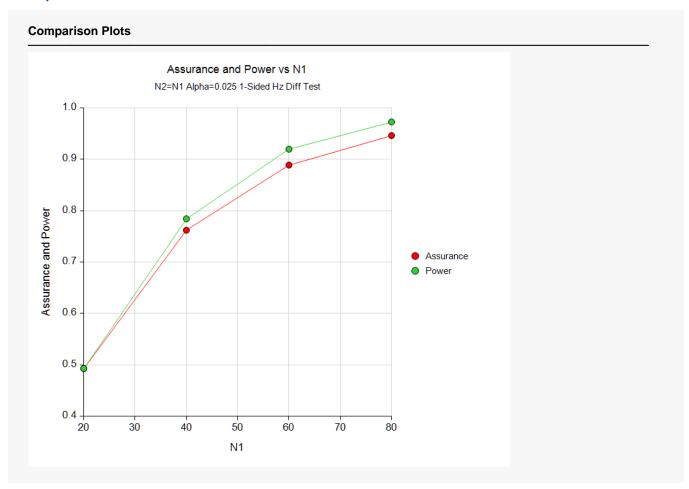
These reports show the assurance values obtained by each sample size.

Plots Section



This plot shows the relationship between the assurance and sample size.

Comparison Plots Section



This plot compares the assurance and power across values of sample size.

Example 2 - Validation using Hand Computation

We could not find a validation example in the literature for this procedure, so we have developed a validation example of our own.

Suppose a one-sided test of the difference between hazard rates will be used in which N1 = N2 = 100 and the significance level is 0.025.

The prior distribution of $\lambda 1$ is approximated by the following table. These are loaded into C1 and C2.

λ1 Prob0.6 0.40.7 0.6

The prior distribution of the $\lambda 2$ is approximated by the following table. These are loaded into C3 and C4.

λ2 Prob0.3 0.40.4 0.6

The prior distribution of the $\omega 1$ is approximated by the following table. These are loaded into C5 and C6.

<u>ω1</u> Prob 0.10 0.5 0.16 0.5

The prior distribution of the $\omega 2$ is approximated by the following table. These are loaded into C7 and C8.

ω2 Prob0.10 0.50.16 0.5

The prior distribution of the A is approximated by the following table. These are loaded into C9 and C10.

<u>A</u> Prob 30 0.5 50 0.5

To run this example, the spreadsheet will need to be loaded with the following ten columns corresponding to the values listed above.

<u>C1</u>	<u>C2</u>	<u>C3</u>	<u>C4</u>	<u>C5</u>	<u>C6</u>	<u>C7</u>	<u>C8</u>	<u>C9</u>	<u>C10</u>
0.6	0.4	0.3	0.4	0.1	0.5	0.1	0.5	30	0.5
0.7	0.6	0.4	0.6	0.16	0.5	0.16	0.5	50	0.5

Assurance for Tests for the Difference of Two Hazard Rates Assuming an Exponential Model

The Tests for the Difference of Two Hazard Rates Assuming an Exponential Model procedure is used to compute the power for each of the 32 parameter combinations. Note that the first report is for A = 30 and the next reports is for A = 50 (Uniform).

Numeric Results

Solve For:

Groups: 1 = Control, 2 = TreatmentHypotheses: $\text{H0: h2 - h1} \ge 0$ vs. Ha: h2 - h1 < 0Accrual: 30% of Accrual Time Results in 50% of Total Enrollment

	9.	ample S	izo	Hazar	d Rate	Hazard Rate	Hazard		oss d Rate	1	Гime		
		ample 3			u Nate	Difference	Ratio		u Nate	Accrual	Follow-Up		Report
Power	N	N1	N2	h1	h2	D	HR	ω1	ω2	R	T - R	Alpha	Row
0.95213	200	100	100	0.6	0.3	-0.3	0.50000	0.10	0.10	1	2	0.025	1
0.62311	200	100	100	0.6	0.4	-0.2	0.66667	0.10	0.10	1	2	0.025	2
0.99282	200	100	100	0.7	0.3	-0.4	0.42857	0.10	0.10	1	2	0.025	3
0.88104	200	100	100	0.7	0.4	-0.3	0.57143	0.10	0.10	1	2	0.025	4
0.94884	200	100	100	0.6	0.3	-0.3	0.50000	0.10	0.16	1	2	0.025	5
0.61356	200	100	100	0.6	0.4	-0.2	0.66667	0.10	0.16	1	2	0.025	6
0.99214	200	100	100	0.7	0.3	-0.4	0.42857	0.10	0.16	1	2	0.025	7
0.87509	200	100	100	0.7	0.4	-0.3	0.57143	0.10	0.16	1	2	0.025	8
0.94442	200	100	100	0.6	0.3	-0.3	0.50000	0.16	0.10	1	2	0.025	9
0.60761	200	100	100	0.6	0.4	-0.2	0.66667	0.16	0.10	1	2	0.025	10
0.99083	200	100	100	0.7	0.3	-0.4	0.42857	0.16	0.10	1	2	0.025	11
0.86924	200	100	100	0.7	0.4	-0.3	0.57143	0.16	0.10	1	2	0.025	12
0.94094	200	100	100	0.6	0.3	-0.3	0.50000	0.16	0.16	1	2	0.025	13
0.59845	200	100	100	0.6	0.4	-0.2	0.66667	0.16	0.16	1	2	0.025	14
0.99005	200	100	100	0.7	0.3	-0.4	0.42857	0.16	0.16	1	2	0.025	15
0.86324	200	100	100	0.7	0.4	-0.3	0.57143	0.16	0.16	1	2	0.025	16

	N	Number o Events	f	Percent		ent ability	Vari	ance	Donort
Power	E	E1	E2	Group 1 %N1	Pr(E1)	Pr(E2)	σ²(h1)	σ²(h2)	Report Row
0.95213	120.8	72.0	48.8	50	0.71987	0.48785	0.50009	0.18448	1
0.62311	130.4	72.0	58.5	50	0.71987	0.58460	0.50009	0.27369	2
0.99282	125.5	76.7	48.8	50	0.76680	0.48785	0.63902	0.18448	3
0.88104	135.1	76.7	58.5	50	0.76680	0.58460	0.63902	0.27369	4
0.94884	117.7	72.0	45.7	50	0.71987	0.45727	0.50009	0.19682	5
0.61356	127.0	72.0	55.0	50	0.71987	0.54977	0.50009	0.29103	6
0.99214	122.4	76.7	45.7	50	0.76680	0.45727	0.63902	0.19682	7
0.87509	131.7	76.7	55.0	50	0.76680	0.54977	0.63902	0.29103	8
0.94442	116.9	68.1	48.8	50	0.68122	0.48785	0.52846	0.18448	9
0.60761	126.6	68.1	58.5	50	0.68122	0.58460	0.52846	0.27369	10
0.99083	121.6	72.8	48.8	50	0.72773	0.48785	0.67332	0.18448	11
0.86924	131.2	72.8	58.5	50	0.72773	0.58460	0.67332	0.27369	12
0.94094	113.8	68.1	45.7	50	0.68122	0.45727	0.52846	0.19682	13
0.59845	123.1	68.1	55.0	50	0.68122	0.54977	0.52846	0.29103	14
0.99005	118.5	72.8	45.7	50	0.72773	0.45727	0.67332	0.19682	15
0.86324	127.8	72.8	55.0	50	0.72773	0.54977	0.67332	0.29103	16

Assurance for Tests for the Difference of Two Hazard Rates Assuming an Exponential Model

Numeric Results

Solve For: Power

Groups: 1 = Control, 2 = Treatment H0: $h2 - h1 \ge 0$ vs. Ha: h2 - h1 < 0

Hypotheses: Accrual: Uniform

	٠	ample S	izo	Lazar	d Rate	Hazard Rate	Hazard		oss d Rate	7	Гime		
Dawar		N1				Difference	Ratio			Accrual	Follow-Up	Almha	Report
Power	N	NT	N2	h1	h2	D	HK	ω1	ω2	R	T - R	Alpha	Row
0.94769	200	100	100	0.6	0.3	-0.3	0.50000	0.10	0.10	1	2	0.025	1
0.61307	200	100	100	0.6	0.4	-0.2	0.66667	0.10	0.10	1	2	0.025	2
0.99184	200	100	100	0.7	0.3	-0.4	0.42857	0.10	0.10	1	2	0.025	3
0.87447	200	100	100	0.7	0.4	-0.3	0.57143	0.10	0.10	1	2	0.025	4
0.94432	200	100	100	0.6	0.3	-0.3	0.50000	0.10	0.16	1	2	0.025	5
0.60389	200	100	100	0.6	0.4	-0.2	0.66667	0.10	0.16	1	2	0.025	6
0.99112	200	100	100	0.7	0.3	-0.4	0.42857	0.10	0.16	1	2	0.025	7
0.86856	200	100	100	0.7	0.4	-0.3	0.57143	0.10	0.16	1	2	0.025	8
0.93985	200	100	100	0.6	0.3	-0.3	0.50000	0.16	0.10	1	2	0.025	9
0.59820	200	100	100	0.6	0.4	-0.2	0.66667	0.16	0.10	1	2	0.025	10
0.98974	200	100	100	0.7	0.3	-0.4	0.42857	0.16	0.10	1	2	0.025	11
0.86278	200	100	100	0.7	0.4	-0.3	0.57143	0.16	0.10	1	2	0.025	12
0.93631	200	100	100	0.6	0.3	-0.3	0.50000	0.16	0.16	1	2	0.025	13
0.58940	200	100	100	0.6	0.4	-0.2	0.66667	0.16	0.16	1	2	0.025	14
0.98891	200	100	100	0.7	0.3	-0.4	0.42857	0.16	0.16	1	2	0.025	15
0.85684	200	100	100	0.7	0.4	-0.3	0.57143	0.16	0.16	1	2	0.025	16

	١	Number o Events	f	Percent		ent ability	Vari	ance	Danast
Power	E	E1	E2	Group 1 %N1	Pr(E1)	Pr(E2)	σ²(h1)	σ²(h2)	Report Row
0.94769	117.7	70.5	47.2	50	0.70513	0.47225	0.51054	0.19058	1
0.61307	127.4	70.5	56.8	50	0.70513	0.56840	0.51054	0.28149	2
0.99184	122.6	75.3	47.2	50	0.75340	0.47225	0.65039	0.19058	3
0.87447	132.2	75.3	56.8	50	0.75340	0.56840	0.65039	0.28149	4
0.94432	114.9	70.5	44.4	50	0.70513	0.44385	0.51054	0.20277	5
0.60389	124.1	70.5	53.6	50	0.70513	0.53583	0.51054	0.29860	6
0.99112	119.7	75.3	44.4	50	0.75340	0.44385	0.65039	0.20277	7
0.86856	128.9	75.3	53.6	50	0.75340	0.53583	0.65039	0.29860	8
0.93985	114.1	66.9	47.2	50	0.66853	0.47225	0.53849	0.19058	9
0.59820	123.7	66.9	56.8	50	0.66853	0.56840	0.53849	0.28149	10
0.98974	118.8	71.6	47.2	50	0.71619	0.47225	0.68417	0.19058	11
0.86278	128.5	71.6	56.8	50	0.71619	0.56840	0.68417	0.28149	12
0.93631	111.2	66.9	44.4	50	0.66853	0.44385	0.53849	0.20277	13
0.58940	120.4	66.9	53.6	50	0.66853	0.53583	0.53849	0.29860	14
0.98891	116.0	71.6	44.4	50	0.71619	0.44385	0.68417	0.20277	15
0.85684	125.2	71.6	53.6	50	0.71619	0.53583	0.68417	0.29860	16

The assurance calculation is made by summing the quantities

$$\left[\left(power_{i,j,k,l,m}\right)p(\lambda 1_i)p(\lambda 2_j)p(\omega 1_k)p(\omega 2_l)p(A_m)\right]$$

as follows

$$Assurance = (0.95213 \times 0.4 \times 0.4 \times 0.5 \times 0.5 \times 0.5) + (0.62311 \times 0.4 \times 0.6 \times 0.5 \times 0.5 \times 0.5) + \cdots + (0.85684 \times 0.6 \times 0.6 \times 0.5 \times 0.5 \times 0.5)$$

$$= 0.84714.$$

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 2** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Solve For	Assurance
Prior Entry Method	Individual (Enter a prior distribution for each applicable parameter)
Alternative Hypothesis	Η1: λ2 - λ1 < 0
Alpha	0.025
Group Allocation	Equal (N1 = N2)
Sample Size Per Group	100
Prior Distribution of ω1	Custom (Values and Probabilities in Spreadsheet)
Column of Values	
Column of Pr(Values)	C6
Prior Distribution of ω2	Custom (Values and Probabilities in Spreadsheet)
Column of Values	С7
Column of Pr(Values)	C8
Accrual Time (R)	1
Follow-Up Time (T - R)	2
Prior Distribution of A	Custom (Values and Probabilities in Spreadsheet)
Column of Values	C9
Column of Pr(Values)	C10
Prior Distribution of λ1	Custom (Values and Probabilities in Spreadsheet)
Column of Values	C1
Column of Pr(Values)	C2
Prior Distribution of λ2	Custom (Values and Probabilities in Spreadsheet)
Column of Values	C3
Column of Pr(Values)	C4
Options Tab	
Number of Computation Points fo	r each 50
Prior Distribution	
Maximum N1 in Sample Size Sea	rch 5000

Input Spreadsheet Data

Row	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10
1	0.6	0.4	0.3	0.4	0.10	0.5	0.10	0.5	50	0.5
2	0.7	0.6	0.4	0.6	0.16	0.5	0.16	0.5	30	0.5

Assurance for Tests for the Difference of Two Hazard Rates Assuming an Exponential Model

Output

Click the Calculate button to perform the calculations and generate the following output.

Solve For: Assurance Groups: $1 = \text{Control}, 2 = \text{Treatment}$ Hypotheses: $H0: \lambda 2 - \lambda 1 \ge 0 \text{ vs. } H1: \lambda 2 - \lambda 1 < 0$ Test Statistic: Hazard Rate Difference, $\lambda 2 - \lambda 1$ Elapsed Times: Accrual = 1, Follow-Up = 2, Total = 3 Prior Type: Independent Univariate Distributions													
C1: 0.6 (C2: 0.4 (A2: Poin C3: 0.3 (C4: 0.4 (W1: Poin C5: 0.1 (C6: 0.5 (C6	t List (Value).7).6 t List (Value).4).6 t List (Value).16).5 t List (Value).16	es = C: es = C: es = C:	3, Prob 5, Prob 7, Prob	os = C4) os = C6) os = C8)	i. i.								
C8: 0.5 (A: Poin C9: 50 3 C10: 0.5 (es = C:	,										
A: Poin C9: 50 3	0 `		Requir lumbe Event	r of	Sa	imple S	Size	Expected Hazard Rate Group 1	Expected Hazard Rate Group 2	Expected Loss Hazard Rate Group 1	Expected Loss Hazard Rate Group 2	Expected Percent Accrual Time until 50% Accrued	

PASS has also calculated the assurance as 0.84714 which validates the procedure.

Example 3 – Finding the Sample Size Needed to Achieve a Specified Assurance

Continuing with Example 1, the researchers want to investigate the sample sizes necessary to achieve assurances of 0.4, 0.6, and 0.8.

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 3** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Solve For	Sample Size
Prior Entry Method	Individual (Enter a prior distribution for each applicable parameter)
Alternative Hypothesis	Η1: λ2 - λ1 < 0
Assurance	0.4 0.6 0.8
Alpha	0.025
Group Allocation	Equal (N1 = N2)
Prior Distribution of ω1	Normal (Mean, SD)
Mean	0.165
SD	0.01
Truncation Boundaries	None
Prior Distribution of ω2	Normal (Mean, SD)
Mean	0.165
SD	0.01
Truncation Boundaries	None
Accrual Time (R)	1
Follow-Up Time (T - R)	2
Prior Distribution of A	Normal (Mean, SD)
Mean	50
SD	3
Truncation Boundaries	None
Prior Distribution of λ1	Normal (Mean, SD)
Mean	0.693
SD	0.05
Truncation Boundaries	None
Prior Distribution of λ2	Normal (Mean, SD)
Mean	0.288
SD	0.05
Truncation Boundaries	None
Ontions Tab	
Options Tab	

Assurance for Tests for the Difference of Two Hazard Rates Assuming an Exponential Model

Output

Click the Calculate button to perform the calculations and generate the following output.

Numeric Reports

Numeric Results

Solve For: Sample Size

 $\begin{array}{lll} \mbox{Groups:} & 1 = \mbox{Control}, \ 2 = \mbox{Treatment} \\ \mbox{Hypotheses:} & \mbox{Ho:} \ \lambda 2 - \lambda 1 \geq 0 \ \mbox{vs.} \ \mbox{H1:} \ \lambda 2 - \lambda 1 < 0 \\ \mbox{Test Statistic:} & \mbox{Hazard Rate Difference,} \ \lambda 2 - \lambda 1 \\ \mbox{Elapsed Times:} & \mbox{Hocycle House} \ \ \mbox{Accrual} = 1, \mbox{Follow-Up} = 2, \mbox{Total} = 3 \\ \mbox{Independent Univariate Distributions} \\ \mbox{Homes Total} \ \ \mbox{Homes} \mbox{Homes} \ \mbox{Homes} \mbox{Homes} \mbox{Homes} \ \mbox{Homes} \ \mbox{Homes} \ \mbo$

Prior Distributions

λ1: Normal (Mean = 0.693, SD = 0.05).
 λ2: Normal (Mean = 0.288, SD = 0.05).
 ω1: Normal (Mean = 0.165, SD = 0.01).
 ω2: Normal (Mean = 0.165, SD = 0.01).
 A: Normal (Mean = 50, SD = 3).

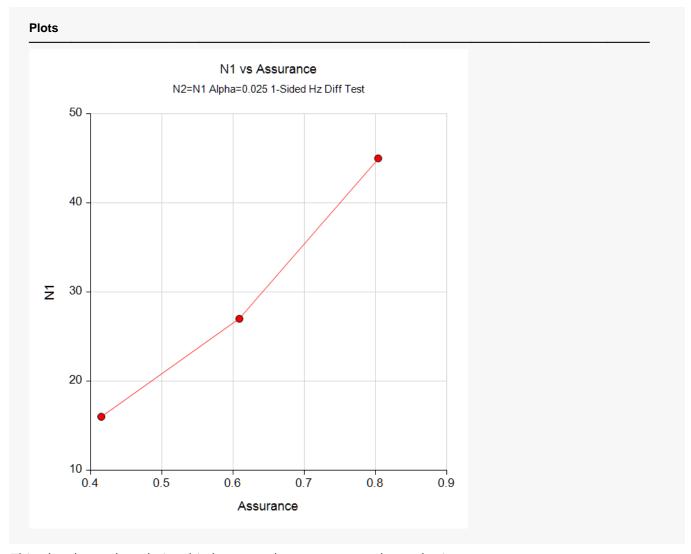
		N	equire umber Events	of	Sa	mple \$	Size	Expected Hazard Rate Group 1	Expected Hazard Rate Group 2	Expected Loss Hazard Rate Group 1	Expected Loss Hazard Rate Group 2	Percent Accrual Time until 50% Accrued	
Assurance*	Power‡	E1	E2	Е	N1	N2	N	E(λ1)	E(λ2)	E(ω1)	E(ω2)	E(A)	Alpha
0.41488	0.41185	11	7	18	16	16	32	0.693	0.288	0.165	0.165	50	0.025
0.60875	0.61665	19	12	31	27	27	54	0.693	0.288	0.165	0.165	50	0.025
0.80357	0.82980	32	19	51	45	45	90	0.693	0.288	0.165	0.165	50	0.025

^{*} The number of points used for computation of the prior(s) was 10.

This report shows the sample size required for each requested assurance value.

[‡] Power was calculated using $\lambda 1 = E(\lambda 1) = 0.693$, $\lambda 2 = E(\lambda 2) = 0.288$, $\omega 1 = E(\omega 1) = 0.165$, $\omega 2 = E(\omega 2) = 0.165$, and A = E(A) = 50.

Plots Section



This plot shows the relationship between the assurance and sample size.

Example 4 - Joint Prior Distribution

The following example shows the complexity required to specify a joint distribution for five parameters.

Suppose a one-sided test will be used in which $N1 = N2 = (100\ 200\ 300\ 400)$ and the significance level is 0.025. Further suppose that the joint prior distribution of the parameters is approximated by the following table. In a real study, the values in this table would be provided by an elicitation study.

Note that the program will rescale the probabilities so they sum to one.

<u>λ1</u>	<u>λ2</u>	<u>ω1</u>	<u>ω2</u>	<u>A</u>	<u>Prob</u>
0.6	0.3	0.05	0.05	30	0.07
0.6	0.3	0.1	0.1	30	0.09
0.6	0.3	0.15	0.15	30	0.11
0.65	0.3	0.05	0.05	30	0.07
0.65	0.3	0.1	0.1	30	0.09
0.65	0.3	0.15	0.15	30	0.11
0.7	0.3	0.05	0.05	30	0.07
0.7	0.3	0.1	0.1	30	0.09
0.7	0.3	0.15	0.15	30	0.11
0.6	0.4	0.05	0.05	30	0.27
0.6	0.4	0.1	0.1	30	0.29
0.6	0.4	0.15	0.15	30	0.31
0.65	0.4	0.05	0.05	30	0.27
0.65	0.4	0.1	0.1	30	0.29
0.65	0.4	0.15	0.15	30	0.31
0.7	0.4	0.05	0.05	30	0.27
0.7	0.4	0.1	0.1	30	0.29
0.7	0.4	0.15	0.15	30	0.31
0.6	0.5	0.05	0.05	30	0.17
0.6	0.5	0.1	0.1	30	0.19
0.6	0.5	0.15	0.15	30	0.21
0.65	0.5	0.05	0.05	30	0.17
0.65	0.5	0.1	0.1	30	0.19
0.65	0.5	0.15	0.15	30	0.21
0.7	0.5	0.05	0.05	30	0.17
0.7	0.5	0.1	0.1	30	0.19
0.7	0.5	0.15	0.15	30	0.21
0.6	0.3	0.05	0.05	50	0.12
0.6	0.3	0.1	0.1	50	0.14
0.6	0.3	0.15	0.15	50	0.16
0.65	0.3	0.05	0.05	50	0.12
0.65	0.3	0.1	0.1	50	0.14
0.65	0.3	0.15	0.15	50	0.16
0.7	0.3	0.05	0.05	50	0.12
0.7	0.3	0.1	0.1	50	0.14
0.7	0.3	0.15	0.15	50	0.16
0.6	0.4	0.05	0.05	50	0.32

0.6	0.4	0.1	0.1	50	0.34
0.6	0.4	0.15	0.15	50	0.36
0.65	0.4	0.05	0.05	50	0.32
0.65	0.4	0.1	0.1	50	0.34
0.65	0.4	0.15	0.15	50	0.36
0.7	0.4	0.05	0.05	50	0.32
0.7	0.4	0.1	0.1	50	0.34
0.7	0.4	0.15	0.15	50	0.36
0.6	0.5	0.05	0.05	50	0.22
0.6	0.5	0.1	0.1	50	0.24
0.6	0.5	0.15	0.15	50	0.26
0.65	0.5	0.05	0.05	50	0.22
0.65	0.5	0.1	0.1	50	0.24
0.65	0.5	0.15	0.15	50	0.26
0.7	0.5	0.05	0.05	50	0.22
0.7	0.5	0.1	0.1	50	0.24
0.7	0.5	0.15	0.15	50	0.26
0.6	0.3	0.05	0.05	70	0.07
0.6	0.3	0.1	0.1	70	0.09
0.6	0.3	0.15	0.15	70	0.11
0.65	0.3	0.05	0.05	70	0.07
0.65	0.3	0.1	0.1	70	0.09
0.65	0.3	0.15	0.15	70	0.11
0.7	0.3	0.05	0.05	70	0.07
0.7	0.3	0.1	0.1	70	0.09
0.7	0.3	0.15	0.15	70	0.11
0.6	0.4	0.05	0.05	70	0.27
0.6	0.4	0.1	0.1	70	0.29
0.6	0.4	0.15	0.15	70	0.31
0.65	0.4	0.05	0.05	70	0.27
0.65	0.4	0.1	0.1	70	0.29
0.65	0.4	0.15	0.15	70	0.31
0.7	0.4	0.05	0.05	70	0.27
0.7	0.4	0.1	0.1	70	0.29
0.7	0.4	0.15	0.15	70	0.31
0.6	0.5	0.05	0.05	70	0.17
0.6	0.5	0.1	0.1	70	0.19
0.6	0.5	0.15	0.15	70	0.21
0.65	0.5	0.05	0.05	70	0.17
0.65	0.5	0.1	0.1	70	0.19
0.65	0.5	0.15	0.15	70	0.21
0.7	0.5	0.05	0.05	70	0.17
0.7	0.5	0.1	0.1	70	0.19
0.7	0.5	0.15	0.15	70	0.21

To run this example, the above data will need to be loaded into columns C1 to C6.

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 4** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Solve For	Assurance
Prior Entry Method	Combined (Enter parameter values and probabilities on spreadsheet)
Alternative Hypothesis	Η1: λ2 - λ1 < 0
Alpha	0.025
Group Allocation	Equal (N1 = N2)
Sample Size Per Group	100 200 300 400
Column of ω1 Values	C3
Column of ω2 Values	C4
Accrual Time (R)	1
Follow-Up Time (T - R)	2
Column of A Values	C5
Column of λ1 Values	C1
Column of λ2 Values	C2
Column of Pr(Values)	C6
Options Tab	
Number of Computation Points for	each10
Prior Distribution	
Maximum N1 in Sample Size Sear	rch 5000

Input Spreadsheet Data

Row	C1	C2	C3	C4	C5	C6
1	0.60	0.3	0.05	0.05	30	0.07
2	0.60	0.3	0.10	0.10	30	0.09
3	0.60	0.3	0.15	0.15	30	0.11
4	0.65	0.3	0.05	0.05	30	0.07
5	0.65	0.3	0.10	0.10	30	0.09
6	0.65	0.3	0.15	0.15	30	0.11
7	0.70	0.3	0.05	0.05	30	0.07
8	0.70	0.3	0.10	0.10	30	0.09
9	0.70	0.3	0.15	0.15	30	0.11
10	0.60	0.4	0.05	0.05	30	0.27
11	0.60	0.4	0.10	0.10	30	0.29
12	0.60	0.4	0.15	0.15	30	0.31
13	0.65	0.4	0.05	0.05	30	0.27
14	0.65	0.4	0.10	0.10	30	0.29
15	0.65	0.4	0.15	0.15	30	0.31
16	0.70	0.4	0.05	0.05	30	0.27
17	0.70	0.4	0.10	0.10	30	0.29
18	0.70	0.4	0.15	0.15	30	0.31
19	0.60	0.5	0.05	0.05	30	0.17
20	0.60	0.5	0.10	0.10	30	0.19
21	0.60	0.5	0.15	0.15	30	0.21
22	0.65	0.5	0.05	0.05	30	0.17

22	0.65	0.5	0.10	0.40	20	0.40	
23	0.65	0.5	0.10	0.10	30	0.19	
24 25	0.65	0.5	0.15	0.15	30 30	0.21 0.17	
25 26	0.70 0.70	0.5	0.05 0.10	0.05 0.10	30 30	0.17	
26 27	0.70	0.5 0.5	0.10	0.10	30	0.19	
28	0.60	0.3	0.05	0.05	50 50	0.12	
29	0.60	0.3	0.10	0.10	50	0.14	
30	0.60	0.3	0.15	0.15	50	0.16	
31	0.65	0.3	0.05	0.05	50	0.12	
32	0.65	0.3	0.10	0.10	50	0.14	
33	0.65	0.3	0.15	0.15	50 50	0.16	
34	0.70	0.3	0.05	0.05	50	0.12	
35	0.70	0.3	0.10	0.10	50	0.14	
36	0.70	0.3	0.15	0.15	50 50	0.16 0.32	
37	0.60	0.4	0.05	0.05	50 50		
38	0.60	0.4	0.10 0.15	0.10 0.15	50 50	0.34	
39	0.60	0.4			50	0.36	
40 41	0.65	0.4	0.05 0.10	0.05	50 50	0.32	
41 42	0.65 0.65	0.4 0.4	0.10	0.10 0.15	50 50	0.34 0.36	
43 44	0.70 0.70	0.4 0.4	0.05 0.10	0.05 0.10	50 50	0.32 0.34	
			0.10	0.10			
45 46	0.70 0.60	0.4 0.5	0.15	0.15	50 50	0.36 0.22	
46 47	0.60	0.5	0.05	0.05	50 50	0.22	
47 48	0.60	0.5	0.10	0.10	50 50	0.24	
46 49	0.65	0.5	0.15	0.15	50 50	0.26	
50	0.65	0.5	0.03	0.03	50	0.22	
51	0.65	0.5	0.10	0.10	50	0.24	
52	0.03	0.5	0.15	0.15	50	0.20	
53	0.70	0.5	0.03	0.03	50	0.22	
54	0.70	0.5	0.10	0.10	50	0.24	
55	0.60	0.3	0.15	0.05	70	0.07	
56	0.60	0.3	0.10	0.10	70	0.09	
57	0.60	0.3	0.15	0.15	70	0.11	
58	0.65	0.3	0.05	0.05	70	0.07	
59	0.65	0.3	0.10	0.10	70	0.09	
60	0.65	0.3	0.15	0.15	70	0.11	
61	0.70	0.3	0.05	0.05	70	0.07	
62	0.70	0.3	0.10	0.10	70	0.09	
63	0.70	0.3	0.15	0.15	70	0.11	
64	0.60	0.4	0.05	0.05	70	0.27	
65	0.60	0.4	0.10	0.10	70	0.29	
66	0.60	0.4	0.15	0.15	70	0.31	
67	0.65	0.4	0.05	0.05	70	0.27	
68	0.65	0.4	0.10	0.10	70	0.29	
69	0.65	0.4	0.15	0.15	70	0.31	
70	0.70	0.4	0.05	0.05	70	0.27	
71	0.70	0.4	0.10	0.10	70	0.29	
72	0.70	0.4	0.15	0.15	70	0.31	
73	0.60	0.5	0.05	0.05	70	0.17	
74	0.60	0.5	0.10	0.10	70	0.19	
75	0.60	0.5	0.15	0.15	70	0.21	
76	0.65	0.5	0.05	0.05	70	0.17	
77	0.65	0.5	0.10	0.10	70	0.19	
78	0.65	0.5	0.15	0.15	70	0.21	
79	0.70	0.5	0.05	0.05	70	0.17	
80	0.70	0.5	0.10	0.10	70	0.19	
81	0.70	0.5	0.15	0.15	70	0.21	

Assurance for Tests for the Difference of Two Hazard Rates Assuming an Exponential Model

Output

Click the Calculate button to perform the calculations and generate the following output.

Numeric Reports

Numeric Results Solve For: Assurance Groups: 1 = Control, 2 = Treatment Hypotheses: H0: $\lambda 2 - \lambda 1 \ge 0$ vs. H1: $\lambda 2 - \lambda 1 < 0$ Test Statistic: Hazard Rate Difference, λ2 - λ1 Elapsed Times: Accrual = 1, Follow-Up = 2, Total = 3 Prior Type: Joint Multivariate Distribution **Prior Distribution** Point Lists $\textbf{C1:} \quad 0.6 \,\, 0.6 \,\, 0.65 \,\, 0.65 \,\, 0.65 \,\, 0.65 \,\, 0.7 \,\, 0.7 \,\, 0.7 \,\, 0.7 \,\, 0.6 \,\, 0.6 \,\, 0.65 \,\, 0.65 \,\, 0.65 \,\, 0.65 \,\, 0.7 \,\, 0.7 \,\, 0.7 \,\, 0.6 \,\, 0.6 \,\, 0.65 \,\, 0.65 \,\, 0.65 \,\, 0.65 \,\, 0.65 \,\, 0.7 \,\, 0.7 \,\, 0.7 \,\, 0.6 \,\, 0.6 \,\, 0.65$ $0.65\ 0.65\ 0.7\ 0.7\ 0.7\ 0.6\ 0.6\ 0.65\ 0.6$ $0.7\ 0.7\ 0.6\ 0.6\ 0.65\ 0.65\ 0.65\ 0.65\ 0.7\ 0.7\ 0.7\ 0.6\ 0.6\ 0.6\ 0.65\ 0.65\ 0.65\ 0.7\ 0.7\ 0.7$ λ2. $C2: \quad 0.3 \ 0.3 \ 0.3 \ 0.3 \ 0.3 \ 0.3 \ 0.3 \ 0.3 \ 0.3 \ 0.3 \ 0.3 \ 0.3 \ 0.4 \ 0.4 \ 0.4 \ 0.4 \ 0.4 \ 0.4 \ 0.4 \ 0.5 \ 0.5 \ 0.5 \ 0.5 \ 0.5 \ 0.5 \ 0.5 \ 0.5 \ 0.5 \ 0.5 \ 0.3$ $\textbf{C3:} \quad 0.05 \ 0.1 \ 0.15 \ 0.05 \ 0.10 \ 0.15 \ 0.05 \ 0.10 \ 0.15 \ 0.05 \ 0.10 \ 0.15 \ 0.05 \ 0.10 \ 0.15 \ 0.1$ ω1· $0.1\ 0.15\ 0.05\ 0.1\ 0.15\ 0.05\ 0.1\ 0.15\ 0.05\ 0.1\ 0.15\ 0.05\ 0.1\ 0.15\ 0.05\ 0.1$ $0.15\ 0.05\ 0.1\ 0.15\ 0.05\ 0.1\ 0.15\ 0.05\ 0.1\ 0.15\ 0.05\ 0.1\ 0.15\ 0.05\ 0.1\ 0.15\ 0.05\ 0.1$ $C4: \quad 0.05 \ 0.1 \ 0.15 \ 0.15 \ 0.15$ ω2: $0.1\ 0.15\ 0.05\ 0.1\ 0.15\ 0.05\ 0.1\ 0.15\ 0.05\ 0.1\ 0.15\ 0.05\ 0.1$ $0.15\; 0.05\; 0.1\; 0.15\; 0.05\; 0.10\; 0.15\; 0.05\; 0.10\; 0.15\; 0.05\; 0.10\; 0.15\; 0.05\; 0.10\; 0.15\; 0.05\; 0.10\; 0.15\; 0.05\; 0.10\; 0.15\; 0.05\; 0.10\; 0.15\; 0.05\; 0.10\; 0.15\; 0.05\; 0.10\; 0.15\; 0.05\; 0.10\; 0.15\; 0.05\; 0.10\; 0.15\; 0.05\; 0.10\; 0.15\; 0.$ $C5: \hspace{0.2cm} 30 \hspace{0.3cm} 50 \hspace{0.3cm} 50$ Prob: C6: 0.07 0.09 0.11 0.07 0.09 0.11 0.07 0.09 0.11 0.07 0.09 0.11 0.27 0.29 0.31 0.27 0.29 0.31 0.27 0.29 0.31 0.17 0.19 0.21 0.17 0.19 0.21 0.17 0.19 $0.21\ 0.12\ 0.14\ 0.16\ 0.12\ 0.14\ 0.16\ 0.12\ 0.14\ 0.16\ 0.32\ 0.34\ 0.36\ 0.32\ 0.34\ 0.36\ 0.32\ 0.34\ 0.36\ 0.22\ 0.24\ 0.26\ 0.22\ 0.24$ $0.22\ 0.24\ 0.26\ 0.07\ 0.09\ 0.11\ 0.07\ 0.09\ 0.11\ 0.07\ 0.09\ 0.11\ 0.27\ 0.29\ 0.31\ 0.27\ 0.29\ 0.31\ 0.27\ 0.29\ 0.31\ 0.27\ 0.29\ 0.31$ 0.19 0.21 0.17 0.19 0.21

		N	Require umber Events	of	Sa	mple S	Size	Expected Hazard Rate Group 1	Expected Hazard Rate Group 2	Expected Loss Hazard Rate Group 1	Expected Loss Hazard Rate Group 2	Expected Percent of Accrual Time until 50% are Accrued	
Assurance	Power‡	E1	E2	E	N1	N2	N	Ε(λ1)	Ε(λ2)	Ε(ω1)	Ε(ω2)	E(A)	Alpha
0.65150	0.70370	73	58	131	100	100	200	0.65	0.41613	0.10323	0.10323	50	0.025
0.82896	0.94162	146	116	262	200	200	400	0.65	0.41613	0.10323	0.10323	50	0.025
0.89728	0.99090	219	174	393	300	300	600	0.65	0.41613	0.10323	0.10323	50	0.025
0.93170	0.99878	291	232	523	400	400	800	0.65	0.41613	0.10323	0.10323	50	0.025

[‡] Power was calculated using $\lambda 1 = E(\lambda 1) = 0.65$, $\lambda 2 = E(\lambda 2) = 0.41613$, $\omega 1 = E(\omega 1) = 0.10323$, $\omega 2 = E(\omega 2) = 0.10323$, and A = E(A) = 50.

This report shows the assurance values obtained by each sample size.

Example 5 – Joint Prior Validation

The problem given in Example 2 will be used to validate the joint prior distribution method. This will be done by running the independent-prior scenario used in that example through the joint-prior method and checking that the assurance values match.

In Example 2, the prior distributions of the parameters are

<u>λ1</u>	<u>P(λ1)</u>	<u>λ2</u>	<u>P(λ2)</u>	<u>ω1</u>	<u>P(ω1)</u>	<u>ω2</u>	<u>P(ω2)</u>	<u>A</u>	<u>P(A)</u>
0.6	0.4	0.3	0.4	0.1	0.5	0.1	0.5	30	0.5
0.7	0.6	0.4	0.6	0.16	0.5	0.16	0.5	50	0.5

The joint prior distribution can be found by multiplying the five independent probabilities in each row. This results in the following discrete joint probability distribution.

		_		-	
<u>λ1</u>	<u>λ2</u>	<u>ω1</u>	<u>ω2</u>	<u>A</u>	<u>Prob</u>
0.6	0.3	0.1	0.1	30	0.02
0.6	0.4	0.1	0.1	30	0.03
0.7	0.3	0.1	0.1	30	0.03
0.7	0.4	0.1	0.1	30	0.045
0.6	0.3	0.1	0.16	30	0.02
0.6	0.4	0.1	0.16	30	0.03
0.7	0.3	0.1	0.16	30	0.03
0.7	0.4	0.1	0.16	30	0.045
0.6	0.3	0.16	0.1	30	0.02
0.6	0.4	0.16	0.1	30	0.03
0.7	0.3	0.16	0.1	30	0.03
0.7	0.4	0.16	0.1	30	0.045
0.6	0.3	0.16	0.16	30	0.02
0.6	0.4	0.16	0.16	30	0.03
0.7	0.3	0.16	0.16	30	0.03
0.7	0.4	0.16	0.16	30	0.045
0.6	0.3	0.1	0.1	50	0.02
0.6	0.4	0.1	0.1	50	0.03
0.7	0.3	0.1	0.1	50	0.03
0.7	0.4	0.1	0.1	50	0.045
0.6	0.3	0.1	0.16	50	0.02
0.6	0.4	0.1	0.16	50	0.03
0.7	0.3	0.1	0.16	50	0.03
0.7	0.4	0.1	0.16	50	0.045
0.6	0.3	0.16	0.1	50	0.02
0.6	0.4	0.16	0.1	50	0.03
0.7	0.3	0.16	0.1	50	0.03
0.7	0.4	0.16	0.1	50	0.045
0.6	0.3	0.16	0.16	50	0.02
0.6	0.4	0.16	0.16	50	0.03
0.7	0.3	0.16	0.16	50	0.03
0.7	0.4	0.16	0.16	50	0.045

To run this example, the spreadsheet is loaded with the following six columns.

<u>C1</u>	<u>C2</u>	<u>C3</u>	<u>C4</u>	<u>C5</u>	<u>C6</u>
0.6	0.3	0.1	0.1	30	0.02
0.6	0.4	0.1	0.1	30	0.03
0.7	0.3	0.1	0.1	30	0.03
0.7	0.4	0.1	0.1	30	0.045
0.6	0.3	0.1	0.16	30	0.02
0.6	0.4	0.1	0.16	30	0.03
0.7	0.3	0.1	0.16	30	0.03
0.7	0.4	0.1	0.16	30	0.045
0.6	0.3	0.16	0.1	30	0.02
0.6	0.4	0.16	0.1	30	0.03
0.7	0.3	0.16	0.1	30	0.03
0.7	0.4	0.16	0.1	30	0.045
0.6	0.3	0.16	0.16	30	0.02
0.6	0.4	0.16	0.16	30	0.03
0.7	0.3	0.16	0.16	30	0.03
0.7	0.4	0.16	0.16	30	0.045
0.6	0.3	0.1	0.1	50	0.02
0.6	0.4	0.1	0.1	50	0.03
0.7	0.3	0.1	0.1	50	0.03
0.7	0.4	0.1	0.1	50	0.045
0.6	0.3	0.1	0.16	50	0.02
0.6	0.4	0.1	0.16	50	0.03
0.7	0.3	0.1	0.16	50	0.03
0.7	0.4	0.1	0.16	50	0.045
0.6	0.3	0.16	0.1	50	0.02
0.6	0.4	0.16	0.1	50	0.03
0.7	0.3	0.16	0.1	50	0.03
0.7	0.4	0.16	0.1	50	0.045
0.6	0.3	0.16	0.16	50	0.02
0.6	0.4	0.16	0.16	50	0.03
0.7	0.3	0.16	0.16	50	0.03
0.7	0.4	0.16	0.16	50	0.045

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 5** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

olve For	Assurance
rior Entry Method	
Iternative Hypothesis	Η1: λ2 - λ1 < 0
lpha	0.025
roup Allocation	Equal (N1 = N2)
ample Size Per Group	100
olumn of ω1 Values	C3
olumn of ω2 Values	C4
ccrual Time (R)	1
ollow-Up Time (T - R)	2
olumn of A Values	C5
olumn of λ1 Values	C1
olumn of λ2 Values	C2
olumn of Pr(Values)	C6
ptions Tab	

Input Spreadsheet Data

Row	C1	C2	C3	C4	C5	C6
1	0.6	0.3	0.10	0.10	30	0.020
2	0.6	0.4	0.10	0.10	30	0.030
3	0.7	0.3	0.10	0.10	30	0.030
4	0.7	0.4	0.10	0.10	30	0.045
5	0.6	0.3	0.10	0.16	30	0.020
6	0.6	0.4	0.10	0.16	30	0.030
7	0.7	0.3	0.10	0.16	30	0.030
8	0.7	0.4	0.10	0.16	30	0.045
9	0.6	0.3	0.16	0.10	30	0.020
10	0.6	0.4	0.16	0.10	30	0.030
11	0.7	0.3	0.16	0.10	30	0.030
12	0.7	0.4	0.16	0.10	30	0.045
13	0.6	0.3	0.16	0.16	30	0.020
14	0.6	0.4	0.16	0.16	30	0.030
15	0.7	0.3	0.16	0.16	30	0.030
16	0.7	0.4	0.16	0.16	30	0.045
17	0.6	0.3	0.10	0.10	50	0.020
18	0.6	0.4	0.10	0.10	50	0.030
19	0.7	0.3	0.10	0.10	50	0.030
20	0.7	0.4	0.10	0.10	50	0.045

Maximum N1 in Sample Size Search5000

Assurance for Tests for the Difference of Two Hazard Rates Assuming an Exponential Model

21	0.6	0.3	0.10	0.16	50	0.020
22	0.6	0.4	0.10	0.16	50	0.030
23	0.7	0.3	0.10	0.16	50	0.030
24	0.7	0.4	0.10	0.16	50	0.045
25	0.6	0.3	0.16	0.10	50	0.020
26	0.6	0.4	0.16	0.10	50	0.030
27	0.7	0.3	0.16	0.10	50	0.030
28	0.7	0.4	0.16	0.10	50	0.045
29	0.6	0.3	0.16	0.16	50	0.020
30	0.6	0.4	0.16	0.16	50	0.030
31	0.7	0.3	0.16	0.16	50	0.030
32	0.7	0.4	0.16	0.16	50	0.045

Output

Click the Calculate button to perform the calculations and generate the following output.

Prior Distri	oution												
λ2: C2:	0.3 0.4 0.3	0.4 0.3 0.1 0.1	0.4 0	.3 0.4 (0.3 0.4	0.3 0.4	0.3 0.4	1 0.3 0.4 0.3	0.4 0.3 0.4 0.3	3 0.4 0.3 0.4 0	0.3 0.4 0.3 0.4	7 0.6 0.6 0.7 0.7 4 0.3 0.4 0.3 0.4 6 0.16 0.16 0.16 0	.16 0.16
A: C5:	0.16 0.16 30 30 30 3	30 30	30 30	30 30	30 30	30 30	30 30 5	0 50 50 50 5	0 50 50 50 50	50 50 50 50	50 50 50	3 0.1 0.1 0.1 0.1 0	
A: C5:	0.16 0.16 30 30 30 3	30 30 30 30 30 30 30 30	30 30 30 30	30 30 02 0.03	30 30 0.03 0	30 30 3 .045 0	30 30 5	0 50 50 50 5	0 50 50 50 50	50 50 50 50	50 50 50	6 0.1 0.1 0.1 0.1 0 45 0.02 0.03 0.03	
A: C5:	0.16 0.16 30 30 30 3 0.02 0.03 0	0 30 30 0 30 30 0 03 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	30 30 30 30	0 30 30 02 0.03 0.02 0.0	30 30 0.03 0 03 0.03	30 30 3 .045 0	30 30 5 02 0.03	0 50 50 50 50 3 0.03 0.045 (Expected Hazard Rate	0 50 50 50 50 0.02 0.03 0.03 Expected Hazard Rate	50 50 50 50 3 0.045 0.02 (Expected Loss Hazard Rate	50 50 50 0.03 0.03 0.04 Expected Loss Hazard Rate	Expected Percent of Accrual Time until 50%	
A: C5:	0.16 0.16 30 30 30 3 0.02 0.03 0	0 30 30 0 30 30 0 03 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	9 30 30 945 0.0 9.045 0 9.045 0 equire	0 30 30 02 0.03 0.02 0.0	30 30 0.03 0 03 0.03	30 30 3 .045 0 0.045	30 30 5 02 0.03	0 50 50 50 50 3 0.03 0.045 (Expected Hazard	0 50 50 50 50 0.02 0.03 0.03 Expected Hazard	50 50 50 50 3 0.045 0.02 (Expected Loss Hazard	50 50 50 0.03 0.03 0.04 Expected Loss Hazard	Expected Percent of Accrual Time	

PASS has also calculated the assurance as 0.84714 which matches Example 2 and thus validates the procedure.