

## Chapter 164

# Multi-Arm Superiority by a Margin Tests for the Ratio of Treatment and Control Proportions

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## Introduction

This module computes power and sample size for multi-arm, superiority by a margin tests of the ratio of treatment and control proportions. This procedure is based on the results in Machin, Campbell, Tan, and Tan (2018). In this design, there are  $k$  treatment groups and one control group. The groups are independent and are sampled using simple random sampling. A proportion is measured in each group. A total of  $k$  hypothesis tests are anticipated each comparing a treatment group with the common control group using a superiority by a margin test of the ratio of two proportions.

The Bonferroni multiplicity adjustment of the type I error rate may be optionally made because several tests are being constructed from the same data. Making a multiplicity adjustment is usually recommended, but not always. In fact, Saville (1990) advocates not applying it and Machin, Campbell, Tan, and Tan (2018) include omitting it as a possibility.

Whether you want to test several doses of a single treatment or several types of treatments, good research practice requires that each treatment be compared with a control. For example, a popular three-arm design consists of three groups: control, treatment A, and treatment B. Two tests are run: treatment A versus control and treatment B versus the same control. This avoids having to obtain a second control group for treatment B. Besides the obvious efficiency in subjects, it may be easier to recruit subjects if their chances of receiving a new treatment are better than 50%.

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## Example

Suppose that the current treatment for a disease works 60% of the time. Unfortunately, this treatment is expensive and occasionally exhibits serious side-effects. Two promising new treatments have been developed and are now ready to be tested. Hence, three groups are needed to complete this study. Two superiority by a margin hypotheses need to be tested in this study: whether each new treatment is better than the current treatment.

Because of the costs of switching to a new treatment, clinicians will only recommend it if it is definitely more effective than the current treatment. They must determine, however, how much more effective the new treatment must be to be adopted. Should it be adopted if its ratio with the control group is 1.05? 1.1? 1.25? There is a ratio that is so low that decrease in response is no longer ignorable. In this example, after thoughtful discussion with several clinicians, it was decided that if the response ratio is at least 1.25, the new treatment will be adopted. The ratio between these two percentages is called the *superiority ratio* ( $R_0$ ).

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The developers must design an experiment to test the hypothesis that the response rate ratio is at least 1.25. The statistical hypotheses to be tested are

$$H_0: P_A/P_C \leq R_0 \quad \text{vs.} \quad H_1: P_A/P_C > R_0$$

$$H_0: P_B/P_C \leq R_0 \quad \text{vs.} \quad H_1: P_B/P_C > R_0$$

where  $R_0 = 1.25$ .

Notice that when the null hypothesis is rejected, the conclusion is that the ratio is higher than 1.25. Note that even though the response rate of the current treatment is 0.60, the hypothesis test is about a response rate ratio of 1.25. This results in a response rate boundary of  $0.6(1.25) = 0.75$ .

## Technical Details

Suppose you have  $k$  treatment groups with response probabilities  $P_i$  of size  $N_i$  and one control group with response probability  $P_C$  of size  $N_C$ . The total sample size is  $N = N_1 + N_2 + \dots + N_k + N_C$ .

The  $k$  one-sided superiority tests are

$$H_{0i}: P_i/P_C \leq R_0 \quad \text{vs.} \quad H_{1i}: P_i/P_C > R_0 \quad \text{for } i = 1, 2, \dots, k$$

Note that if higher proportions are better,  $R_0 > 1$  and if lower proportions are better,  $R_0 < 1$ .

If we define  $R_i = P_i/P_C$ , these are equivalent to

$$H_{0i}: R_i \leq R_0 \quad \text{vs.} \quad H_{1i}: R_i > R_0 \quad \text{for } i = 1, 2, \dots, k$$

For convenience, these hypotheses are collectively referred to as

$$H_0: R \leq R_0 \quad \text{vs.} \quad H_1: R > R_0$$

## Test Statistics

Three test statistics are available in this procedure.

### Miettinen and Nurminen's Likelihood Score Test

Miettinen and Nurminen (1985) proposed a test statistic for testing whether the ratio is equal to a specified value  $R_0$ . The regular MLE's,  $\hat{p}_i$  and  $\hat{p}_C$ , are used in the numerator of the score statistic while MLE's  $\tilde{p}_i$  and  $\tilde{p}_C$ , constrained so that  $\tilde{p}_i / \tilde{p}_C = R_0$ , are used in the denominator. A correction factor of  $N/(N-1)$  is applied to make the variance estimate less biased. The significance level of the test statistic is based on the asymptotic normality of the score statistic.

The formula for computing the test statistic is

$$z_{MNR} = \frac{\hat{p}_i / \hat{p}_C - R_0}{\sqrt{\left( \frac{\tilde{p}_i \tilde{q}_i}{N_i} + R_0^2 \frac{\tilde{p}_C \tilde{q}_C}{N_C} \right) \left( \frac{N}{N-1} \right)}}$$

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where

$$\tilde{p}_i = \tilde{p}_c R_0$$

$$\tilde{p}_c = \frac{-B - \sqrt{B^2 - 4AC}}{2A}$$

$$A = NR_0$$

$$B = -[N_i R_0 + x_{11} + N_c + x_{21} R_0]$$

$$C = m_1$$

$$m_1 = \text{number of successes}$$

### Farrington and Manning's Likelihood Score Test

Farrington and Manning (1990) proposed a test statistic for testing whether the ratio is equal to a specified value  $R_0$ . The regular MLE's,  $\hat{p}_i$  and  $\hat{p}_c$ , are used in the numerator of the score statistic while MLE's  $\tilde{p}_i$  and  $\tilde{p}_c$ , constrained so that  $\tilde{p}_i / \tilde{p}_c = R_0$ , are used in the denominator. The significance level of the test statistic is based on the asymptotic normality of the score statistic.

The formula for computing the test statistic is

$$z_{FMR} = \frac{\hat{p}_i / \hat{p}_c - R_0}{\sqrt{\left( \frac{\tilde{p}_i \tilde{q}_i}{N_i} + R_0^2 \frac{\tilde{p}_c \tilde{q}_c}{N_c} \right)}}$$

where the estimates  $\tilde{p}_i$  and  $\tilde{p}_c$  are computed as in the corresponding test of Miettinen and Nurminen (1985) given above.

### Gart and Nam's Likelihood Score Test

Gart and Nam (1988), page 329, proposed a modification to the Farrington and Manning (1988) ratio test that corrects for skewness. Let  $z_{FMR}(R)$  stand for the Farrington and Manning ratio test statistic described above. The skewness corrected test statistic,  $z_{GNR}$ , is the appropriate solution to the quadratic equation

$$(-\tilde{\varphi})z_{GNR}^2 + (-1)z_{GNR} + (z_{FMR}(R) + \tilde{\varphi}) = 0$$

where

$$\tilde{\varphi} = \frac{1}{6\tilde{u}^{3/2}} \left( \frac{\tilde{q}_i(\tilde{q}_i - \tilde{p}_i)}{N_i^2 \tilde{p}_i^2} - \frac{\tilde{q}_c(\tilde{q}_c - \tilde{p}_c)}{N_c^2 \tilde{p}_c^2} \right)$$

$$\tilde{u} = \frac{\tilde{q}_i}{N_i \tilde{p}_i} + \frac{\tilde{q}_c}{N_c \tilde{p}_c}$$

## Asymptotic Approximation to Power

A large sample approximation is used to compute power. The large sample approximation is made by replacing the values of  $\hat{p}_i$  and  $\hat{p}_c$  in the z statistic with the corresponding values of  $P_i$  and  $P_c$ , and then computing the results based on the normal distribution. Note that in large samples, the Farrington and Manning statistic is substituted for the Gart and Nam statistic.

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## Multiplicity Adjustment

Because  $k$  z-tests between treatment groups and the control group are run when analyzing the results of this study, many statisticians recommend that the Bonferroni adjustment be applied. This adjustment is easy to apply: the value of alpha that is used in the test is found by dividing the original alpha by the number of tests. For example, if the original alpha is set at 0.05 and the number of treatment (not including the control) groups is five, the individual tests will be conducted using an alpha of 0.01.

The main criticism of this procedure is that if there are many tests, the value of alpha becomes very small. To mitigate against this complaint, some statisticians recommend separating the treatment groups into those that are of primary interest and those that are of secondary interest. The Bonferroni adjustment is made by the using the number of primary treatments rather than the total number of treatments.

There are some who advocate ignoring the adjustment entirely in the case of randomized clinical trials. See for example Saville (1990) and the discussion in chapter 14 of Machin, Campbell, Tan, and Tan (2018).

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## Size of the Control Group

Because the control group is used over and over, some advocate increasing the number of subjects in this group. The standard adjustment is to include  $\sqrt{k}$  subjects in the control group for each subject in one of the treatment groups. See Machin, Campbell, Tan, and Tan (2018, pages 231-232). Note that often, the treatment groups all have the same size.

## Example 1 – Finding the Sample Size

A parallel-group, clinical trial is being designed to compare three doses of a test compound with the current standard therapy using three superiority Miettinen and Nurminen Likelihood Scores tests. Suppose the standard therapy has a response rate of 0.6. The investigators would like a sample size large enough to find statistical significance at an overall 0.05 level and an individual-test power of 0.80. The superiority odds ratio is 1.15.

The response rates of treatment group 1 are set to 0.74, 0.76, 0.78. The response rate of group 2 is 0.8. The response rate of group 3 is 0.85.

Following common practice, the control-group sample-size multiplier will be set to  $\sqrt{k} = \sqrt{3} = 1.732$  since there are three treatment groups in this design.

### Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 1** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

#### Design Tab

Solve For .....	<b>Sample Size</b>
Higher Proportions Are .....	<b>Better (H1: R &gt; R0)</b>
Test Type .....	<b>Likelihood Score (Miet. &amp; Nurm.)</b>
Power of Each Test .....	<b>0.8</b>
Overall Alpha .....	<b>0.05</b>
Bonferroni Adjustment .....	<b>Standard Bonferroni</b>
Group Allocation .....	<b>Enter Group Allocation Pattern, solve for group sample sizes</b>
R0 (Superiority Ratio) .....	<b>1.15</b>
Control Proportion.....	<b>0.6</b>
Control Sample Size Allocation.....	<b>1.732</b>
Set A Number of Groups.....	<b>1</b>
Set A Proportion .....	<b>0.74 0.76 0.78</b>
Set A Sample Size Allocation .....	<b>1</b>
Set B Number of Groups.....	<b>1</b>
Set B Proportion .....	<b>0.8</b>
Set B Sample Size Allocation .....	<b>1</b>
Set C Number of Groups .....	<b>1</b>
Set C Proportion .....	<b>0.85</b>
Set C Sample Size Allocation .....	<b>1</b>
Set D Number of Groups .....	<b>0</b>
More.....	<b>Unchecked</b>

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## Output

Click the Calculate button to perform the calculations and generate the following output.

## Numeric Reports

## Numeric Results

Solve For: [Sample Size](#)  
 Group Allocation: Enter Group Allocation Pattern, solve for group sample sizes  
 Test Type: Miettinen & Nurminen Likelihood Score Test  
 Higher Proportions Are: Better  
 Hypotheses:  $H_0: R \leq R_0$  vs.  $H_1: R > R_0$   
 Number of Groups: 4  
 Bonferroni Adjustment: Standard Bonferroni (Divisor = 3)

Comparison	Power		Sample Size		Proportion		Ratio		Alpha	
	Target	Actual	Ni	Allocation	Pi H0 Pi.0	Pi H1 Pi.1	Superiority R0	Actual Ri	Overall	Bonferroni- Adjusted
Control			2335	1.732	0.60	0.60				
vs A	0.8	0.80027	1348	1.000	0.69	0.74	1.15	1.23333	0.05	0.016667
vs B	0.8	1.00000	1348	1.000	0.69	0.80	1.15	1.33333	0.05	0.016667
vs C	0.8	1.00000	1348	1.000	0.69	0.85	1.15	1.41667	0.05	0.016667
Total			6379							
Control			1169	1.732	0.60	0.60				
vs A	0.8	0.80002	675	1.000	0.69	0.76	1.15	1.26667	0.05	0.016667
vs B	0.8	0.99632	675	1.000	0.69	0.80	1.15	1.33333	0.05	0.016667
vs C	0.8	1.00000	675	1.000	0.69	0.85	1.15	1.41667	0.05	0.016667
Total			3194							
Control			695	1.732	0.60	0.60				
vs A	0.8	0.80091	401	1.000	0.69	0.78	1.15	1.30000	0.05	0.016667
vs B	0.8	0.94089	401	1.000	0.69	0.80	1.15	1.33333	0.05	0.016667
vs C	0.8	0.99976	401	1.000	0.69	0.85	1.15	1.41667	0.05	0.016667
Total			1898							

Comparison	The group that is involved in the comparison between the treatment and control displayed on this report line. The comparison is made using the ratio.
Target Power	The power desired. Power is probability of rejecting a false null hypothesis for this comparison. This power is of the comparison shown on this line only.
Actual Power	The power actually achieved.
Ni	The number of subjects in the ith group. The total sample size shown below the groups is equal to the sum of all individual group sample sizes.
Allocation	The group sample size allocation ratio of the ith group. The value on each row represents the relative number of subjects assigned to the group.
Pi.0	The response proportion in the ith group assumed by the null hypothesis, $H_0$ . Note that $Pi.0 = P_c \times R_0$ , where $P_c$ is the control group proportion.
Pi.1	The response proportion in the ith group at which the power is calculated.
R0	The superiority ratio is the ratio boundary between a treatment that is concluded to be superior and a treatment that is not concluded to be superior.
Ri	The ratio of the ith group proportion (Pi.1) and the control group proportion ( $P_c$ ) at which the power is calculated. The formula is $R_i = Pi.1 / P_c$ .
Overall Alpha	The probability of rejecting at least one of the comparisons in this experiment when each null hypothesis is true.
Bonferroni Alpha	The adjusted significance level at which each individual comparison is made.

## Summary Statements

A parallel, 4-group design (with one control group and 3 treatment groups) will be used to test whether the proportion for each treatment group is superior to the control group proportion by a margin, with a superiority ratio of 1.15 ( $H_0: R \leq 1.15$  vs.  $H_1: R > 1.15$ ,  $R = P_i / P_c$ ). In this study, higher proportions are considered to be better. The superiority-by-a-margin hypotheses will be evaluated using 3 one-sided, two-sample, Bonferroni-adjusted Miettinen & Nurminen Likelihood Score tests of the ratio, with an overall (experiment-wise) Type I error rate ( $\alpha$ ) of 0.05. The control group proportion is assumed to be 0.6. To detect the treatment proportions 0.74, 0.8, and 0.85 with at least 80% power for each test, the control group sample size needed will be 2335 and the number of needed subjects for the treatment groups will be 1348, 1348, and 1348 (totaling 6379 subjects overall).

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## Dropout-Inflated Sample Size

Group	Dropout Rate	Sample Size Ni	Dropout- Inflated Enrollment Sample Size Ni'	Expected Number of Dropouts Di
1	20%	2335	2919	584
2	20%	1348	1685	337
3	20%	1348	1685	337
4	20%	1348	1685	337
Total		6379	7974	1595
1	20%	1169	1462	293
2	20%	675	844	169
3	20%	675	844	169
4	20%	675	844	169
Total		3194	3994	800
1	20%	695	869	174
2	20%	401	502	101
3	20%	401	502	101
4	20%	401	502	101
Total		1898	2375	477

Group Lists the group numbers.

Dropout Rate The percentage of subjects (or items) that are expected to be lost at random during the course of the study and for whom no response data will be collected (i.e., will be treated as "missing"). Abbreviated as DR.

Ni The evaluable sample size for each group at which power is computed (as entered by the user). If Ni subjects are evaluated out of the Ni' subjects that are enrolled in the study, the design will achieve the stated power.

Ni' The number of subjects that should be enrolled in each group in order to obtain Ni evaluable subjects, based on the assumed dropout rate. Ni' is calculated by inflating Ni using the formula  $Ni' = Ni / (1 - DR)$ , with Ni' always rounded up. (See Julious, S.A. (2010) pages 52-53, or Chow, S.C., Shao, J., Wang, H., and Lokhnygina, Y. (2018) pages 32-33.)

Di The expected number of dropouts in each group.  $Di = Ni' - Ni$ .

## Dropout Summary Statements

Anticipating a 20% dropout rate, group sizes of 2919, 1685, 1685, and 1685 subjects should be enrolled to obtain final group sample sizes of 2335, 1348, 1348, and 1348 subjects.

## Multi-Arm Superiority by a Margin Tests for the Ratio of Treatment and Control Proportions

**References**

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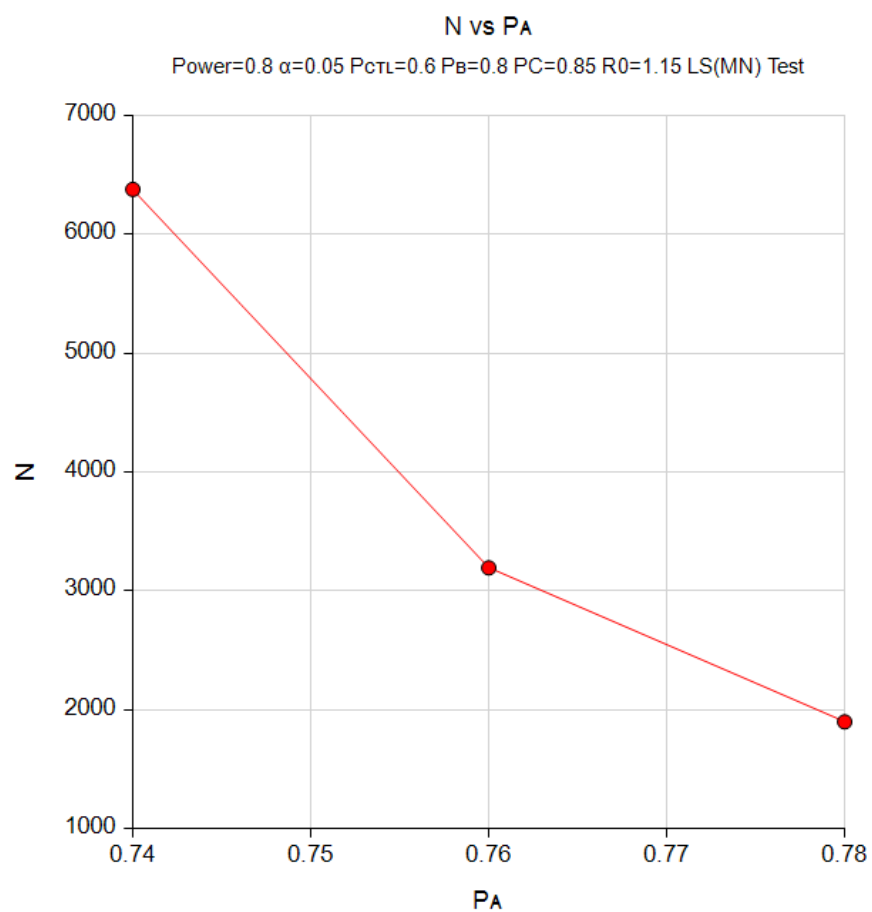
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This report shows the numeric results of this power study. Notice that the results are shown in blocks of three rows at a time. Each block represents a single design.



## Plots Section

### Plots



This plot gives a visual presentation of the results in the Numeric Report. We can quickly see the impact on the sample size of changing the expected value of the response rate for treatment 1.

## Example 2 – Validation using a Previously Validated Procedure

We could not find a validation result in the statistical literature, so we will use a previously validated **PASS** procedure (**Superiority by a Margin Tests for the Ratio of Two Proportions**) to produce the results for the following example.

Suppose a parallel-group, clinical trial is being designed to compare two doses of a test compound against the standard therapy using two superiority by a margin Miettinen and Nurminen Likelihood Scores tests. Suppose the standard therapy has a response rate of 0.60. The investigators would like a sample size large enough to find statistical significance at an overall 0.05 level and an individual-test power of 0.80. The response rates of groups 1 and 2 are 0.75 and 0.81, respectively. The superiority ratio is 1.15.

Following common practice, the control-group sample-size multiplier will be set to  $\sqrt{k} = \sqrt{2} \approx 1.4$  since there are two treatment groups in this design.

The **Superiority by a Margin Tests for the Ratio of Two Proportions** procedure is set up as follows.

### Design Tab

Solve For ..... **Sample Size**  
 Power Calculation Method ..... **Normal Approximation**  
 Higher Proportions Are ..... **Better (H1: P1/P2 > R0)**  
 Test Type ..... **Likelihood Score (Miet. & Nurm.)**  
 Power ..... **0.8**  
 Alpha ..... **0.025** (which is Alpha / k)  
 Group Allocation ..... **Enter R = N2/N1, solve for N1 and N2**  
 R ..... **1.4**  
 R0 (Superiority Ratio) ..... **1.15**  
 R1 (Actual Ratio) ..... **1.25 1.35**  
 P2 (Group 2 Proportion) ..... **0.6**

This set of options generates the following report.

### Numeric Results

Solve For: [Sample Size](#)  
 Groups: 1 = Treatment, 2 = Reference  
 Test Statistic: Miettinen & Nurminen Likelihood Score Test  
 Hypotheses: H0: P1 / P2 ≤ R0 vs. H1: P1 / P2 > R0

Power		Sample Size			R (Allocation Ratio)		Proportions			Ratio		
Target	Actual*	N1	N2	N	Target	Actual	Superiority P1.0	Actual P1.1	Reference P2	Superiority R0	Actual R1	Alpha
0.8	0.80001	915	1281	2196	1.4	1.4	0.69	0.75	0.6	1.15	1.25	0.025
0.8	0.80076	215	301	516	1.4	1.4	0.69	0.81	0.6	1.15	1.35	0.025

\* Power was computed using the normal approximation method.

In order to maintain a power of 80% for both groups, it is apparent that the groups will all need to have a sample size of 915 in the treatment groups and 1281 in the control group. We next calculate the powers of the two groups using these sample sizes. The results are displayed in the following table.

## Multi-Arm Superiority by a Margin Tests for the Ratio of Treatment and Control Proportions

## Numeric Results

Solve For: **Power**  
 Groups: 1 = Treatment, 2 = Reference  
 Test Statistic: Miettinen & Nurminen Likelihood Score Test  
 Hypotheses:  $H_0: P_1 / P_2 \leq R_0$  vs.  $H_1: P_1 / P_2 > R_0$

Power*	Sample Size			Proportions			Ratio		Alpha
	N1	N2	N	Superiority P1.0	Actual P1.1	Reference P2	Superiority R0	Actual R1	
0.80001	915	1281	2196	0.69	0.75	0.6	1.15	1.25	0.025
0.99995	915	1281	2196	0.69	0.81	0.6	1.15	1.35	0.025

\* Power was computed using the normal approximation method.

This table contains the validation values. We will now run these values through the current procedure and compare the results with these values.

## Setup

If the procedure window is not already open, use the PASS Home window to open it. The parameters for this example are listed below and are stored in the **Example 2** settings file. To load these settings to the procedure window, click **Open Example Settings File** in the Help Center or File menu.

## Design Tab

Solve For ..... **Sample Size**  
 Higher Proportions Are ..... **Better (H1: R > R0)**  
 Test Type ..... **Likelihood Score (Miet. & Nurm.)**  
 Power of Each Test ..... **0.8**  
 Overall Alpha ..... **0.05**  
 Bonferroni Adjustment ..... **Standard Bonferroni**  
 Group Allocation ..... **Enter Group Allocation Pattern, solve for group sample sizes**  
 R0 (Superiority Ratio) ..... **1.15**  
 Control Proportion ..... **0.6**  
 Control Sample Size Allocation ..... **1.4**  
 Set A Number of Groups ..... **1**  
 Set A Proportion ..... **0.75**  
 Set A Sample Size Allocation ..... **1**  
 Set B Number of Groups ..... **1**  
 Set B Proportion ..... **0.81**  
 Set B Sample Size Allocation ..... **1**  
 Set C Number of Groups ..... **0**  
 Set D Number of Groups ..... **0**  
 More ..... **Unchecked**

## Multi-Arm Superiority by a Margin Tests for the Ratio of Treatment and Control Proportions

## Output

Click the Calculate button to perform the calculations and generate the following output.

### Numeric Results

Solve For: [Sample Size](#)  
 Group Allocation: Enter Group Allocation Pattern, solve for group sample sizes  
 Test Type: Miettinen & Nurminen Likelihood Score Test  
 Higher Proportions Are: Better  
 Hypotheses:  $H_0: R \leq R_0$  vs.  $H_1: R > R_0$   
 Number of Groups: 3  
 Bonferroni Adjustment: Standard Bonferroni (Divisor = 2)

Comparison	Power		Sample Size		Proportion		Ratio		Alpha	
	Target	Actual	Ni	Allocation	Pi H0 Pi.0	Pi H1 Pi.1	Superiority R0	Actual Ri	Overall	Bonferroni- Adjusted
Control			1281	1.4	0.60	0.60				
vs A	0.8	0.80001	915	1.0	0.69	0.75	1.15	1.25	0.05	0.025
vs B	0.8	0.99995	915	1.0	0.69	0.81	1.15	1.35	0.05	0.025
Total			3111							

The sample sizes and powers match which validates this procedure.