PASS Sample Size Software NCSS.com

Chapter 476

Group-Sequential Tests for Two Means (Simulation) (Legacy)

This procedure uses simulation for the calculation of the boundaries as well as for calculation of power (and sample size). Futility boundaries are limited. A variety of test statistics and simulated distributions are available.

Introduction

This procedure can be used to determine power, sample size and/or boundaries for group sequential tests comparing the means of two groups. The common two-sample T-Test and the Mann-Whitney U test can be simulated in this procedure. For two-sided tests, significance (efficacy) boundaries can be generated. For one-sided tests, significance and futility boundaries can be produced. The spacing of the looks can be equal or custom specified. Boundaries can be computed based on popular alpha- and beta-spending functions (O'Brien-Fleming, Pocock, Hwang-Shih-DeCani Gamma family, linear) or custom spending functions. Boundaries can also be input directly to verify alpha- and/or beta-spending properties. Futility boundaries can be binding or non-binding. Maximum and average (expected) sample sizes are reported as well as the alpha and/or beta spent and incremental power at each look. Corresponding P-Value boundaries are also given for each boundary statistic. Plots of boundaries are also produced.

The distributions of each of the groups under the null and alternative hypotheses can be specified directly using over ten distributions including normal, exponential, Gamma, Uniform, Beta, and Cauchy.

Technical Details

This section outlines many of the technical details of the techniques used in this procedure including the simulation summary, the test statistic details, and the use of spending functions.

An excellent text for the background and details of many group-sequential methods is Jennison and Turnbull (2000).

Simulation Procedure

In this procedure, a large number of simulations are used to calculate boundaries and power using the following steps:

- 1. Based on the specified distributions, random samples of size N1 and N2 are generated under the null distribution and under the alternative distribution. These are simulated samples as though the final look is reached.
- 2. For each sample, test statistics for each look are produced. For example, if N1 and N2 are 100 and there are 5 equally spaced looks, test statistics are generated from the random samples at N1 = N2 = 20, N1 = N2 = 40, N1 = N2 = 60, N1 = N2 = 80, and N1 = N2 = 100 for both null and alternative samples.

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- 3. To generate the first significance boundary, the null distribution statistics of the first look (e.g., at N1 = N2 = 20) are ordered and the percent of alpha to be spent at the first look is determined (using either the alpha-spending function or the input value). The statistic for which the percent of statistics above (or below, as the case may be) that value is equal to the percent of alpha to be spent at the first look is the boundary statistic. It is seen here how important a large number of simulations is to the precision of the boundary estimates.
- 4. All null distribution samples that are outside the first significance boundary at the first look are removed from consideration for the second look. If binding futility boundaries are also being computed, all null distribution samples with statistics that are outside the first futility boundary are also removed from consideration for the second look. If non-binding futility boundaries are being computed, null distribution samples with statistics outside the first futility boundary are not removed.
- 5. To generate the second significance boundary, the remaining null distribution statistics of the second look (e.g., at N1 = N2 = 40) are ordered and the percent of alpha to be spent at the second look is determined (again, using either the alpha-spending function or the input value). The percent of alpha to be spent at the second look is multiplied by the total number of simulations to determine the number of the statistic that is to be the second boundary statistic. The statistic for which that number of statistics is above it (or below, as the case may be) is the second boundary statistic. For example, suppose there are initially 1000 simulated samples, with 10 removed at the first look (from, say, alpha spent at Look 1 equal to 0.01), leaving 990 samples considered for the second look. Suppose further that the alpha to be spent at the second look is 0.02. This is multiplied by 1000 to give 20. The 990 still-considered statistics are ordered and the 970th (20 in from 990) statistic is the second boundary.
- 6. All null distribution samples that are outside the second significance boundary and the second futility boundary, if binding, at the second look are removed from consideration for the third look (e.g., leaving 970 statistics computed at N1 = N2 = 60 to be considered at the third look). Steps 4 and 5 are repeated until the final look is reached.

Futility boundaries are computed in a similar manner using the desired beta-spending function or custom beta-spending values and the alternative hypothesis simulated statistics at each look. For both binding and non-binding futility boundaries, samples for which alternative hypothesis statistics are outside either the significance or futility boundaries of the previous look are excluded from current and future looks.

Because the final futility and significance boundaries are required to be the same, futility boundaries are computed beginning at a small value of beta (e.g., 0.0001) and incrementing beta by that amount until the futility and significance boundaries meet.

When boundaries are entered directly, this procedure uses the null hypothesis and alternative hypothesis simulations to determine the number of test statistics that are outside the boundaries at each look. The cumulative proportion of alternative hypothesis statistics that are outside the significance boundaries is the overall power of the study.

Generating Random Distributions

Two methods are available in **PASS** to simulate random samples. The first method generates the random variates directly, one value at a time. The second method generates a large pool (over 10,000) of random values and then draws the random numbers from this pool. This second method can cut the running time of the simulation by 70%.

As mentioned above, the second method begins by generating a large pool of random numbers from the specified distributions. Each of these pools is evaluated to determine if its mean is within a small relative tolerance (0.0001) of the target mean. If the actual mean is not within the tolerance of the target mean, individual members of the population are replaced with new random numbers if the new random number moves the mean towards its target. Only a few hundred such swaps are required to bring the actual mean to within tolerance of the target mean. This population is then sampled with replacement using the uniform distribution. We have found that this method works well as long as the size of the pool is the maximum of twice the number of simulated samples desired and 10,000.

Test Statistics

This section describes the test statistics that are available in this procedure.

Two-Sample T-Test

The two-sample t-test assumes that the data are simple random samples from Normal populations with the same variance. This assumption implies that the data are continuous, and their distribution is symmetric. The calculation of the t statistic is as follows

$$t_{df} = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{s_{\bar{X}_1 - \bar{X}_2}}$$

where

$$\bar{X}_k = \frac{\sum_{i=1}^{N_k} X_{ki}}{N_k}$$

$$s_{\bar{X}_1 - \bar{X}_2} = \sqrt{\frac{\sum_{i=1}^{N_1} (X_{1i} - \bar{X}_1)^2 + \sum_{i=1}^{N_2} (X_{2i} - \bar{X}_2)^2}{N_1 + N_2 - 2}} \left(\frac{1}{N_1} + \frac{1}{N_2}\right)$$

$$df = N_1 + N_2 - 2$$

The significance of the test statistic is determined by computing the p-value based on the t distribution with degrees of freedom df. If this p-value is less than a specified level (often 0.05), the null hypothesis is rejected. Otherwise, no conclusion can be reached.

Mann-Whitney U Test

This test is the nonparametric substitute for the equal-variance t-test. Two key assumptions for this test are that the distributions are at least ordinal and that they are identical under H0. This implies that ties (repeated values) are not acceptable. When ties are present, the approximation provided can be used, but know that the theoretic results no longer hold.

The Mann-Whitney test statistic is defined as follows in Gibbons (1985).

$$z = \frac{W_1 - \frac{N_1(N_1 + N_2 + 1)}{2} + C}{s_W}$$

where

$$W_1 = \sum_{k=1}^{N_1} Rank(X_{1k})$$

The ranks are determined after combining the two samples. The standard deviation is calculated as

$$s_W = \sqrt{\frac{N_1 N_2 (N_1 + N_2 + 1)}{12} - \frac{N_1 N_2 \sum_{i=1} (t_i^3 - t_i)}{12 (N_1 + N_2) (N_1 + N_2 - 1)}}$$

where t_1 is the number of observations tied at value one, t_2 is the number of observations tied at some value two, and so forth.

The correction factor, C, is 0.5 if the rest of the numerator of Z is negative or -0.5 otherwise. The value of Z is then compared to the standard normal distribution.

Standard Deviations

Care must be used when either the null or alternative distribution is not normal. In these cases, the standard deviation is usually not specified directly. For example, you might use a gamma distribution with a shape parameter of 1.5 and a mean of 4 as the null distribution and a gamma distribution with the same shape parameter and a mean of 5 as the alternative distribution. This allows you to compare the two means. However, although the shape parameters are constant, the standard deviations, which are based on both the shape parameter and the mean, are not. Thus, the distributions not only have different means, but also different standard deviations.

Spending Functions

Spending functions can be used in this procedure to specify the proportion of alpha or beta that is spent at each look without having to specify the proportion directly.

Spending functions have the characteristics that they are increasing and that

$$\alpha(0) = 0$$

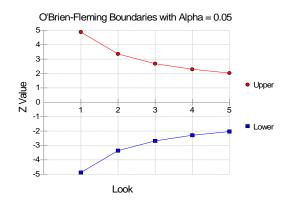
$$\alpha(1) = \alpha$$

The last characteristic guarantees a fixed α level when the trial is complete. This methodology is very flexible since neither the times nor the number of analyses must be specified in advance. Only the functional form of $\alpha(\tau)$ must be specified.

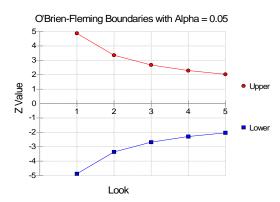
PASS provides several popular spending functions plus the ability to enter and analyze your own percents of alpha or beta spent. These are calculated as follows (beta may be substituted for alpha for beta-spending functions):

1. Hwang-Shih-DeCani (gamma family)

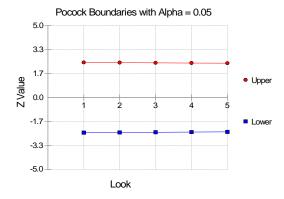
$$\alpha \left[\frac{1 - e^{-\gamma t}}{1 - e^{-\gamma}} \right], \gamma \neq 0; \quad \alpha t, \gamma = 0$$



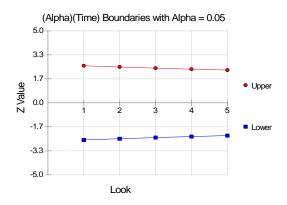
2. O'Brien-Fleming Analog $2-2\Phi\left(\frac{Z_{\alpha/2}}{\sqrt{t}}\right)$



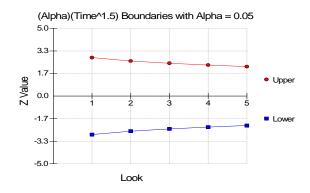
3. Pocock Analog $\alpha \cdot \ln(1 + (e-1)t)$



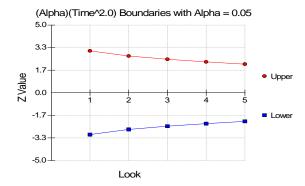
4. Alpha * time $\alpha \cdot t$



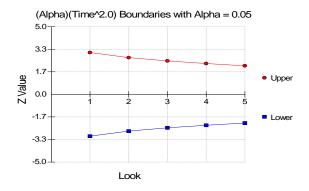
5. Alpha * time^1.5 $\alpha \cdot t^{3/2}$



6. Alpha * time^2 $\alpha \cdot t^2$



7. Alpha * time^C $\alpha \cdot t^C$



8. User Supplied Percents

A custom set of percents of alpha to be spent at each look may be input directly.

The O'Brien-Fleming Analog spends very little alpha or beta at the beginning and much more at the final looks. The Pocock Analog and (Alpha or Beta)(Time) spending functions spend alpha or beta more evenly across the looks. The Hwang-Shih-DeCani (C) (gamma family) spending functions and (Alpha or Beta)(Time^C) spending functions are flexible spending functions that can be used to spend more alpha or beta early or late or evenly, depending on the choice of C.

Example 1 – Power and Output

A clinical trial is to be conducted over a two-year period to compare the mean response of a new treatment to that of the current treatment. The current response mean is 108. Although the researchers do not know the true mean of the new treatment, they would like to examine the power that is achieved if the mean of the new treatment is 113. The standard deviation for both groups is assumed to be 25. The sample size at the final look is to be 500 per group. Testing will be done at the 0.05 significance level. A total of five tests are going to be performed on the data as they are obtained. The O'Brien-Fleming (Analog) boundaries will be used.

Find the power and test boundaries assuming equal sample sizes per arm and two-sided hypothesis tests.

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 1** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Solve For	Power
Test Type	T-Test
Alternative Hypothesis	Mean1 - Mean2 ≠ Diff0
Simulations	20000
Random Seed	3357968 (for Reproducibility)
Alpha	0.05
Group Allocation	Equal (N1 = N2)
Sample Size Per Group	500
Grp 1 (Cntrl) Distribution H0	Normal(M0 S)
Grp 1 (Cntrl) Distribution H1	Normal(M0 S)
Grp 2 (Trt) Distribution H0	Normal(M0 S)
Grp 2 (Trt) Distribution H1	Normal(M1 S)
M0 (Mean H0) Parameter Value(s)	108
M1 (Mean H1) Parameter Value(s)	113
Parameter 1 Label	S
Parameter 1 Value(s)	25
Looks & Boundaries Tab	
Specification of Looks and Boundaries	Simple
Number of Equally Spaced Looks	5
Alpha Spending Function	O'Brien-Fleming Analog

Output

Click the Calculate button to perform the calculations and generate the following output.

Scenario 1 Numeric Results for Group Sequential Testing Mean Difference = Diff0

Solve For: Power

Hypotheses: H0: Diff1 = Diff0; H1: Diff1 ≠ Diff0 H0 Distributions: Normal(M0 S) & Normal(M0 S) H1 Distributions: Normal(M0 S) & Normal(M1 S)

Test Statistic: T-Test

Alpha-Spending Function: O'Brien-Fleming Analog

Beta-Spending Function: None
Futility Boundary Type: None
Number of Looks: 5
Simulations: 20000
Pool Size: 40000

Random Seed: 3357968 (User-Entered)

Numeric Summary for Scenario 1

Power				Alpha					
Value	95% LCL	95% UCL	Target	Actual	95% LCL	95% UCL	Beta		
0.8829	0.8784	0.8873	0.05	0.053	0.05	0.056	0.1172		

		,	Average S	ample Siz	е						
		Give	en H0	Give	en H1						
N1	N2	Grp1	Grp2	Grp1	Grp2	Diff0	Diff1	МО	M1	S	
500	500	497	497	380	380	0	-5	108	113	25	
Power					ion of alter	jecting a fals					
Power	95% LCL	and UCL		The lowe	r and uppe	r confidence			estimate. T	he width o	f the
Target	Alpha					robability of			ypothesis	. It is the to	tal alpha
Alpha	or Actual A	Alpha		The alph	ion of the n	was actually ull hypothes					
Alpha	95% LCL	and UCL		The lowe	r and uppe	r confidence			Ipha estim	nate. The w	idth of the
Beta				The prob	ability of ac	cepting a fa	lse null hyp	othesis. It			
N1 and	d N2				<i>,</i> ,	each group			J		
Averaç	ge Sample	Size Given	n H0	on the	proportion (ected sampl of null hypot at each look	hesis simula				
Averag	ge Sample	Size Given	n H1	on the	proportion of	ected sampl of alternative es at each lo	e hypothesis				
H0 Diff	fO			The mea H0.	n difference	e between g	roups (Grp1	- Grp2) a	ssuming t	he null hyp	othesis,
H1 Diff	f1				n difference esis, H1.	e between g	roups (Grp1	- Grp2) a	ssuming t	he alternat	ive
The pa	arameters	to the right	of H1 Diff1	The para	,	were set by tions.	the user to	define the	e null and	alternative	

Group-Sequential Tests for Two Means (Simulation) (Legacy)

Summary Statements

A group sequential trial with sample sizes of 500 and 500 at the final look achieves 88% power to detect a difference of 5 between the null hypothesis mean difference of 0 and the actual mean difference of -5 at the 0.053 significance level (alpha) using a two-sided T-Test. These results are based on 20000 simulations (Monte Carlo samples) from the null distributions: Normal(M0 S) and Normal(M0 S), and the alternative distributions: Normal(M0 S) and Normal(M1 S).

Accumulated Information Details for Scenario 1

	Accumulated Information	Accumu	lated Sample	Size
Look	Percent	Group 1	Group 2	Total
1	20	100	100	200
2	40	200	200	400
3	60	300	300	600
4	80	400	400	800
5	100	500	500	1000

Look

Accumulated Information Percent Accumulated Sample Size Group 1 Accumulated Sample Size Group 2 Accumulated Sample Size Total The number of the look.

The percent of the sample size accumulated up to the corresponding look.

The total number of individuals in group 1 at the corresponding look.

The total number of individuals in group 2 at the corresponding look.

The total number of individuals in the study (group 1 + group 2) at the corresponding look.

Boundaries for Scenario 1

	Significance	Boundary
Look	T-Value Scale	P-Value Scale
1	+/- 3.93425	0.00012
2	+/- 3.39829	0.00075
3	+/- 2.74342	0.00626
4	+/- 2.25134	0.02464
5	+/- 1.99317	0.04651

Look

Significance Boundary T-Value Scale

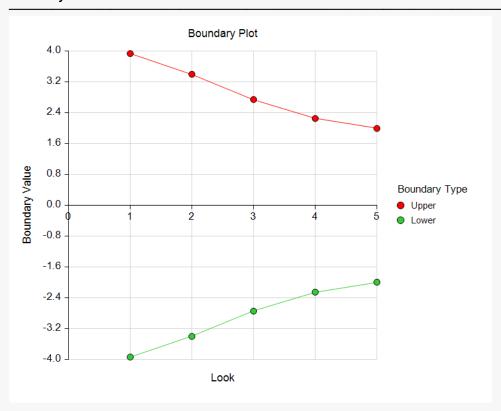
The number of the look.

The value such that statistics outside this boundary at the corresponding look indicate termination of the study and rejection of the null hypothesis. They are sometimes called efficacy boundaries.

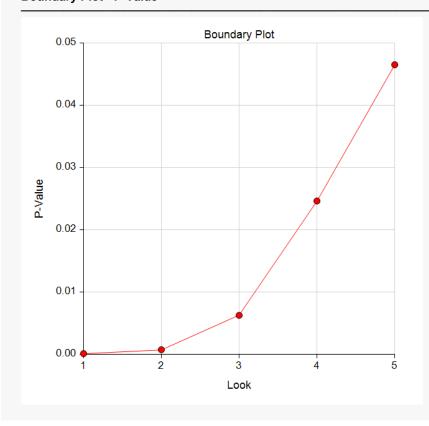
Significance Boundary P-Value Scale

The value such that P-Values outside this boundary at the corresponding look indicate termination of the study and rejection of the null hypothesis. This P-Value corresponds to the T-Value Boundary and is sometimes called the nominal alpha.

Boundary Plot



Boundary Plot - P-Value



Significance Boundaries with 95% Simulation Confidence Intervals for Scenario 1

	T-	Value Boundar	у	P	P-Value Boundary				
Look	Value	95% LCL	95% UCL	Value	95% LCL	95% UCL			
	+/- 3.93425			0.00012					
<u>)</u>	+/- 3.39829	-3.73753	-3.27404	0.00075	0.00021	0.00115			
3	+/- 2.74342	-2.82815	-2.67388	0.00626	0.00484	0.00770			
4	+/- 2.25134	-2.32286	-2.19529	0.02464	0.02044	0.02843			
5	+/- 1.99317	-2.03193	-1.96006	0.04651	0.04242	0.05027			
.ook		The number of	the look.						
-Value	Boundary Value		that statistics ound rejection of the						
P-Value	Boundary Value	•	that P-Values ou		•				

of the study and rejection of the null hypothesis. This P-Value corresponds to the T-Value Boundary and is sometimes called the nominal alpha.

95% LCL and UCL

The lower and upper confidence limits for the boundary at the given look. The width of the interval is based on the number of simulations.

			Tar	rget	Ac	tual	D	0
	Signif. Bo	undary	Spending	Cum. Spending		Cum.	Proportion H1 Sims Outside	Cum. H1 Sims Outside
Look	T-Value Scale	P-Value Scale	Function Alpha	Function Alpha	Alpha Spent	Alpha Spent	Signif. Boundary	Signif. Boundary
1	+/- 3.93425	0.00012	0.000	0.000	0.000	0.000	0.0065	0.0065
2	+/- 3.39829	0.00075	0.001	0.001	0.001	0.001	0.0783	0.0848
3	+/- 2.74342	0.00626	0.007	0.008	0.006	0.007	0.3023	0.3871
4	+/- 2.25134	0.02464	0.017	0.024	0.019	0.026	0.3320	0.7190
5	+/- 1.99317	0.04651	0.026	0.050	0.026	0.053	0.1639	0.8829
Look	ance Boundary T-	Valua Saala		The number of		tion outside	this boundary at t	·ho
Significa	ance boundary 1-	Value Scale					ition of the study a	
							times called effica	
Significa	ance Boundary P-	-Value Scale					this boundary at	
				•	-		tion of the study a	•
				, ,			orresponds to the s called the nomin	U
Spendir	ng Function Alpha	l					ed to the particula	
				the alpha-sp				
Cumula	tive Spending Fu	nction Alpha					cated to the partic Alpha up to the co	
Alpha S	pent						simulations result	ing in statistics

Cumulative Alpha Spent

Proportion H1 Sims Outside Significance Boundary

Cumulative H1 Sims Outside Significance Boundary

outside the Significance Boundary at this look.

The proportion of the null hypothesis simulations resulting in Significance Boundary termination up to and including this look. It is the sum of the Alpha Spent up to the corresponding look.

The proportion of the alternative hypothesis simulations resulting in statistics outside the Significance Boundary at this look. It may be thought of as the incremental power.

The proportion of the alternative hypothesis simulations resulting in Significance Boundary termination up to and including this look. It is the sum of the Proportion H1 Sims Outside Significance Boundary up to the corresponding look.

Group-Sequential Tests for Two Means (Simulation) (Legacy)

Numeric Results for Group Sequential Testing Mean Difference = Diff0.

Solve For: Power

 $\begin{array}{lll} \mbox{Hypotheses:} & \mbox{H0: Diff1 = Diff0; H1: Diff1 \neq Diff0} \\ \mbox{H0 Distributions:} & \mbox{Normal(M0 S) & Normal(M0 S)} \\ \mbox{H1 Distributions:} & \mbox{Normal(M0 S) & Normal(M1 S)} \\ \end{array}$

Test Statistic: T-Test

Alpha-Spending Function: O'Brien-Fleming Analog

Beta-Spending Function: None
Futility Boundary Type: None
Number of Looks: 5
Simulations: 20000
Pool Size: 40000

Random Seed: 3357968 (User-Entered)

Numeric Summary of Scenarios

Scenario	Power	N1	N2	Alpha	Diff0	H1 Diff1	МО	M1	s	
1	0.8829	500	500	0.053	0	-5	108	113	25	
Power			pr		, .					s. It is the total e significance
Alpha			pr	alpha level to oportion of the oundaries.		•	•	•		
N1 and N2 H0 Diff0				sample size	_	•	•			ull hypothesis.

H0.

The mean difference between groups (Grp1 - Grp2) assuming the alternative

hypothesis, H1.

The parameters to the right of H1 Diff1 The parameters that were set by the user to define the null and alternative

simulation distributions.

Power and Alpha Summary

H1 Diff1

		Power				Alpha		
Scenario	Value	95% LCL	95% UCL	Target	Actual	95% LCL	95% UCL	Beta
1 (0.8829	0.8784	0.8873	0.05	0.053	0.05	0.056	0.1172
Power			lity of rejecting a				It is the total proboundaries.	portion of
Power 95% LCI	and UCL		nd upper confidence of the con		r the power e	estimate. The wi	dth of the interva	al is based
Target Alpha		The user-sp	ecified probabili	ty of rejecting	g a true null h	nypothesis. It is	the total alpha sp	ent.
Alpha or Actual	Alpha		evel that was act s simulations tha				total proportion	of the null
Alpha 95% LCL	and UCL		nd upper confident the number of si		r the actual a	alpha estimate.	The width of the	interval is
Beta			lity of accepting s simulations that				ortion of alternat s.	tive

Group-Sequential Tests for Two Means (Simulation) (Legacy)

Sample Size Summary

						Average S	ample Siz	:e	
					Give	en H0	Give	en H1	•
Scenario	Power	Alpha	N1	N2	Grp1	Grp2	Grp1	Grp2	•
1	0.8829	0.053	500	500	497	497	380	380	-
Power			•	,		, pourioc	5110 01		s. It is the total
Alpha		bo The	oundaries. alpha lev	el that was	s actually ac	chieved by th	ne experime	ent. It is the	e significance e total proportion of
Alpha N1 and N2		bo The th	oundaries. alpha lev e null hype	el that was othesis sin	s actually ac	chieved by that are outside	ne experime le the signifi	ent. It is the	e total proportion of
N1 and N2	nple Size Give	bo The the The en H0 The pr	oundaries. alpha lev e null hype sample s average o	el that was othesis sin izes of eac or expecte of null hypo	s actually ac nulations the ch group if the d sample si	chieved by the at are outsice he study read zes of each	ne experime le the signifi iches the fin group if H0	ent. It is the cance bot al look. is true. Th	e total proportion of

Run Time: 27.89 seconds.

References

Jennison, C., Turnbull, B.W. 2000. Group Sequential Methods with Applications to Clinical Trials. Chapman & Hall. Boca Raton, FL.

Devroye, Luc. 1986. Non-Uniform Random Variate Generation. Springer-Verlag. New York.

Matsumoto, M. and Nishimura, T. 1998. 'Mersenne twister: A 623-dimensionally equidistributed uniform pseudorandom number generator.' ACM Trans. On Modeling and Computer Simulations.

Zar, Jerrold H. 1984. Biostatistical Analysis (Second Edition). Prentice-Hall. Englewood Cliffs, New Jersey.

The values obtained from any given run of this example will vary slightly due to the variation in simulations.

Example 2 – Power for One-Sided Test with Futility Boundaries

Suppose researchers would like to compare two treatments with a one-sided test at each look. Further, suppose they would like to terminate the study early when it can be deemed highly unlikely that the new treatment is better than the standard. Suppose the control group mean is 108. The researchers wish to know the power of the test if the treatment group mean is 113. The sample size at the final look is to be 500 per group. Testing will be done at the 0.05 significance level. A total of five tests are going to be performed on the data as they are obtained. The O'Brien-Fleming (Analog) boundaries will be used for both significance and futility boundaries.

Find the power and test boundaries assuming equal sample sizes per arm and one-sided hypothesis tests.

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 2** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Solve For	Power
Test Type	T-Test
Alternative Hypothesis	Mean1 - Mean2 < Diff0
Simulations	20000
Random Seed	3435689 (for Reproducibility)
Alpha	0.05
Group Allocation	Equal (N1 = N2)
Sample Size Per Group	500
Grp 1 (Cntrl) Distribution H0	Normal(M0 S)
Grp 1 (Cntrl) Distribution H1	Normal(M0 S)
Grp 2 (Trt) Distribution H0	Normal(M0 S)
Grp 2 (Trt) Distribution H1	Normal(M1 S)
M0 (Mean H0) Parameter Value(s)	108
M1 (Mean H1) Parameter Value(s)	113
Parameter 1 Label	S
Parameter 1 Value(s)	25
Looks & Boundaries Tab	
Specification of Looks and Boundaries	Simple
Number of Equally Spaced Looks	5
Alpha Spending Function	O'Brien-Fleming Analog
Type of Futility Boundary	Non-binding
Number of Skipped Futility Looks	0
Beta Spending Function	O'Brien-Fleming Analog

Output

Click the Calculate button to perform the calculations and generate the following output.

Scenario 1 Numeric Results for Group Sequential Testing Mean Difference = Diff0

Solve For: Power

Hypotheses: H0: Diff1 = Diff0; H1: Diff1 < Diff0 H0 Distributions: Normal(M0 S) & Normal(M0 S) H1 Distributions: Normal(M0 S) & Normal(M1 S)

Test Statistic: T-Test

Alpha-Spending Function: O'Brien-Fleming Analog Beta-Spending Function: O'Brien-Fleming Analog

Futility Boundary Type: Non-Binding

Number of Looks: 5 Simulations: 20000 Pool Size: 40000

Random Seed: 3435689 (User-Entered)

Numeric Summary for Scenario 1

Power				Alpha				
Value	95% LCL	95% UCL	Target	Actual	95% LCL	95% UCL	Beta	
0.9153	0.9114	0.9192	0.05	0.045	0.042	0.048	0.0847	

			Average S	ample Siz	е					
		Give	n H0	Give	n H1					
N1	N2	Grp1	Grp2	Grp1	Grp2	Diff0	Diff1	MO	M1	s
500	500	306	306	335	335	0	-5	108	113	25

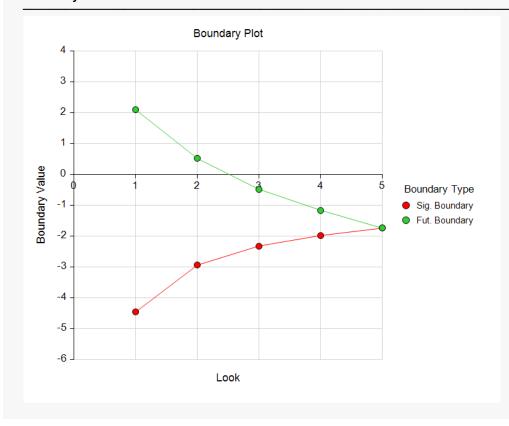
Accumulated Information Details for Scenario 1

	Accumulated Information	Accumu	ulated Sample	Size
Look	Percent	Group 1	Group 2	Total
1	20	100	100	200
2	40	200	200	400
3	60	300	300	600
4	80	400	400	800
5	100	500	500	1000

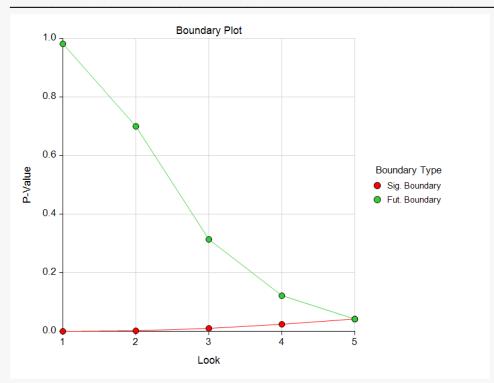
Boundaries for Scenario 1

	Significanc	e Boundary	Futility B	Boundary
Look	T-Value Scale	P-Value Scale	T-Value Scale	P-Value Scale
1	-4.45275	0.00001	2.10108	0.98155
2	-2.93228	0.00178	0.52459	0.69992
3	-2.32642	0.01016	-0.48477	0.31401
4	-1.98034	0.02400	-1.16769	0.12164
5	-1.73123	0.04186	-1.73123	0.04186

Boundary Plot



Boundary Plot - P-Value



Significance Boundaries with 95% Simulation Confidence Intervals for Scenario 1

	T-	-Value Bounda	ary	P-Value Boundary				
Look	Value	95% LCL	95% UCL	Value	95% LCL	95% UCL		
1	-4.45275			0.00001				
2	-2.93228	-3.05685	-2.82278	0.00178	0.00119	0.00250		
3	-2.32642	-2.37620	-2.26510	0.01016	0.00890	0.01193		
4	-1.98034	-2.01571	-1.94272	0.02400	0.02208	0.02620		
5	-1.73123	-1.75693	-1.70208	0.04186	0.03962	0.04453		

Futility Boundaries with 95% Simulation Confidence Intervals for Scenario 1

	T	-Value Bounda	ary	P	-Value Bound	ary
Look	Value	95% LCL	95% UCL	Value	95% LCL	95% UCL
1	2.10108			0.98155		
2	0.52459	0.47378	0.57327	0.69992	0.68204	0.71661
3	-0.48477	-0.51881	-0.44443	0.31401	0.30204	0.32845
4	-1.16769	-1.19474	-1.13772	0.12164	0.11627	0.12779
5	-1.73123	-1.75962	-1.70644	0.04186	0.03939	0.04412

Alpha-Spending and Null Hypothesis Simulation Details for Scenario 1

			Tar	get	Ac	tual	D	•
	Signif. B	oundary	Spending	Cum. Spending		Cum.	Proportion H0 Sims Outside	Cum. H0 Sims Outside
Look	T-Value Scale	P-Value Scale	Function Alpha	Function Alpha	Alpha Spent	Alpha Spent	Futility Boundary	Futility Boundary
1	-4.45275	0.00001	0.000	0.000	0.000	0.000	0.018	0.018
2	-2.93228	0.00178	0.002	0.002	0.002	0.002	0.289	0.307
3	-2.32642	0.01016	0.009	0.011	0.009	0.011	0.383	0.691
4	-1.98034	0.02400	0.017	0.028	0.017	0.028	0.194	0.885
5	-1.73123	0.04186	0.022	0.050	0.017	0.045	0.070	0.955

Beta-Spending and Alternative Hypothesis Simulation Details for Scenario 1

			Taı	rget	Ac	tual	D	0
	Futility B	Soundary	Spending	Cum. Spending		Cum.	Proportion H1 Sims Outside	Cum. H1 Sims Outside
Look	T-Value Scale	P-Value Scale	Function Beta	Function Beta	Beta Spent	Beta Spent	Signif. Boundary	Signif. Boundary
1	2.10108	0.98155	0.0001	0.0001	0.0001	0.0001	0.0014	0.0014
2	0.52459	0.69992	0.0063	0.0065	0.0064	0.0065	0.1829	0.1843
3	-0.48477	0.31401	0.0197	0.0262	0.0197	0.0262	0.3785	0.5627
4	-1.16769	0.12164	0.0280	0.0541	0.0280	0.0541	0.2490	0.8117
5	-1.73123	0.04186	0.0309	0.0850	0.0306	0.0847	0.1036	0.9153

The values obtained from any given run of this example will vary slightly due to the variation in simulations.

Example 3 - Enter Boundaries

With a set-up similar to Example 2, suppose we wish to investigate the properties of a set of significance (-3, -3, -2, -1) and futility (2, 1, 0, 0, -1) boundaries.

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 3** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Solve For	Alpha and Power (Enter Boundaries)
Test Type	T-Test
Alternative Hypothesis	Mean1 - Mean2 < Diff0
Simulations	20000
Random Seed	3470742 (for Reproducibility)
Group Allocation	Equal (N1 = N2)
Sample Size Per Group	500
Grp 1 (Cntrl) Distribution H0	Normal(M0 S)
Grp 1 (Cntrl) Distribution H1	Normal(M0 S)
Grp 2 (Trt) Distribution H0	Normal(M0 S)
Grp 2 (Trt) Distribution H1	Normal(M1 S)
M0 (Mean H0) Parameter Value(s)	108
M1 (Mean H1) Parameter Value(s)	113
Parameter 1 Label	S
Parameter 1 Value(s)	25
Looks & Boundaries Tab	
Number of Looks	5
Equally Spaced	Checked
	Significance and Futility Boundaries
Significance Boundary	-3 -3 -3 -2 -1 (for looks 1 through 5)
Futility Boundary	2 1 0 0 -1 (for looks 1 through 5)

Output

Click the Calculate button to perform the calculations and generate the following output.

Scenario 1 Numeric Results for Group Sequential Testing Mean Difference = Diff0

Solve For: Alpha and Power (Enter Boundaries)
Hypotheses: H0: Diff1 = Diff0; H1: Diff1 < Diff0
H0 Distributions: Normal(M0 S) & Normal(M0 S)
H1 Distributions: Normal(M0 S) & Normal(M1 S)

Test Statistic: T-Test

Type of Boundaries: Significance and Futility Boundaries

Number of Looks: 5 Simulations: 20000 Pool Size: 40000

Random Seed: 3470742 (User-Entered)

Numeric Summary for Scenario 1

	Power			Alpha				
Value	95% LCL	95% UCL	Value	95% LCL	95% LCL	Beta		
0.9799	0.978	0.9818	0.149	0.144	0.154	0.0201		

			Average S	ample Siz	e					
		Give	en H0	Give	n H1					
N1	N2	Grp1	Grp2	Grp1	Grp2	Diff0	Diff1	МО	M1	S
500	500	367	367	364	364	0	-5	108	113	25

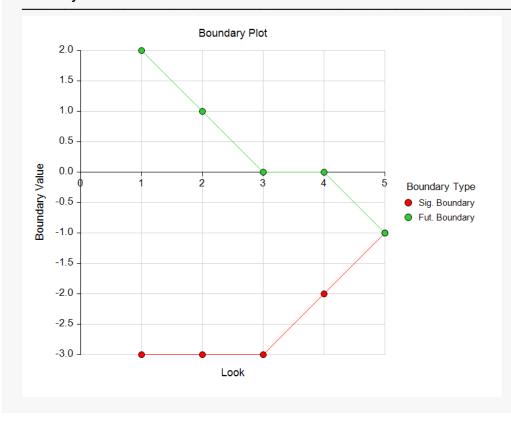
Accumulated Information Details for Scenario 1

	Accumulated Information	Accumu	ulated Sample	Size
Look	Percent	Group 1	Group 2	Total
1	20	100	100	200
2	40	200	200	400
3	60	300	300	600
4	80	400	400	800
5	100	500	500	1000

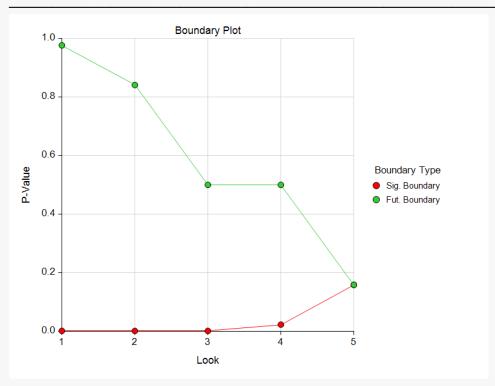
Boundaries for Scenario 1

	Significand	e Boundary	Futility E	Boundary
Look	T-Value Scale	P-Value Scale	T-Value Scale	P-Value Scale
1	-3	0.00152	2	0.97657
2	-3	0.00143	1	0.84104
3	-3	0.00141	0	0.50000
4	-2	0.02292	0	0.50000
5	-1	0.15878	-1	0.15878

Boundary Plot



Boundary Plot - P-Value



Alpha-Spending and Null Hypothesis Simulation Details for Scenario 1

	Signif. E	Soundary		0	Proportion H0 Sims	Cum. H0 Sims	
Look	T-Value Scale	P-Value Scale	Alpha Spent	Cum. Alpha Spent	Outside Futility Boundary	Outside Futility Boundary	
1	-3	0.00152	0.002	0.002	0.022	0.022	
2	-3	0.00143	0.001	0.003	0.148	0.170	
3	-3	0.00141	0.001	0.004	0.341	0.511	
4	-2	0.02292	0.022	0.026	0.082	0.593	
5	-1	0.15878	0.123	0.149	0.258	0.851	

Beta-Spending and Alternative Hypothesis Simulation Details for Scenario 1

	Futility E	Boundary		•	Proportion H1 Sims	Cum. H1 Sims	
Look	T-Value Scale	P-Value Scale	Beta Spent	Cum. Beta Spent	Outside Signif. Boundary	Outside Signif. Boundary	
1	2	0.97657	0.0004	0.0004	0.0580	0.0580	
2	1	0.84104	0.0019	0.0023	0.1166	0.1746	
3	0	0.50000	0.0055	0.0078	0.1431	0.3176	
4	0	0.50000	0.0010	0.0088	0.4731	0.7907	
5	-1	0.15878	0.0113	0.0201	0.1892	0.9799	

The values obtained from any given run of this example will vary slightly due to the variation in simulations.

Example 4 - Validation Using Simulation

With a set-up similar to Example 1, we examine the power and alpha generated by the set of two-sided significance boundaries (+/- 4.0302, +/- 3.3336, +/- 2.7016, +/- 2.2941, +/- 2.0350).

Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 4** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

Solve For	Alpha and Power (Enter Boundaries)
Test Type	T-Test
Alternative Hypothesis	Mean1 - Mean2 ≠ Diff0
Simulations	20000
Random Seed	3504339 (for Reproducibility)
Group Allocation	Equal (N1 = N2)
Sample Size Per Group	500
Grp 1 (Cntrl) Distribution H0	Normal(M0 S)
Grp 1 (Cntrl) Distribution H1	Normal(M0 S)
Grp 2 (Trt) Distribution H0	Normal(M0 S)
Grp 2 (Trt) Distribution H1	Normal(M1 S)
M0 (Mean H0) Parameter Value(s)	108
M1 (Mean H1) Parameter Value(s)	113
Parameter 1 Label	S
Parameter 1 Value(s)	25
Looks & Boundaries Tab	
Number of Looks	5
Equally Spaced	Checked
Significance Boundary	4.0302, 3.3336, 2.7016, 2.2941, 2.0350

Output

Click the Calculate button to perform the calculations and generate the following output.

Scenario 1 Numeric Results for Group Sequential Testing Mean Difference = Diff0

Solve For: Alpha and Power (Enter Boundaries)
Hypotheses: H0: Diff1 = Diff0; H1: Diff1 ≠ Diff0
H0 Distributions: Normal(M0 S) & Normal(M0 S)
H1 Distributions: Normal(M0 S) & Normal(M1 S)

Test Statistic: T-Test

Type of Boundaries: Significance Boundaries Only

Number of Looks: 5 Simulations: 20000 Pool Size: 40000

Random Seed: 3504339 (User-Entered)

Numeric Summary for Scenario 1

Power						
Value	95% LCL	95% UCL	Value	95% LCL	95% LCL	Beta
0.8781	0.8736	0.8826	0.049	0.046	0.052	0.1219

			Average Sample Size							
		Give	en H0	Give	en H1					
N1	N2	Grp1	Grp2	Grp1	Grp2	Diff0	Diff1	МО	M1	s
500	500	496	496	378	378	0	-5	108	113	25

The values obtained from any given run of this example will vary slightly due to the variation in simulations. The power and alpha generated with these boundaries are very close to the values of Example 1.